Structure of the nucleon and its resonances

Cédric Mezrag

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July 2^{nd} , 2018

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Chapter 1: Dyson-Schwinger equations

July 2^{nd} , 2018 2 / 27

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- Dyson-Schwinger equations relate Green (Schwinger) functions among each other.
- \bullet One get in the case of QCD, an infinite system \rightarrow truncations are required.
- DSEs are usually solved in Euclidean space, yielding Schwinger functions instead of Green functions.

(Although some works are performed to solve them directly in Minkowski space)

- Dyson-Schwinger equations relate Green (Schwinger) functions among each other.
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Truncating the DSEs yields an non-perturbative approximation of QCD Schwinger functions.

The Gap Equation

• The gap equation for the quark propagator $S(q)$:

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The Gap Equation

• The gap equation for the quark propagator $S(q)$:

• It has successfully described the quark mass behaviour:

- ► $S(q)^{-1} = i \frac{q}{q} A(q^2) + B(q^2)$
- \triangleright Non-perturbative description of the quark mass
- \blacktriangleright Dynamical mass generation
- Figure from Bashir et al. (2012)

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The Faddeev equation provides a covariant framework to describe the nucleon as a bound state of three dressed quarks.

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- Mostly two types of diquark are dynamically generated by the Faddeev equation:
	- Scalar diquarks, whose mass is roughly $2/3$ of the nucleon mass,
	- Axial-Vector (AV) diquarks, whose mass is around $3/4$ of the nucleon one.

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	- Scalar diquarks, whose mass is roughly $2/3$ of the nucleon mass,
	- Axial-Vector (AV) diquarks, whose mass is around $3/4$ of the nucleon one.
- Can we understand the nucleon structure in terms of quark-diquarks correlations? $E|E|$ \bigcirc Q \bigcirc

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Chapter 2: Baryon Distribution Amplitudes

CM, J. Segovia, L. Chang, C.D. Roberts, arXiv:1711.09101

July 2^{nd} , 2018 6 / 27

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Hadrons seen as Fock States

Lightfront quantization allows to expand hadrons on a Fock basis:

$$
|P,\pi\rangle \propto \sum_{\beta} \Psi_{\beta}^{q\bar{q}} |q\bar{q}\rangle + \sum_{\beta} \Psi_{\beta}^{q\bar{q},q\bar{q}} |q\bar{q},q\bar{q}\rangle + \dots
$$

$$
|P,N\rangle \propto \sum_{\beta} \Psi_{\beta}^{qqq} |qqq\rangle + \sum_{\beta} \Psi_{\beta}^{qqq,q\bar{q}} |qqq,q\bar{q}\rangle + \dots
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 $E|E| \leq 0.90$

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- Non-perturbative physics is contained in the N-particles Lightfront-Wave Functions (LFWF) Ψ^N
- Schematically a distribution amplitude φ is related to the LFWF through:

$$
\varphi(x) \propto \int \frac{\mathrm{d}^2 k_{\perp}}{(2\pi)^2} \Psi(x, k_{\perp})
$$

S. Brodsky and G. Lepage, PRD 22, (1980)

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• 3 bodies matrix element:

 $\langle 0 | \epsilon^{ijk} u^i_\alpha(z_1) u^j_\beta$ $\frac{d}{d\beta}(z_2)d^{k}_{\gamma}(z_3)|P\rangle$

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• 3 bodies matrix element expanded at leading twist:

$$
\langle 0|\epsilon^{ijk}u_{\alpha}^{i}(z_{1})u_{\beta}^{j}(z_{2})d_{\gamma}^{k}(z_{3})|P\rangle = \frac{1}{4}\left[\left(\rlap{/}{\varphi C}\right)_{\alpha\beta}\left(\gamma_{5}N^{+}\right)_{\gamma}V(z_{i}^{-})\right] + \left(\rlap{/}{\varphi}\gamma_{5}C\right)_{\alpha\beta}\left(N^{+}\right)_{\gamma}A(z_{i}^{-}) - \left(i\rho^{\mu}\sigma_{\mu\nu}C\right)_{\alpha\beta}\left(\gamma^{\nu}\gamma_{5}N^{+}\right)_{\gamma}T(z_{i}^{-})\right]
$$

V. Chernyak and I. Zhitnitsky, Nucl. Phys. B 246, (1984)

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- Usually, one defines $\varphi = V A$
- 3 bodies Fock space interpretation (leading twist):

$$
|P,\uparrow\rangle = \int \frac{[\mathrm{d}x]}{8\sqrt{6x_1x_2x_3}}|uud\rangle \otimes [\varphi(x_1,x_2,x_3)] \uparrow \downarrow \uparrow\rangle
$$

$$
+ \varphi(x_2,x_1,x_3)| \downarrow \uparrow \uparrow\rangle - 2\mathcal{T}(x_1,x_2,x_3)| \uparrow \uparrow \downarrow\rangle]
$$

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$$

• Isospin symmetry:

$$
2\, \mathcal{T}(x_1,x_2,x_3)=\varphi(x_1,x_3,x_2)+\varphi(x_2,x_3,x_1)
$$

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Evolution and Asymptotic results

• Both φ and τ are scale dependent objects: they obey evolution equations

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Evolution and Asymptotic results

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July 2^{nd} , 2018 10 / 27

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- QCD Sum Rules
	- ▶ V. Chernyak and I. Zhitnitsky, Nucl. Phys. B 246 (1984)
- Relativistic quark model
	- ▶ Z. Dziembowski, PRD 37 (1988)
- Scalar diquark clustering
	- ▶ Z. Dziembowski and J. Franklin, PRD 42 (1990)
- Phenomenological fit
	- \blacktriangleright J. Bolz and P. Kroll, Z. Phys. A 356 (1996)
- **•** Lightcone quark model
	- \triangleright B. Pasquini et al., PRD 80 (2009)
- Lightcone sum rules
	- \blacktriangleright I. Anikin et al., PRD 88 (2013)
- Lattice Mellin moment computation
	- \triangleright G. Bali et al., JHEP 2016 02

- Algebraic parametrisation inspired by the results obtained from DSEs and Faddeev equations.
- It is based on Nakanishi representation, which is completely general.
- This is an exploratory work: we want to know what we can or cannot do.
- We also assume the dynamical diquark correlations, both scalar and AV, and compare in the end with Lattice QCD one.

Nakanishi Representation

At all order of perturbation theory, one can write (Euclidean space):

$$
\Gamma(k, P) = \mathcal{N} \int_0^\infty d\gamma \int_{-1}^1 dz \frac{\rho_n(\gamma, z)}{(\gamma + (k + \frac{z}{2}P)^2)^n}
$$

We use a "simpler" version of the latter as follow:

$$
\tilde{\Gamma}(q,P) = \mathcal{N} \int_{-1}^{1} \mathrm{d}z \frac{\rho_n(z)}{(\Lambda^2 + (q - \frac{1-z}{2}P)^2)^n}
$$

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July 2^{nd} , 2018 13 / 27

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Operator point of view for every DA (and at every twist):

$$
\langle 0|\epsilon^{ijk}\left(u_1^i(z_1)\mathcal{C}\rlap{/} \hskip-2.5pt\mu u_\downarrow^i(z_2)\right)\rlap{/} \hskip-2.5pt\mu d_1^k(z_3)|P,\lambda\rangle\to \varphi(x_1,x_2,x_3),
$$

Braun et al., Nucl.Phys. B589 (2000)

July 2^{nd} , 2018 14 / 27

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Operator point of view for every DA (and at every twist):

$$
\langle 0 | \epsilon^{ijk} \left(u^i_\uparrow(z_1) C \hbar u^j_\downarrow(z_2) \right) \hbar d^k_\uparrow(z_3) | P, \lambda \rangle \rightarrow \varphi(x_1, x_2, x_3),
$$

Brain et al., Nucl. Phys. B589 (2000)

• We can apply it on the wave function:

Operator point of view for every DA (and at every twist):

$$
\langle 0|\epsilon^{ijk}\left(u_\uparrow^i(z_1)\,C\hskip.03cm\hskip-1.5cm\mu u_\downarrow^j(z_2)\right)\hskip.03cm\hskip-1.5cm\hskip-1.6cm\mu d_\uparrow^k(z_3)|P,\lambda\rangle\to\varphi(x_1,x_2,x_3),
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The operator then selects the relevant component of the wave function.

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$$

Braun et al., Nucl.Phys. B589 (2000)

• We can apply it on the wave function:

- The operator then selects the relevant component of the wave function.
- Our ingredients are:
	- \triangleright Perturbative-like quark and diquark propagator
	- \triangleright Nakanishi based diquark Bethe-Salpeter-like amplitude (green disks)
	- \triangleright Nakanishi based quark-diquark amplitude (dark blue ellipses)

Diquark DA

July 2^{nd} , 2018 15 / 27

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$$
\phi(x)\propto 1-\frac{M^2}{K^2}\frac{\ln\left[1+\frac{K^2}{M^2}x(1-x)\right]}{x(1-x)}
$$

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Pion figure from L. Chang et al., PRL 110 (2013)

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July 2^{nd} , 2018 15 / 27

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Diquark DA

Pion figure from L. Chang et al., PRL 110 (2013)

This results provide a broad and concave meson DA parametrisation • The endpoint behaviour remains linear M I → Ele Mar (□) (f)

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Results at 2GeV

- Results evolved from 0.51 to 2 GeV with both scalar and AV diquark
- Nucleon DA is skewed compared to the asymptotic one
- It is also broader than the asymptotic results
- These properties are consequences of our quark-diquark picture

Comparison with lattice

Lattice data from V.Braun et al, PRD 89 (2014)

Chapter 3: Diquarks and the Roper resonance

July 2^{nd} , 2018 18 / 27

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The Roper as a quark-diquark bound state

... but modifying slightly the Quark-Diquark amplitude

Figures from J.Segovia et al., PRL 115 171801 (2015)

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The Roper as a quark-diquark bound state

- The Roper can be described almost exactly in the same way than the nucleon...
- ... but modifying slightly the Quark-Diquark amplitude
- The quark-diquark picture has been succefully applied to the transition FF

Figures from J.Segovia et al., PRL 115 171801 (2015)

Results at 2GeV

- Results evolved from 0.51 to 2 GeV with both scalar and AV diquark
- Contrary to the nucleon PDA, the Roper PDA is not positive definite
- The picture is consistent with our idea of QM radially excited states
- There is a curve of zero, *i.e.* of "forbidden momenta".

Chapter 4: Form Factors

July 2^{nd} , 2018 21 / 27

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Form Factors

July 2^{nd} , 2018 22 / 27

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$$
F_1(Q^2) = \mathcal{N} \int [\mathrm{d}x_i] [\mathrm{d}y_i] \left[\varphi(x_i, \zeta_x^2) H_{\varphi}(x_i, y_i, Q^2, \zeta_x^2, \zeta_y^2) \varphi(y_i, \zeta_y^2) + T(x_i, \zeta_x^2) H_T(x_i, y_i, Q^2, \zeta_x^2, \zeta_y^2) T(y_i, \zeta_y^2) \right]
$$

Form Factors

$$
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$$

- LO Kernel well known since more than 30 years...
- ...but different groups have argued different choices for the treatment of scales:
	- For the DA : $\varphi(Q^2), \varphi((min(x_i) \times Q)^2)$...,
	- \triangleright for the strong coupling constant : $\alpha_{\sf S}(Q^2), \alpha_{\sf s}(<\sf x_i>^2\sf Q^2), \alpha_{\sf s}^{\rm reg}(g(\sf x_i,y_j)Q^2)$
- Use of perturbative coupling vs. effective coupling?

Digression: Pion FF

• In the pion case, the hard kernel is known at NLO allowing us to discuss more extensively the scale effects.

R Field et al., NPB 186 429 (1981)

F. Dittes and A. Radyushkin, YF 34 529 (1981)

B. Melic et al., PRD 60 074004 (1999)

• The UV scale dependent term behaves like:

$$
f_{UV}(\mu) \propto \beta_0 \left(5/3 - \ln((1-x)(1-y)) + \ln\left(\frac{\mu^2}{Q^2}\right)\right)
$$

- Here I take two examples:
	- ighthropole the standard choice of $\zeta_{\rm x}^2 = \zeta_{\rm y}^2 = \mu^2 = Q^2/4$
	- ► the regularised BLM-PMC scale $\zeta_{\sf x}^2=\zeta_{\sf y}^2=\mu^2={\sf e}^{-5/3} {\sf Q}^2/4$

S. Brodsky et al., PRD 28 228 (1983) S. Brodsky and L. Di Giustino, PRD 86 085026 (2011)

• What is the effect on our meson like DA?

$$
\varphi_{\pi}(x,\zeta^2=4\text{GeV}^2)=\mathcal{N}\left(1-\frac{\ln\left[1+\alpha x(1-x)\right]}{\alpha x(1-x)}\right)
$$

 α is tuned on LQCD Mellin Moments

July 2^{nd} , 2018 23 / 27

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Digression: Pion FF

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July 2^{nd} , 2018 23 / 27

S. Brodsky and L. Di Giustino, PRD 86 085026 (2011)

BLM scale reduces significantly the impact of the NLO corrections and increase dramatically the LO one.

- Unfortunately, only the LO treatment has been performed \Rightarrow BLM scale is therefore unknown
- We use the Chernyak-Zhitnitsky formalism to compute the nucleon for factor with:
	- \triangleright the CZ scale setting $\rightarrow \alpha_s (Q^2/9) \alpha_s (4Q^2/9)$
	- ► the pion BLM factor $\to \alpha_s (Q^2/9 \, e^{-5/3}) \alpha_s (4Q^2/9 \, e^{-5/3})$

and using both perturbative and effective couplings.

Proton case

CZ scale setting with frozen PDA at 1GeV^2

Data from Arnold et al. PRL 57

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 $E|E \cap Q$

Proton case

 CZ scale setting $+$ evolution

Data from Arnold et al. PRL 57

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 $E|E| \leq 0.90$

Proton case

Pion BLM Factor + evolution

Data from Arnold et al. PRL 57

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July 2^{nd} , 2018 24 / 27

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	- ► the pion BLM factor $\to \alpha_s (Q^2/9 \, e^{-5/3}) \alpha_s (4Q^2/9 \, e^{-5/3})$

and using both perturbative and effective couplings.

- The data remain flat while the perturbative running show a logarithmic decreasing.
- More work are required to conclude on the validity of the perturbative approach:
	- \blacktriangleright Theory side : we need NLO corrections
	- \triangleright Experimental side : more precise data to spot a logarithmic decreasing

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Conclusion

July 2^{nd} , 2018 25 / 27

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Baryon PDA

- DSE compatible framework for Baryon PDAs.
- Simple Nakanishi representation works well for the nucleon PDA.
- **First calculation of the Roper PDA has been performed**
- Extend the results to more realistic models (running quark masses...).

Form Factors

- Calculation of Leading Order Form Factors is done
- There is a systematic discrepency with available data.
	- NI O Corrections?
	- Scale Setting?
- More work is required

Thank you for your attention

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Back up slides

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B. Berthou et al., accepted in EPJC

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Computation of amplitudes Small distance contributions

First principles and fundamental parameters

Large distance contributions

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http://partons.cea.fr

PARtonic Tomography Of Nucleon Software

PARTONS

Main Page Reference documentation +

Main Page

What is PARTONS?

PARTONS is a C++ software framework dedicated to the phenomenology of Generalized Parton Distributions (GPDs), GPDs provide a comprehensive description of the partonic structure of the nucleon and contain a wealth of new information. In particular, GPDs provide a description of the nucleon as an extended object, referred to as 3-dimensional nucleon tomography, and give an access to the orbital angular momentum of quarks.

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PARTONS provides a necessary bridge between models of GPDs and experimental data measured in various exclusive channels, like Deeply Virtual Compton Scattering (DVCS) and Hard Exclusive Meson Production (HEMP). The experimental programme devoted to study GPDs has been carrying out by several experiments, like HERMES at DESY (closed), COMPASS at CERN, Hall-A and CLAS at JLab. GPD subject will be also a key component of the physics case for the expected Electron Ion Collider (EIC).

Table of Contents

L. What is PARTONS? **J Get RARTONS J** Confloure PARTONS .
« How to use PARTONS a Publications and talks

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J License Contact and nearborne

July 2^{nd} , 2018 31 / 27

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PARTONS is useful to theorists to develop new models, phenomenologists to interpret existing measurements and to experimentalists to design new experiments. A detailed description of the project can be found here.

Get PARTONS

Here you can learn how to get your own version of PARTONS. We offer two ways.

You can use our provided virtual machine with an out-of-the-box PARTONS runtime and development environment. This is the easiest way to start your experience with PARTONS.

Using PARTONS with our provided Virtual Machine

You can also build PARTONS by your own on either GNU/Linux or Mac OS X. This is useful if you want to have PARTONS on your computer without using the virtualization technology or if you want to use PARTONS on computing farms

Using PARTONS on GNU/Linux

Using PARTONS on Mac OS X

Configure PARTONS

If you are using our virtual machine, you will find all configuration files set up and ready to be used. However, if you want to tune the configuration or if you have installed PARTONS by your own, this tutorial will be he