

Extraction of nucleon 3D structure from DVCS data

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The Nature of Hadron Mass and Quark-Gluon Confinement
from JLab Experiments in the 12-GeV Era

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Outline

- ➊ Introduction to Generalized Parton Distributions (GPDs) and Deeply Virtual Compton Scattering (DVCS)
- ➋ Global model fits
- ➌ D-term
- ➍ Higher twists
- ➎ Outlook

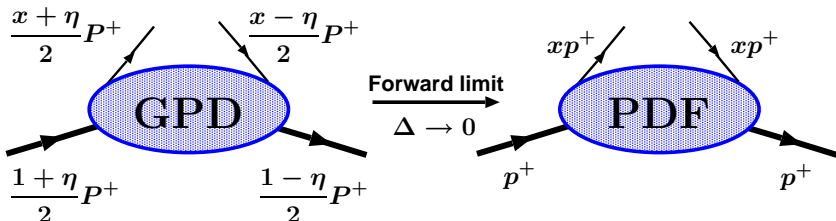
Definition of GPDs

- In QCD **GPDs** are defined as [Müller '92, et al. '94, Ji, Radyushkin '96]

$$F^q(x, \eta, t) = \int \frac{dz^-}{2\pi} e^{ixP^+z^-} \langle P_2 | \bar{q}(-z) \gamma^+ q(z) | P_1 \rangle \Big|_{z^+=0, z_\perp=0}$$

$$\tilde{F}^q(x, \eta, t) = \int \frac{dz^-}{2\pi} e^{ixP^+z^-} \langle P_2 | \bar{q}(-z) \gamma^+ \gamma_5 q(z) | P_1 \rangle \Big|_{z^+=0, z_\perp=0}$$

(and similarly for gluons F^g and \tilde{F}^g).



$$P = P_1 + P_2; \quad t = \Delta^2 = (P_2 - P_1)^2; \quad \eta = -\frac{\Delta^+}{P^+} \text{ (skewedness)}$$

Some properties of GPDs

- Decomposing into spin-non-flip and spin-flip part:

$$F^a = \frac{\bar{u}(P_2)\gamma^+u(P_1)}{P^+} H^a + \frac{\bar{u}(P_2)i\sigma^{+\nu}u(P_1)\Delta_\nu}{2MP^+} E^a \quad a = q, g$$

$$\tilde{F}^a = \frac{\bar{u}(P_2)\gamma^+\gamma_5u(P_1)}{P^+} \tilde{H}^a + \frac{\bar{u}(P_2)\gamma_5u(P_1)\Delta^+}{2MP^+} \tilde{E}^a \quad a = q, g$$

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- Ji's "sum rule" (related to proton spin problem)

$$J^q = \frac{1}{2} \int_{-1}^1 dx x \left[H^q(x, \eta, t) + E^q(x, \eta, t) \right]_{t \rightarrow 0} \quad [\text{Ji '96}]$$

(where E is poorly constrained by present data)

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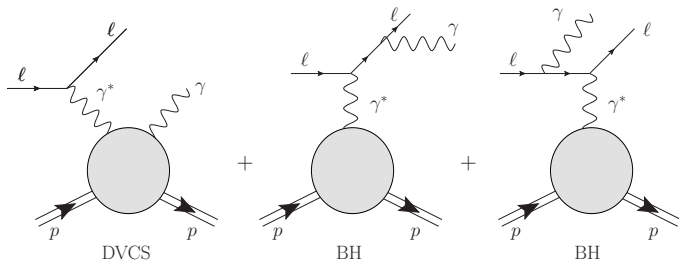
- Distribution of partons in **transversal** space

$$\rho(x, \vec{b}_\perp) = \int \frac{d^2 \vec{\Delta}_\perp}{(2\pi)^2} e^{-i\vec{b}_\perp \cdot \vec{\Delta}_\perp} H(x, 0, -\vec{\Delta}_\perp^2) \quad [\text{Burkardt '00}]$$

(where experiments are mostly sensitive to $H(x, x, t)$)

Access to GPDs via DVCS

- **Deeply virtual Compton scattering (DVCS)** — “gold plated” process of exclusive physics
- DVCS is measured via lepton production of a photon



- **Interference** with Bethe-Heitler process gives unique access to both real and imaginary part of DVCS amplitude.

DVCS cross section

$$d\sigma \propto |\mathcal{T}|^2 = |\mathcal{T}_{\text{BH}}|^2 + |\mathcal{T}_{\text{DVCS}}|^2 + \mathcal{I}.$$

$$\mathcal{I} \propto \frac{-e_\ell}{\mathcal{P}_1(\phi)\mathcal{P}_2(\phi)} \left\{ c_0^{\mathcal{I}} + \sum_{n=1}^3 [c_n^{\mathcal{I}} \cos(n\phi) + s_n^{\mathcal{I}} \sin(n\phi)] \right\},$$

$$|\mathcal{T}_{\text{DVCS}}|^2 \propto \left\{ c_0^{\text{DVCS}} + \sum_{n=1}^2 [c_n^{\text{DVCS}} \cos(n\phi) + s_n^{\text{DVCS}} \sin(n\phi)] \right\},$$

- Choosing polarizations (and charges) we focus on particular harmonics:

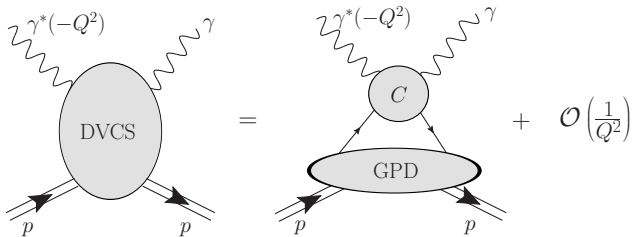
$$c_{1,\text{unpol.}}^{\mathcal{I}} \propto \left[F_1 \Re \mathcal{H} - \frac{t}{4M_p^2} F_2 \Re \mathcal{E} + \frac{x_B}{2 - x_B} (F_1 + F_2) \Re \tilde{\mathcal{H}} \right]$$

[Belitsky, Müller et. al '01-'14]

- $\mathcal{H}(x_B, t, Q^2), \dots$ — four **Compton form factors** (CFFs)

Factorization of DVCS \longrightarrow GPDs

- [Collins et al. '98]



- Compton form factor is a convolution:

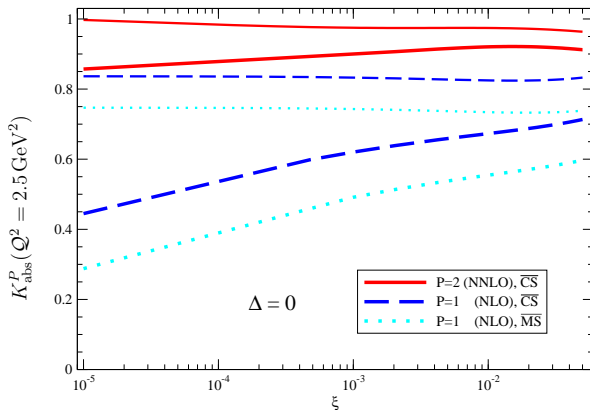
$${}^a\mathcal{H}(x_B, t, Q^2) = \int dx C^a(x, \frac{x_B}{2-x_B}, \frac{Q^2}{Q_0^2}) H^a(x, \frac{x_B}{2-x_B}, t, Q_0^2)$$

$a=q, G$

- $H^a(x, \eta, t, Q_0^2)$ — **Generalized parton distribution (GPD)**

(N)NLO corrections

- [K.K., Müller and Passek-K. '07]



Thick lines:
 “hard” gluon
 $N_G = 0.4$
 $\alpha_G(0) = \alpha_\Sigma(0) + 0.05$

Thin lines:
 “soft” gluon
 $N_G = 0.3$
 $\alpha_G(0) = \alpha_\Sigma(0) - 0.02$

$$K_{\text{abs}}^P \equiv \left| \frac{\mathcal{H}^{(P)}}{\mathcal{H}^{(P-1)}} \right|$$

Status of fits

Hybrid GPD models for global fits

- **Sea quarks and gluons** modelled using $SO(3)$ partial wave expansion in conformal GPD moment space + Q^2 evolution.
- **Valence quarks** — model CFFs directly (ignoring Q^2 evolution):

$$\Im \mathcal{H}(\xi, t) = \pi \left[\frac{4}{9} H^{u_{\text{val}}}(\xi, \xi, t) + \frac{1}{9} H^{d_{\text{val}}}(\xi, \xi, t) + \frac{2}{9} H^{\text{sea}}(\xi, \xi, t) \right]$$

$$H(x, x, t) = n r 2^\alpha \left(\frac{2x}{1+x} \right)^{-\alpha(t)} \left(\frac{1-x}{1+x} \right)^b \frac{1}{\left(1 - \frac{1-x}{1+x} \frac{t}{M^2} \right)^p}.$$

- $\Re \mathcal{H}$ determined by dispersion relations
- 15 free parameters in total for $H, \tilde{H}, E, \tilde{E}$.

Experimental coverage (fixed target part)

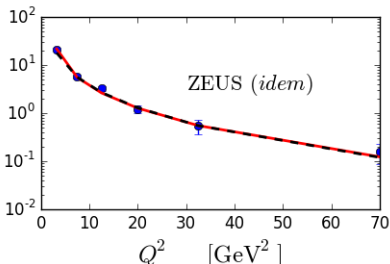
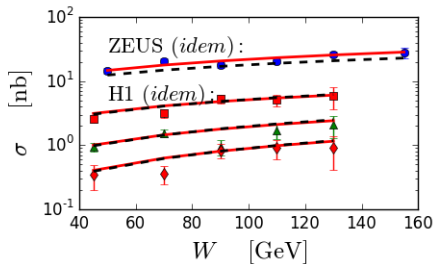
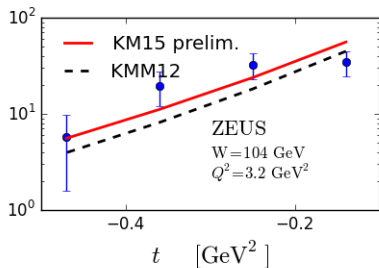
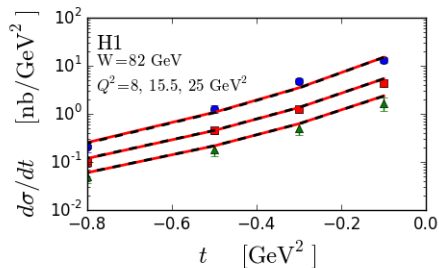
Collab.	Year	Observables	Kinematics			No. of points	
			x_B	Q^2 [GeV ²]	$ t $ [GeV ²]	total	indep.
HERMES	2001	$A_{LU}^{\sin\phi}$	0.11	2.6	0.27	1	1
CLAS	2001	$A_{LU}^{\sin\phi}$	0.19	1.25	0.19	1	1
CLAS	2006	$A_{UL}^{\sin\phi}$	0.2–0.4	1.82	0.15–0.44	6	3
HERMES	2006	$A_C^{\cos\phi}$	0.08–0.12	2.0–3.7	0.03–0.42	4	4
Hall A	2006	$\sigma(\phi), \Delta\sigma(\phi)$	0.36	1.5–2.3	0.17–0.33	$4 \times 24 + 12 \times 24$	$4 \times 24 + 12 \times 24$
CLAS	2007	$A_{LU}(\phi)$	0.11–0.58	1.0–4.8	0.09–1.8	62×12	62×12
HERMES	2008	$A_C^{\cos(0,1)\phi}, A_{UT,DVCS}^{\sin(\phi-\phi_S)}$	0.03–0.35	1–10	<0.7	12+12+12	4+4+4
		$A_{UT,I}^{\sin(\phi-\phi_S)\cos(0,1)\phi}$				12+12	4+4
		$A_{UT,I}^{\cos(\phi-\phi_S)\sin\phi}$				12	4
CLAS	2008	$A_{LU}(\phi)$	0.12–0.48	1.0–2.8	0.1–0.8	66	33
HERMES	2009	$A_{LU,I}^{\sin(1,2)\phi}, A_{LU,DVCS}^{\sin\phi}, A_C^{\cos(0,1,2,3)\phi}$	0.05–0.24	1.2–5.75	<0.7	18+18+18 18+18+18+18	6+6+6 6+6+6+6
HERMES	2010	$A_{UL}^{\sin(1,2,3)\phi}$	0.03–0.35	1–10	<0.7	12+12+12	4+4+4
		$A_{LL}^{\cos(0,1,2)\phi}$				12+12+12	4+4+4
		$A_{LT,I}^{\cos(\phi-\phi_S)\cos(0,1,2)\phi}$				12+12+12	4+4+4
HERMES	2011	$A_{LT,I}^{\sin(\phi-\phi_S)\sin(1,2)\phi}$	0.03–0.35	1–10	<0.7	12+12	4+4
		$A_{LT,I}^{\cos(\phi-\phi_S)\cos(0,1)\phi}$				12+12	4+4
		$A_{LT,BH+DVCS}^{\sin(\phi-\phi_S)\sin\phi}$				12	4
		$A_{LT,BH+DVCS}^{\cos(\phi-\phi_S)\cos(0,1)\phi}$				12	4
HERMES	2012	$A_{LU,I}^{\sin(1,2)\phi}, A_{LU,DVCS}^{\sin\phi}, A_C^{\cos(0,1,2,3)\phi}$	0.03–0.35	1–10	<0.7	18+18+18 18+18+18+18	6+6+6 6+6+6+6
CLAS	2015	$A_{LU}(\phi), A_{UL}(\phi), A_{LL}(\phi)$	0.17–0.47	1.3–3.5	0.1–1.4	166+166+166	166+166+166
CLAS	2015	$\sigma(\phi), \Delta\sigma(\phi)$	0.1–0.58	1–4.6	0.09–0.52	2640+2640	2640+2640
Hall A	2015	$\sigma(\phi), \Delta\sigma(\phi)$	0.33–0.40	1.5–2.6	0.17–0.37	480+600	240+360

Progression of fits over the years

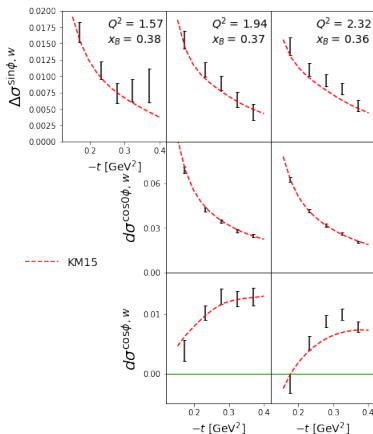
Model	KM09a	KM09b	KM10	KM10a	KM10b	KMS11	KMM12	KM15
free params.	{3}+(3)+5	{3}+(3)+6	{3}+15	{3}+10	{3}+15	NNet	{3}+15	{3}+15
$\chi^2/\text{d.o.f.}$	32.0/31	33.4/34	135.7/160	129.2/149	115.5/126	13.8/36	123.5/80	240./275
F_2	{85}	{85}	{85}	{85}	{85}		{85}	{85}
σ_{DVCS}	(45)	(45)	51	51	45		11	11
$d\sigma_{\text{DVCS}}/dt$	(56)	(56)	56	56	56		24	24
$A_{LU}^{\sin\phi}$	12+12	12+12	12	16	12+12		4	13
$A_{LU,I}^{\sin\phi}$			18	18		18	6	6
$A_C^{\cos 0\phi}$							6	6
$A_C^{\cos\phi}$	12	12	18	18	12	18	6	6
$\Delta\sigma^{\sin\phi,w}$			12				12	63
$\sigma^{\cos 0\phi,w}$			4				4	58
$\sigma^{\cos\phi,w}$			4				4	58
$\sigma^{\cos\phi,w}/\sigma^{\cos 0\phi,w}$		4			4			
$A_{UL}^{\sin\phi}$							10	17
$A_{LL}^{\cos 0\phi}$							4	14
$A_{LL}^{\cos\phi}$								10
$A_{UT,I}^{\sin(\phi-\phi_S)\cos\phi}$							4	4

- [K.K., Müller, et al. '09–'15]
- These models are publicly available (google for "gpd page")

Fit examples (1/2): H1/ZEUS

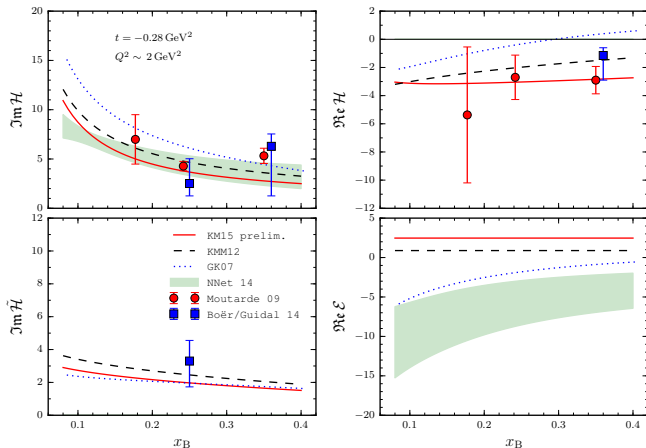


Fit examples (2/2): JLab's Hall A (2015)



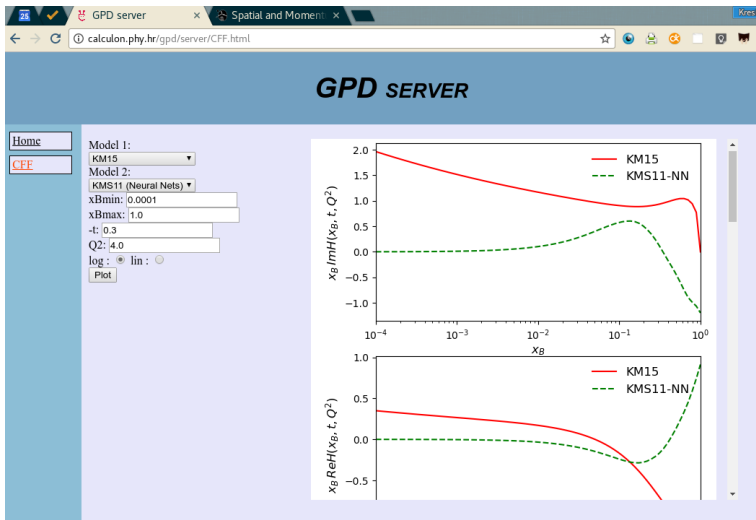
- KM15 global fit is fine. $\chi^2/n_{\text{d.o.f.}} = 240./275$ ✓

CFFs from various fits



(from [K.K., Moutarde and Liuti '16])

GPD/CFF server



- Plots of all CFFs available; numerical values soon to come ...

Accessing D-term

D-term

Matrix element of energy-momentum tensor ($a = q, g$):

$$\begin{aligned} \langle P_2 | T_{\mu\nu}^a | P_1 \rangle = & \bar{U}(P_2) \left[A^a(t) \frac{\gamma_{(\mu} P_{\nu)}}{2} + B^a(t) \frac{iP_{(\mu} \sigma_{\nu)\rho} \Delta^\rho}{4M} \right. \\ & \left. + d_1^a(t) \frac{\Delta_\mu \Delta_\nu - g_{\mu\nu} \Delta^2}{5M} \pm \tilde{c}^a(t) g_{\mu\nu} \right] U(P_1) \end{aligned}$$

- $d_1^a(0)$ — unknown intrinsic property of particle (On par with mass or spin. Related to pressure distribution. [Polyakov '03])

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$$\int dx \, x H^q(x, \eta, t) = A^q(t) + \frac{4}{5} \eta^2 d_1^q(0)$$

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$$\int dx x H^q(x, \eta, t) = A^q(t) + \frac{4}{5} \eta^2 d_1^q(0)$$

- d_1^a appears also in dispersion relations for DVCS form factors:

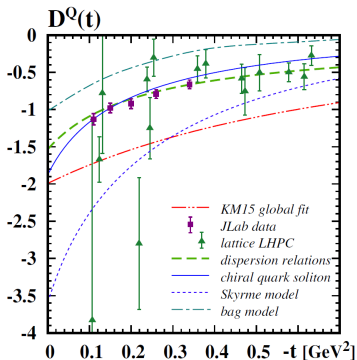
D-term: models, lattice, phenomenology

$$\Re \mathcal{H}(\xi, t) = \frac{1}{\pi} P.V. \int_0^1 dx \left(\frac{1}{\xi - x} - \frac{1}{\xi + x} \right) \Im \mathcal{H}(x, t) + \Delta(t)$$
$$\Delta(t) = 4 \sum_q Q_q^2 (d_1^q(t) + d_3^q(t) + \dots)$$

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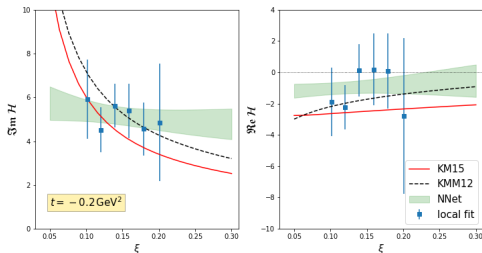
$$\Delta(t) = 4 \sum_q Q_q^2 (d_1^q(t) + d_3^q(t) + \dots)$$



[M. Polyakov, P. Schweitzer '18]

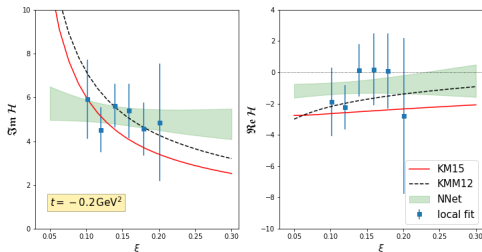
Local fit to just CLAS σ and $\Delta\sigma$

- Two parameters: $\Im\mathcal{H}$, $\Re\mathcal{H}$. Other CFFs are zero.

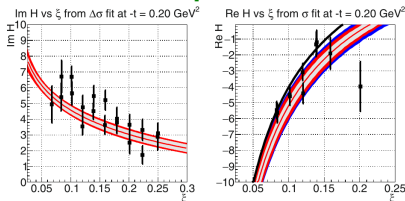


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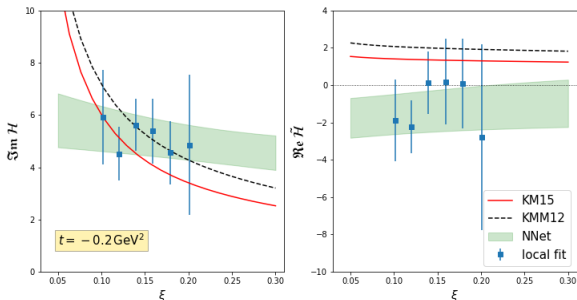
- Two parameters: $\Im m \mathcal{H}$, $\Re e \mathcal{H}$. Other CFFs are zero.



[V. Burkert, L. Eloukhiri, F.-X. Girod '18]

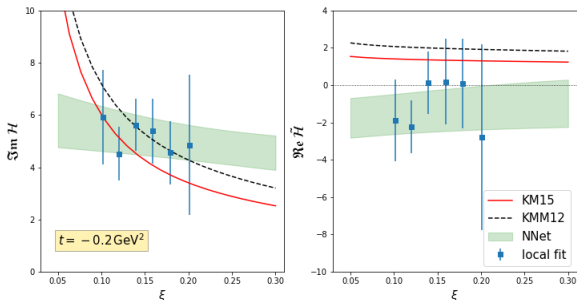


Alternative model: $\text{Im } \mathcal{H}, \text{Re } \mathcal{H} \rightarrow \text{Im } \mathcal{H}, \text{Re } \tilde{\mathcal{H}}$



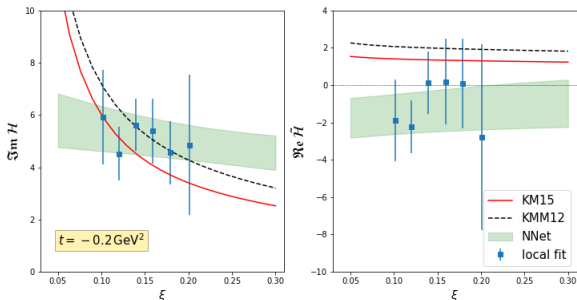
- Works just as well.

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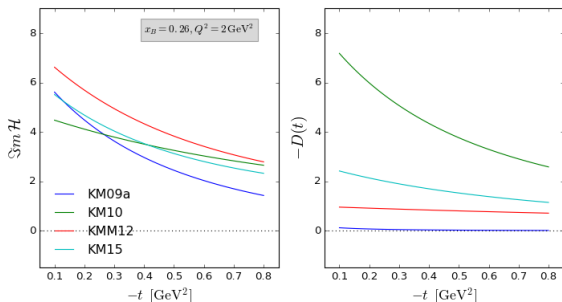
- Works just as well.
- Setting D-term to zero also works well for CLAS data alone

Alternative model: $\text{Im } \mathcal{H}, \text{Re } \mathcal{H} \rightarrow \text{Im } \mathcal{H}, \text{Re } \tilde{\mathcal{H}}$



- Works just as well.
- Setting D-term to zero also works well for CLAS data alone
- We should use all available data — global fits

D-term in global fits over the years



- Better constraint on D-term: measurement of beam **charge** asymmetry, **double DVCS**, ...

Higher twists?

Including higher twists

- Definition of Compton form factors to given twist is convention dependent (e.g. choice of (n, \tilde{n}) —longitudinal plane)
- BMJ [Belitsky, Müller, Ji]: $\mathcal{H}_{++}, \mathcal{E}_{++}, \dots, \mathcal{H}_{0+}, \mathcal{E}_{0+}, \dots,$
- BMP [Braun, Manashov, Pirnay]: $\underbrace{\mathbb{H}_{++}, \mathbb{E}_{++}}_{\text{twist-2} + \dots}, \dots, \mathbb{H}_{0+}, \mathbb{E}_{0+}, \dots,$
- Lorentz transformation from BMP to BMJ frame:

$$\mathcal{H}_{++} = \mathbb{H}_{++} + \frac{\chi}{2}(\mathbb{H}_{++} + \mathbb{H}_{-+}) - \chi_0 \mathbb{H}_{0+}$$

$$\mathcal{H}_{0+} = -(1 + \chi)\mathbb{H}_{0+} + \chi_0(\mathbb{H}_{++} + \mathbb{H}_{-+})$$

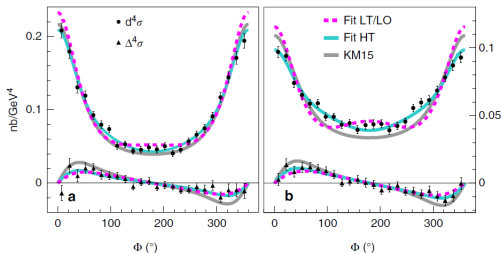
collects most of the HT effects.

$$\chi_0 \sim \mathcal{O}\left(\frac{1}{Q}\right), \quad \chi \sim \mathcal{O}\left(\frac{1}{Q^2}\right)$$

Leading (LT) vs. higher twist (HT) models

- JLab's Hall A performed fits to their 2017 data using BMP conventions (separate fit for each t -bin):

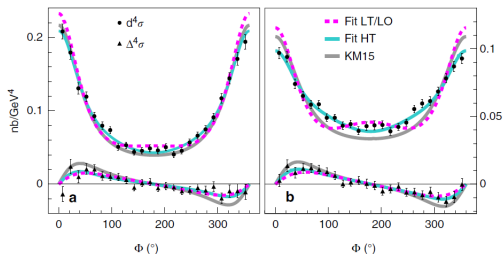
LT/LO	\mathbb{H}_{++} , \mathbb{E}_{++} , $\tilde{\mathbb{H}}_{++}$, $\tilde{\mathbb{E}}_{++}$	✗ bad fit
HT	\mathbb{H}_{++} , \mathbb{H}_{0+} , $\tilde{\mathbb{H}}_{++}$, $\tilde{\mathbb{H}}_{0+}$	✓ good fit
NLO	\mathbb{H}_{++} , \mathbb{H}_{-+} , $\tilde{\mathbb{H}}_{++}$, $\tilde{\mathbb{H}}_{-+}$	✓ good fit



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HT	\mathbb{H}_{++} , \mathbb{H}_{0+} , $\tilde{\mathbb{H}}_{++}$, $\tilde{\mathbb{H}}_{0+}$	✓ good fit
NLO	\mathbb{H}_{++} , \mathbb{H}_{-+} , $\tilde{\mathbb{H}}_{++}$, $\tilde{\mathbb{H}}_{-+}$	✓ good fit



- Hall A conclusion: “We glimpse gluons here!” (at $x_B = 0.36$)

LT vs. HT: chi-squares

- $n_{\text{d.o.f.}} = 208 \pm 2$

		BMP (\mathbb{F})		
		LO/LT	HT	NLO
t/GeV^2				
Hall A:	-0.18	250 ✗	204 ✓	206 ✓
	-0.24	367 ✗	206 ✓	208 ✓
	-0.30	415 ✗	189 ✓	190 ✓

LT vs. HT: chi-squares

- $n_{\text{d.o.f.}} = 208 \pm 2$

		BMP (F)		
		LO/LT	HT	NLO
Hall A:	t/GeV^2			
	-0.18	250 ✗	204 ✓	206 ✓
	-0.24	367 ✗	206 ✓	208 ✓
	-0.30	415 ✗	189 ✓	190 ✓

		BMP (F)		
		LO/LT	HT	NLO
This work:	t/GeV^2			
	-0.18	231 ✗	204 ✓	N/A
	-0.24	254 ✗	199 ✓	N/A
	-0.30	229 ✗	180 ✓	N/A

LT vs. HT: chi-squares

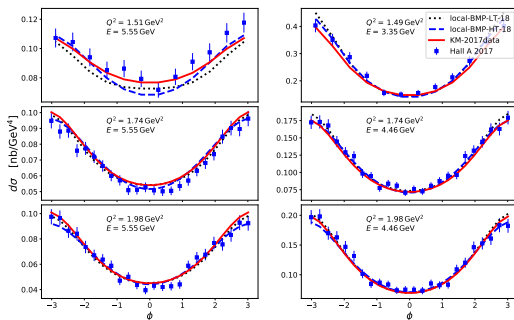
- $n_{\text{d.o.f.}} = 208 \pm 2$

		BMP (\mathbb{F})			
		t/GeV^2	LO/LT	HT	NLO
Hall A:	-0.18	250 \times	204 \checkmark	206 \checkmark	
	-0.24	367 \times	206 \checkmark	208 \checkmark	
	-0.30	415 \times	189 \checkmark	190 \checkmark	

		BMP (\mathbb{F})			BMJ (\mathcal{F})	
		t/GeV^2	LO/LT	HT	NLO	LT (KM)
This work:	-0.18	231 \times	204 \checkmark	N/A	213 \checkmark	
	-0.24	254 \times	199 \checkmark	N/A	210 \checkmark	
	-0.30	229 \times	180 \checkmark	N/A	213 \checkmark	

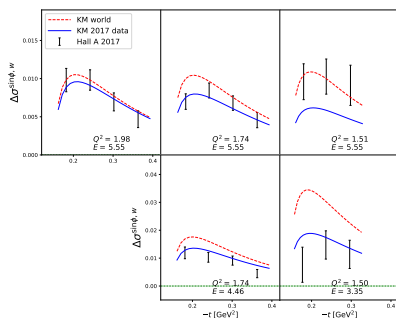
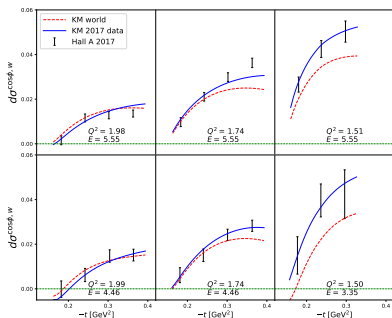
Hall A 2017 $d\sigma$

- $t = -0.18 \text{ GeV}^2$



- Conclusion: Hall A 2017 data **alone** can be satisfactorily described within twist-2 framework

Including Hall A 2017 data in global world fit: fail ✗



Global world DVCS data fit

before 2017

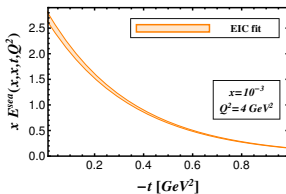
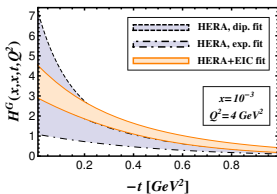
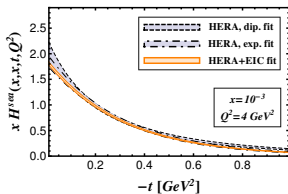
$$\chi^2/n_{\text{d.o.f}} = 240./275 \checkmark$$

including 2017 Hall A

$$\chi^2/n_{\text{d.o.f}} = 545./337 \times$$

DVCS at EIC

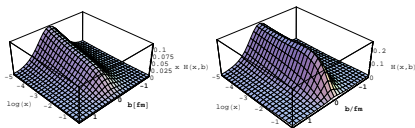
- Future polarized electron-ion collider (EIC) will provide unique insight into sea GPDs.
- [Aschenauer, Fazio, K.K., Müller '13] fit to simulated DVCS data at $20 \text{ GeV} \times 250 \text{ GeV}$ taking $E_{\text{sea}}(x, \eta, t) = \kappa_{\text{sea}} H_{\text{sea}}(x, \eta, t)$



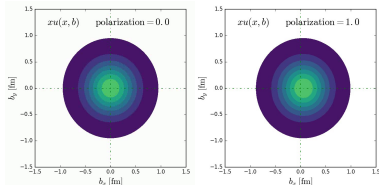
- Improved knowledge of low- t quark and gluon GPDs H (\implies 3D parton imaging)
- Improved knowledge of sea quark GPD E

Tomography

- Quark and gluon sea 2D distributions $H(x, \vec{b}_\perp)$ ([KM] model)



- Sivers effect for valence quarks ([GK] model)



- See also [Dupré, Guidal, Vanderhaeghen '16]
- Tomography is still very much model-dependent; e.g. some extrapolation from $H(x, x, t)$ to $H(x, 0, t)$ is needed.

Summary

- Global fits of all proton DVCS data using flexible hybrid models were in healthy shape until 2017
- Standard global model fitting and neural networks approach are complementing each other
- First steps are made towards extracting the D-term
- Inclusion of higher twist effects is likely important for interpretation of new JLab data, but maybe not for quality of description of this data
- New Hall A 2017 data present a challenge

Summary

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The End