Structure of the nucleon and its resonances

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July 2nd, 2018

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Baryon DAs

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Chapter 1: Dyson-Schwinger equations

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- Dyson-Schwinger equations relate Green (Schwinger) functions among each other.
- $\bullet\,$ One get in the case of QCD, an infinite system $\to\,$ truncations are required.
- DSEs are usually solved in Euclidean space, yielding Schwinger functions instead of Green functions.

(Although some works are performed to solve them directly in Minkowski space)



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Truncating the DSEs yields an non-perturbative approximation of QCD Schwinger functions.

The Gap Equation



• The gap equation for the quark propagator S(q):



The Gap Equation



• The gap equation for the quark propagator S(q):



• It has successfully described the quark mass behaviour:



- $S(q)^{-1} = i q A(q^2) + B(q^2)$
- Non-perturbative description of the quark mass
- Dynamical mass generation
- Figure from Bashir et al. (2012)

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• The Faddeev equation provides a covariant framework to describe the nucleon as a bound state of three dressed quarks.

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- Mostly two types of diquark are dynamically generated by the Faddeev equation:
 - ► Scalar diquarks, whose mass is roughly 2/3 of the nucleon mass,
 - Axial-Vector (AV) diquarks, whose mass is around 3/4 of the nucleon one.



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- Mostly two types of diquark are dynamically generated by the Faddeev equation:
 - ► Scalar diquarks, whose mass is roughly 2/3 of the nucleon mass,
 - Axial-Vector (AV) diquarks, whose mass is around 3/4 of the nucleon one.
- Can we understand the nucleon structure in terms of quark-diquarks correlations?

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Chapter 2: Baryon Distribution Amplitudes

CM, J. Segovia, L. Chang, C.D. Roberts, arXiv:1711.09101

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Hadrons seen as Fock States



• Lightfront quantization allows to expand hadrons on a Fock basis:

$$|P,\pi
angle \propto \sum_{eta} \Psi_{eta}^{qar{q}} |qar{q}
angle + \sum_{eta} \Psi_{eta}^{qar{q},qar{q}} |qar{q},qar{q}
angle + \dots$$

 $|P,N
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- Non-perturbative physics is contained in the N-particles Lightfront-Wave Functions (LFWF) Ψ^N
- Schematically a distribution amplitude φ is related to the LFWF through:

$$arphi(x) \propto \int rac{\mathrm{d}^2 k_\perp}{(2\pi)^2} \Psi(x,k_\perp)$$

S. Brodsky and G. Lepage, PRD 22, (1980)

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• 3 bodies matrix element:

 $\langle 0|\epsilon^{ijk}u^i_{lpha}(z_1)u^j_{eta}(z_2)d^k_{\gamma}(z_3)|P
angle$

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• 3 bodies matrix element expanded at leading twist:

$$\langle 0|\epsilon^{ijk} u^{i}_{\alpha}(z_{1}) u^{j}_{\beta}(z_{2}) d^{k}_{\gamma}(z_{3})|P\rangle = \frac{1}{4} \left[\left(\not p C \right)_{\alpha\beta} \left(\gamma_{5} N^{+} \right)_{\gamma} V(z_{i}^{-}) \right. \\ \left. + \left(\not p \gamma_{5} C \right)_{\alpha\beta} \left(N^{+} \right)_{\gamma} A(z_{i}^{-}) - \left(i p^{\mu} \sigma_{\mu\nu} C \right)_{\alpha\beta} \left(\gamma^{\nu} \gamma_{5} N^{+} \right)_{\gamma} T(z_{i}^{-}) \right]$$

V. Chernyak and I. Zhitnitsky, Nucl. Phys. B 246, (1984)

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- Usually, one defines $\varphi = V A$
- 3 bodies Fock space interpretation (leading twist):

$$\begin{aligned} |P,\uparrow\rangle &= \int \frac{[\mathrm{d}x]}{8\sqrt{6x_1x_2x_3}} |uud\rangle \otimes [\varphi(x_1,x_2,x_3)|\uparrow\downarrow\uparrow\rangle \\ &+\varphi(x_2,x_1,x_3)|\downarrow\uparrow\uparrow\rangle - 2T(x_1,x_2,x_3)|\uparrow\uparrow\downarrow\rangle] \end{aligned}$$



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Isospin symmetry:

$$2T(x_1, x_2, x_3) = \varphi(x_1, x_3, x_2) + \varphi(x_2, x_3, x_1)$$

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Evolution and Asymptotic results



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Baryon DAs

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- QCD Sum Rules
 - V. Chernyak and I. Zhitnitsky, Nucl. Phys. B 246 (1984)
- Relativistic quark model
 - Z. Dziembowski, PRD 37 (1988)
- Scalar diquark clustering
 - Z. Dziembowski and J. Franklin, PRD 42 (1990)
- Phenomenological fit
 - J. Bolz and P. Kroll, Z. Phys. A 356 (1996)
- Lightcone quark model
 - B. Pasquini et al., PRD 80 (2009)
- Lightcone sum rules
 - I. Anikin et al., PRD 88 (2013)
- Lattice Mellin moment computation
 - G. Bali et al., JHEP 2016 02



- Algebraic parametrisation inspired by the results obtained from DSEs and Faddeev equations.
- It is based on Nakanishi representation, which is completely general.
- This is an exploratory work: we want to know what we can or cannot do.
- We also assume the dynamical diquark correlations, both scalar and AV, and compare in the end with Lattice QCD one.

Nakanishi Representation



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At all order of perturbation theory, one can write (Euclidean space):

$$\Gamma(k,P) = \mathcal{N} \int_0^\infty \mathrm{d}\gamma \int_{-1}^1 \mathrm{d}z \frac{\rho_n(\gamma,z)}{(\gamma + (k + \frac{z}{2}P)^2)^n}$$

We use a "simpler" version of the latter as follow:

$$\widetilde{\Gamma}(q,P) = \mathcal{N} \int_{-1}^{1} \mathrm{d}z \frac{\rho_n(z)}{(\Lambda^2 + (q - \frac{1-z}{2}P)^2)^n}$$

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• Operator point of view for every DA (and at every twist):

$$\langle 0|\epsilon^{ijk}\left(u^{i}_{\uparrow}(z_{1})C \not n u^{j}_{\downarrow}(z_{2})\right) \not n d^{k}_{\uparrow}(z_{3})|P,\lambda\rangle \rightarrow \varphi(x_{1},x_{2},x_{3}),$$

Braun et al., Nucl.Phys. B589 (2000)

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• Operator point of view for every DA (and at every twist):

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• We can apply it on the wave function:





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• The operator then selects the relevant component of the wave function.



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• We can apply it on the wave function:



- The operator then selects the relevant component of the wave function.
- Our ingredients are:
 - Perturbative-like quark and diquark propagator
 - Nakanishi based diquark Bethe-Salpeter-like amplitude (green disks)
 - Nakanishi based quark-diquark amplitude (dark blue ellipses)

Diquark DA



$$\phi(x) \propto 1 - rac{M^2}{K^2} rac{\ln\left[1 + rac{K^2}{M^2} x(1-x)
ight]}{x(1-x)}$$



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Diquark DA





Pion figure from L. Chang et al., PRL 110 (2013)

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Diquark DA





Pion figure from L. Chang et al., PRL 110 (2013)

This results provide a broad and concave meson DA parametrisationThe endpoint behaviour remains linear

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Results at 2GeV





- Results evolved from 0.51 to 2 GeV with both scalar and AV diquark
- Nucleon DA is skewed compared to the asymptotic one
- It is also broader than the asymptotic results
- These properties are consequences of our quark-diquark picture

Comparison with lattice





Lattice data from V.Braun et al, PRD 89 (2014)

Chapter 3: Diquarks and the Roper resonance

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The Roper as a quark-diquark bound state



• ... but modifying slightly the Quark-Diquark amplitude



Figures from J.Segovia et al., PRL 115 171801 (2015)

The Roper as a quark-diquark bound state



- The Roper can be described almost exactly in the same way than the nucleon...
- ... but modifying slightly the Quark-Diquark amplitude
- The quark-diquark picture has been succefully applied to the transition FF





Figures from J.Segovia et al., PRL 115 171801 (2015)

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Results at 2GeV





- Results evolved from 0.51 to 2 GeV with both scalar and AV diquark
- Contrary to the nucleon PDA, the Roper PDA is not positive definite
- The picture is consistent with our idea of QM radially excited states
- There is a curve of zero, *i.e.* of "forbidden momenta".

Chapter 4: Form Factors

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Form Factors





$$\begin{split} F_1(Q^2) &= \mathcal{N} \int [\mathrm{d}x_i] [\mathrm{d}y_i] \left[\varphi(x_i, \zeta_x^2) H_{\varphi}(x_i, y_i, Q^2, \zeta_x^2, \zeta_y^2) \varphi(y_i, \zeta_y^2) \right. \\ &+ \mathcal{T}(x_i, \zeta_x^2) H_{\mathcal{T}}(x_i, y_i, Q^2, \zeta_x^2, \zeta_y^2) \mathcal{T}(y_i, \zeta_y^2) \Big] \end{split}$$

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Form Factors





$$F_1(Q^2) = \mathcal{N} \int [\mathrm{d}x_i] [\mathrm{d}y_i] \left[\varphi(x_i, \zeta_x^2) H_{\varphi}(x_i, y_i, Q^2, \zeta_x^2, \zeta_y^2) \varphi(y_i, \zeta_y^2) \right. \\ \left. + T(x_i, \zeta_x^2) H_T(x_i, y_i, Q^2, \zeta_x^2, \zeta_y^2) T(y_i, \zeta_y^2) \right]$$

- LO Kernel well known since more than 30 years...
- ...but different groups have argued different choices for the treatment of scales:
 - for the DA : $\varphi(Q^2), \varphi((\min(x_i) \times Q)^2)...,$
 - ► for the strong coupling constant : $\alpha_{s}(Q^{2}), \alpha_{s}(< x_{i} >^{2} Q^{2}), \alpha_{s}^{reg}(g(x_{i}, y_{j})Q^{2})$
- Use of perturbative coupling vs. effective coupling?



• In the pion case, the hard kernel is known at NLO allowing us to discuss more extensively the scale effects.

R Field *et al.*, NPB 186 429 (1981) F. Dittes and A. Radyushkin, YF 34 529 (1981) B. Melic *et al.*, PRD 60 074004 (1999)

• The UV scale dependent term behaves like:

$$f_{UV}(\mu) \propto eta_0 \left(5/3 - \ln((1-x)(1-y)) + \ln\left(rac{\mu^2}{Q^2}
ight)
ight)$$

- Here I take two examples:
 - the standard choice of $\zeta_x^2 = \zeta_y^2 = \mu^2 = Q^2/4$
 - ▶ the regularised BLM-PMC scale $\zeta_x^2 = \zeta_y^2 = \mu^2 = e^{-5/3}Q^2/4$

S. Brodsky et al., PRD 28 228 (1983) S. Brodsky and L. Di Giustino, PRD 86 085026 (2011)

• What is the effect on our meson like DA?

$$\varphi_{\pi}(x,\zeta^2 = 4 \, \text{GeV}^2) = \mathcal{N}\left(1 - \frac{\ln\left[1 + \alpha x(1-x)\right]}{\alpha x(1-x)}\right)$$

 α is tuned on LQCD Mellin Moments

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 BLM scale reduces significantly the impact of the NLO corrections and increase dramatically the LO one.





- Unfortunately, only the LO treatment has been performed \Rightarrow BLM scale is therefore unknown
- We use the Chernyak-Zhitnitsky formalism to compute the nucleon for factor with:
 - the CZ scale setting $\rightarrow \alpha_s(Q^2/9)\alpha_s(4Q^2/9)$
 - the pion BLM factor $\rightarrow \alpha_s(Q^2/9 e^{-5/3})\alpha_s(4Q^2/9 e^{-5/3})$

and using both perturbative and effective couplings.

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CZ scale setting with frozen PDA at $1 {\rm GeV}^2$



Data from Arnold et al. PRL 57

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CZ scale setting + evolution



Data from Arnold et al. PRL 57

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Pion BLM Factor + evolution



Data from Arnold et al. PRL 57

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and using both perturbative and effective couplings.

- The data remain flat while the perturbative running show a logarithmic decreasing.
- More work are required to conclude on the validity of the perturbative approach:
 - Theory side : we need NLO corrections
 - Experimental side : more precise data to spot a logarithmic decreasing

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Conclusion

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Baryon PDA

- DSE compatible framework for Baryon PDAs.
- Simple Nakanishi representation works well for the nucleon PDA.
- First calculation of the Roper PDA has been performed
- Extend the results to more realistic models (running quark masses...).

Form Factors

- Calculation of Leading Order Form Factors is done
- There is a systematic discrepency with available data.
 - NLO Corrections?
 - Scale Setting?
- More work is required

Thank you for your attention

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Back up slides

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B. Berthou et al., accepted in EPJC

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Experimental data and phenomenology

Full processes

Computation of amplitudes

Small distance contributions

First principles and fundamental parameters

Large distance contributions

Cédric Mezrag (INFN)

Baryon DAs

July 2nd, 2018 30 / 27

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Baryon DAs

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http://partons.cea.fr

PARtonic Tomography Of Nucleon Software

PARTONS

Main Page Reference documentation +

Main Page

What is PARTONS?

PARTONS is a C++ software framework dedicated to the phenomenology of Generalized Parton Distributions (GPDs), GPDs provide a comprehensive description of the partonic structure of the nucleon and contain a wealth of new information. In particular, GPDs provide a description of the nucleon as an extended object, referred to as 3-dimensional nucleon tomography, and give an access to the orbital angular momentum of guarks.

PARTONS provides a necessary bridge between models of GPDs and experimental data measured in various exclusive channels, like Deeply Virtual Compton Scattering (DVCS) and Hard Exclusive Meson Production (HEMP). The experimental programme devoted to study GPDs has been carrying out by several experiments, like HERMES at DESY (closed), COMPASS at CERN, Hall-A and CLAS at JLab. GPD subject will be also a key component of the physics case for the expected Electron Ion Collider (EIC).

PARTONS is useful to theorists to develop new models, phenomenologists to interpret existing measurements and to experimentalists to design new experiments. A detailed description of the project can be found here.

Get PARTONS

Here you can learn how to get your own version of PARTONS. We offer two ways.

You can use our provided virtual machine with an out-of-the-box PARTONS runtime and development environment. This is the easiest way to start your experience with PARTONS.

Using PARTONS with our provided Virtual Machine

You can also build PARTONS by your own on either GNU/Linux or Mac OS X. This is useful if you want to have PARTONS on your computer without using the virtualization technology or if you want to use PARTONS on computing farms

Using PARTONS on GNU/Linux

Using PARTONS on Mac OS X

Configure PARTONS

If you are using our virtual machine, you will find all configuration files set up and ready to be used. However, if you want to tune the configuration or if you have installed PARTONS by your own, this tutorial will be helpful for



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