

Particle Detectors

Their principles and applications

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at Pohang Korea
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- 4. Examples and discussions
 - Magnetic spectrometer
 - ν detectors
 - Comments

References

: books from which tables or figures are cited

- 「Detectors for particle radiation」 K. Kleinknecht (Mainz)
Cambridge Univ. Press 1986 **KK**
- 「Radiation detection and measurement」 G. F. Knoll (Michigan)
John Wiley and Sons 1979 **Knoll**
- 「Review of Particle Physics」 Particle Data Group
Chinese Physics C 40 2016 **PDG**
- 「Principles of Operation of Multi Wire Proportional and Drift Chambers」
F. Sauli, CERN 77-9 1977 **Sauli**

1. Introduction

1-1 Self introduction

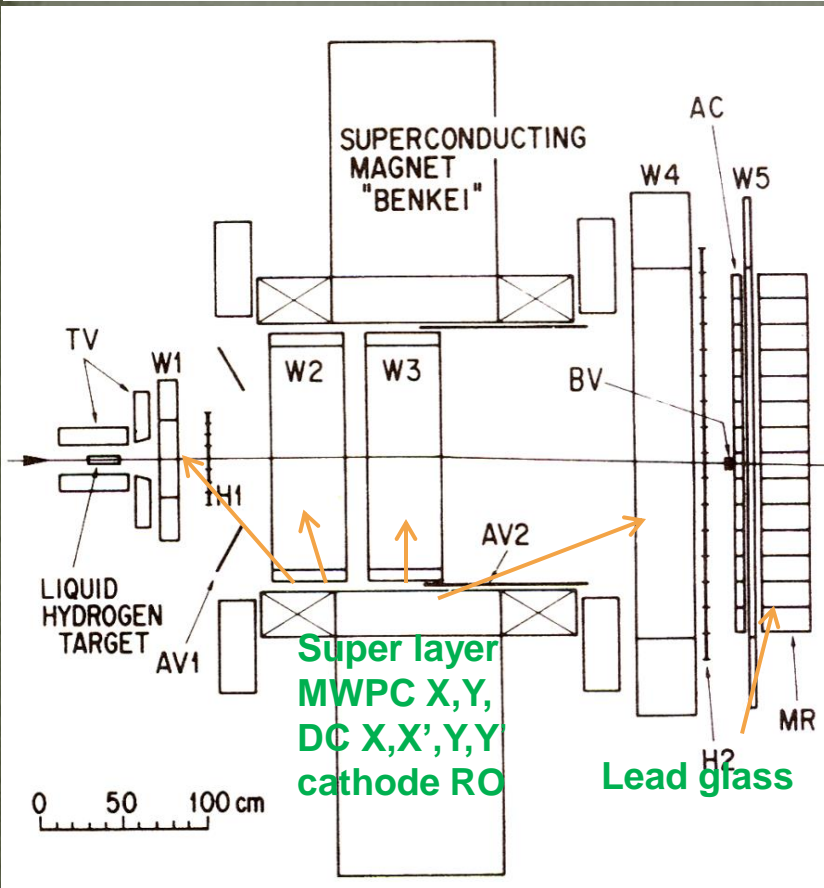
I have performed three search-for experiments
at **KEK 12 GeV proton synchrotron**.

E64 in 1980's “search for glue-ball”

E137 in 1990's “search for lepton flavor
violation”

E391a in 2000's “search for direct CP violation”
succeeded by KOTO at JPARC

**Large solid angle for multi-tracks.
Charged and gamma spectrometer.**



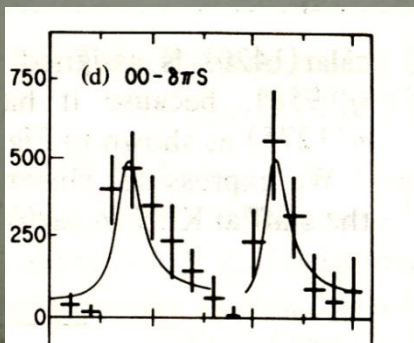
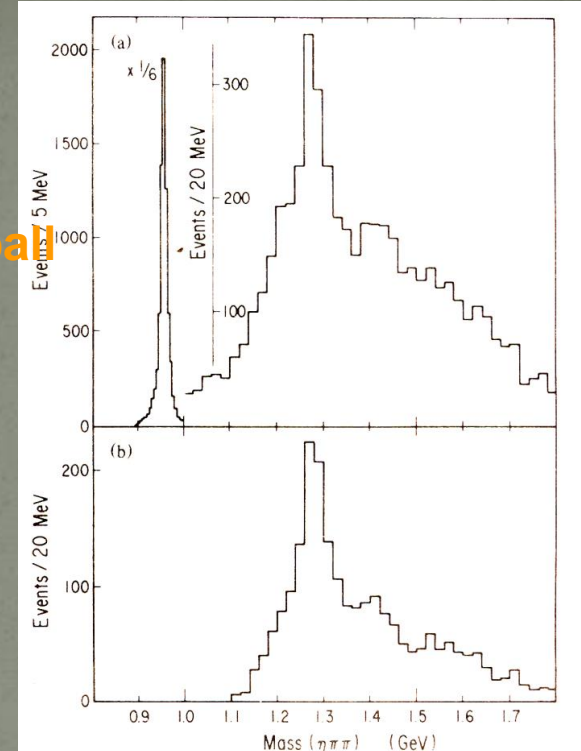
E64

Search for glueball

$\pi p \rightarrow M^0 n$

$M^0 \rightarrow \eta \pi^+ \pi^-$

$\rightarrow \gamma \gamma$
 $\rightarrow \pi^0 \pi^+ \pi^-$
 $\gamma \gamma$

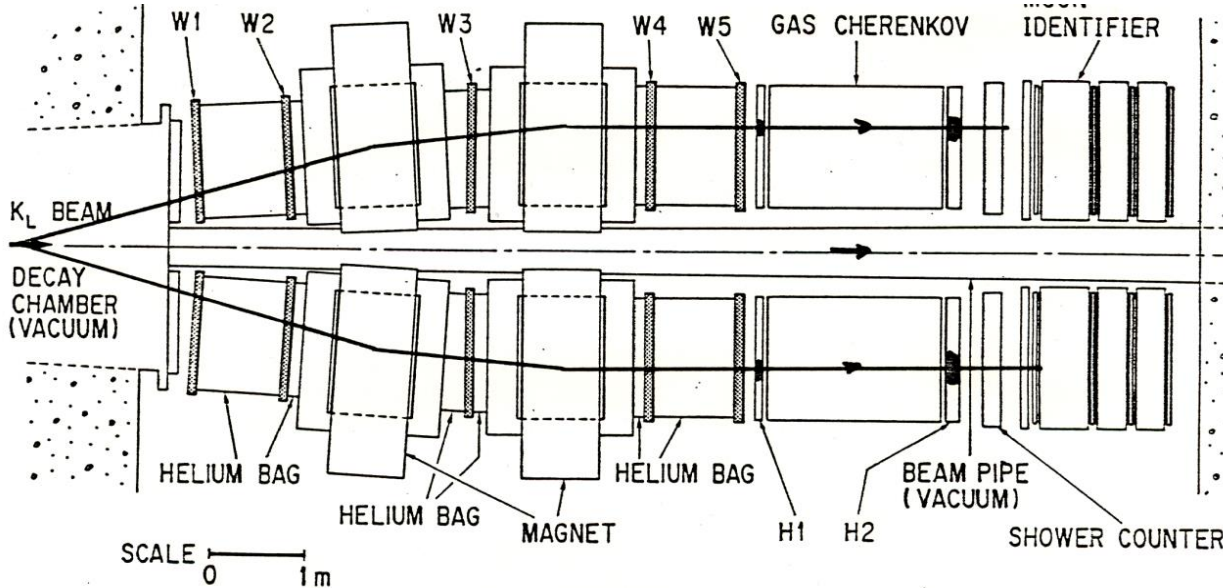


We observed two pseudo-scalar resonances which are consistent with radial excited states of η and η' , and killed a possibility of the glue ball assignment to the state of 1420 MeV.

E137 $K_L \rightarrow \mu e, \mu\mu, ee$ and $eeee$

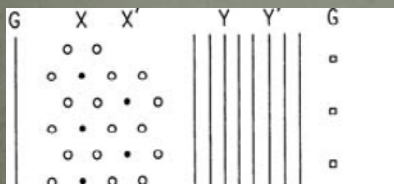
High sensitivity ($10^{-11}BR$) ~ heavy backgrounds

Double-arm spectrometer, two stage spectrometer

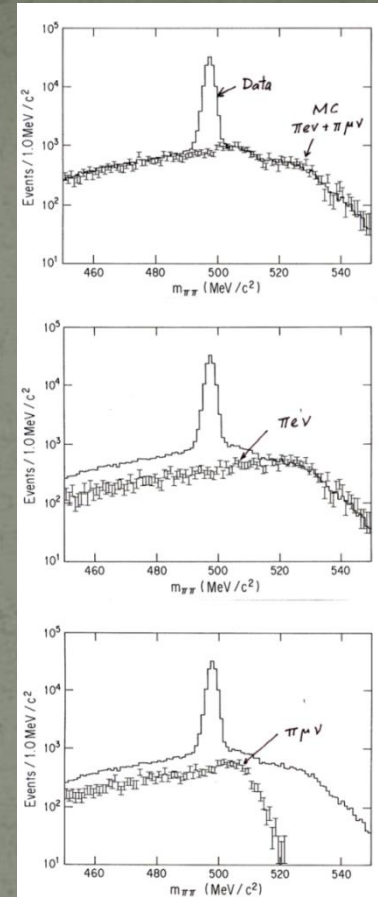
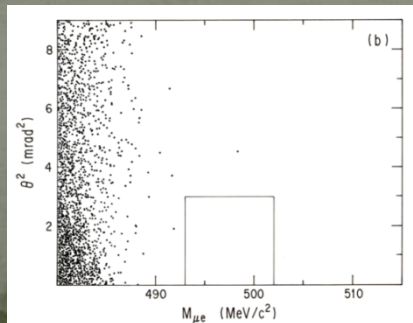


High rate: thin material to reduce n, γ interactions, He-bags, very thin vacuum window.

Wi: Drift Chamber X, X', Y, Y, no separation, Aluminum wire,



- cathode (Al)
- sense wire (W)



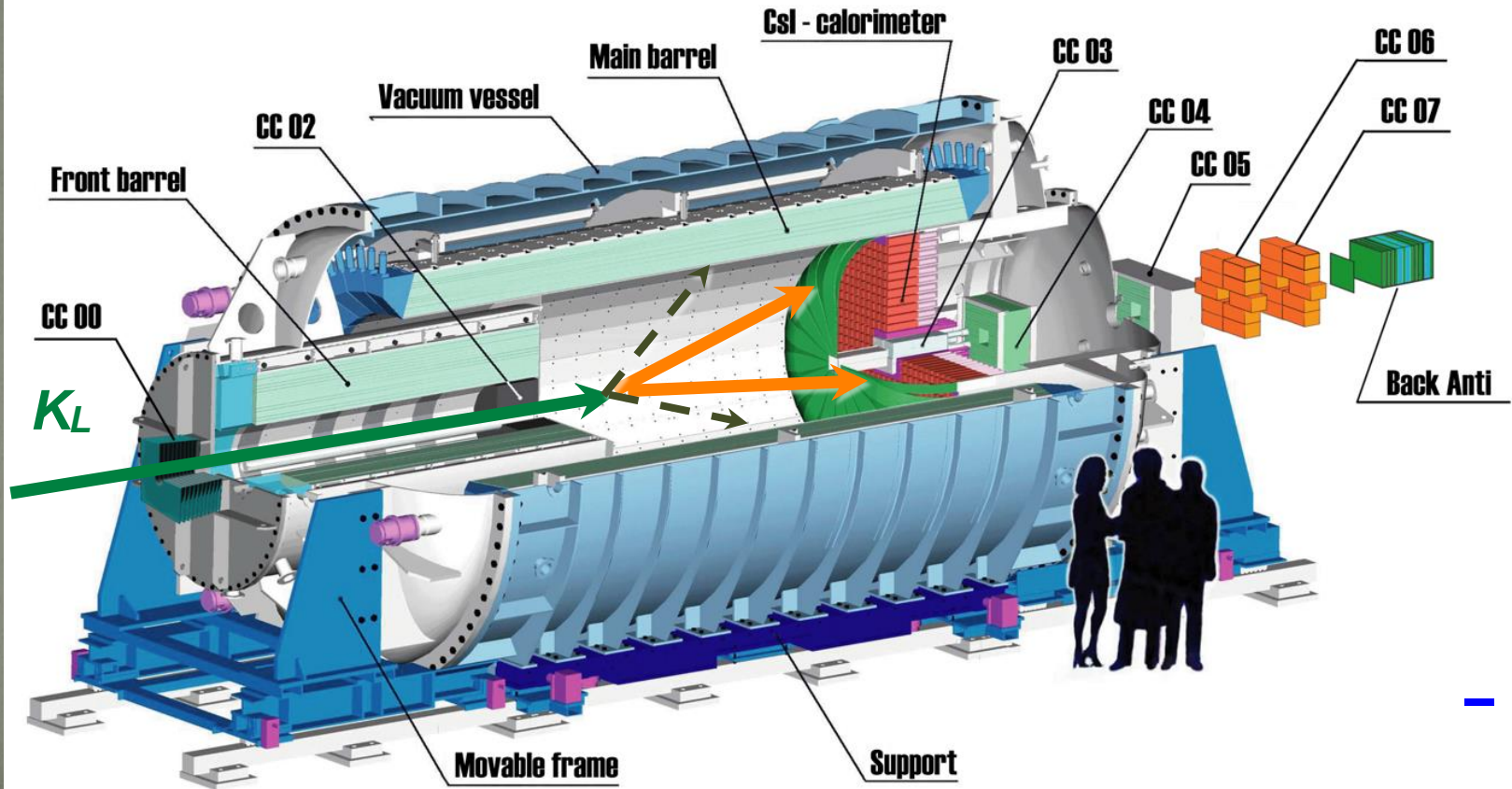
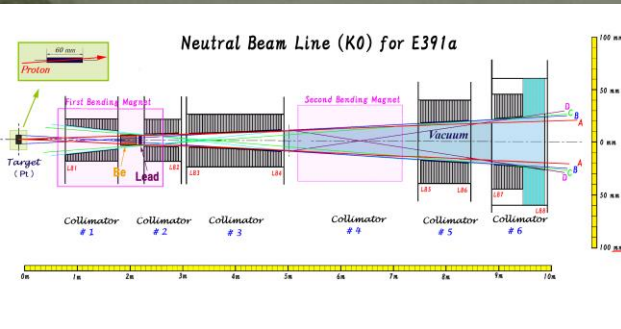
$\pi^+\pi^-$ mass

With a good mass resolution of 1.4 MeV, the upper limit 9.4×10^{-11} was set and it was the world record for two years.

Mostly ruled out the Technicolor Model.

E391a $K_L \rightarrow \pi^0 \nu \nu$

High sensitivity (heavy background) and a little kinematical constraint : thin and sharp beam, detector in vacuum, tight veto.(full coverage and low threshold).



Summary of three experiments

- E64: multi-particle (track) measurements with the charge-gamma spectrometer
 - Large aperture using superconducting magnet
 - Super-layer structure of position
- E137: high resolution under high rate environment
 - Two-arm spectrometer
 - Thin materials in the upstream part
- E391a: super-sensitive vetoing
 - Sharply-collimated neutral beam
 - Detectors in vacuum

Introductory message

Even from examples of these few experiences,

“Detector is closely relate with physics, like as a telescope for astronomer. Deep world can only be explored with well polished detectors”

Classification

Medium

Gas chamber

Scintillator

Semi-conductor



Measurement (Application)

Track measurement

(Spectrometer: momentum,
direction, vertex)

dE/dx measurement

(calorimeter, particle-ID)

1-2 Particle interaction with matter

- Charged particle interaction with matter (ionization) is utilized for particle detector.
- Neutral particles (n, γ, ν) have to be converted to charged particle through production interaction with matter.

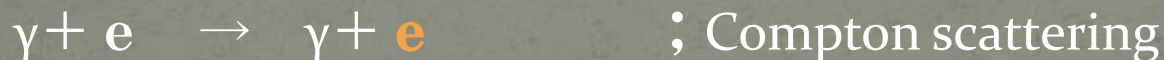
Strong, Electromagnetic and Weak interactions

Interactions to convert n, γ, ν to charged particles

n : Strong interaction



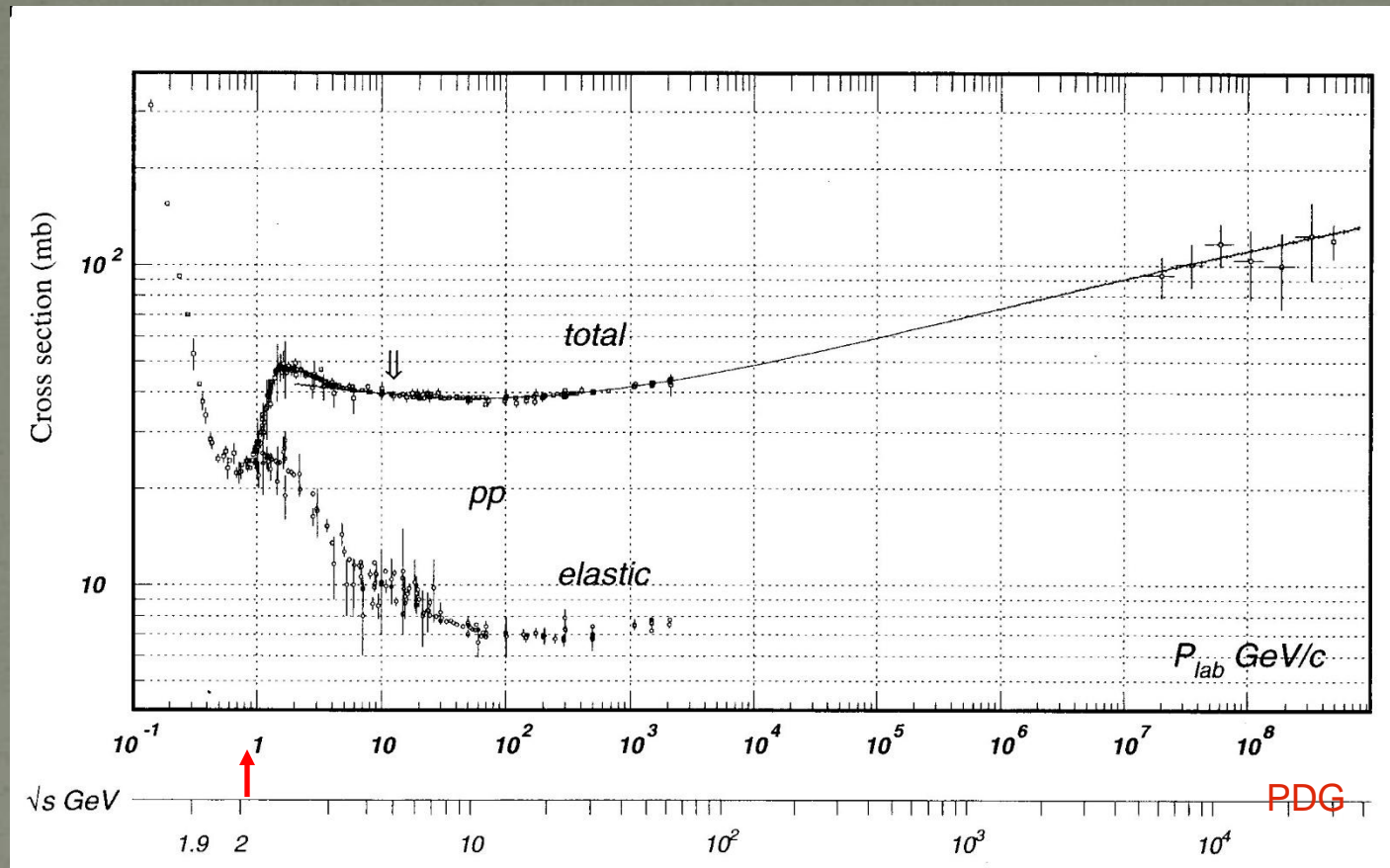
γ : Electro-magnetic interaction



ν : Weak interaction



Strong interaction: Cross section of pp interaction



π

threshold:

$$(E_p + m_p)^2 - p_{Lab}^2 = s = (2m_p + m_\pi)^2,$$

$$E_p^2 = p_p^2 + m_p^2$$

$$pp \sim pn \sim nn: \sigma_A \sim A\sigma_N$$

\Rightarrow Interaction rate \propto thickness in the unit of gr/cm²

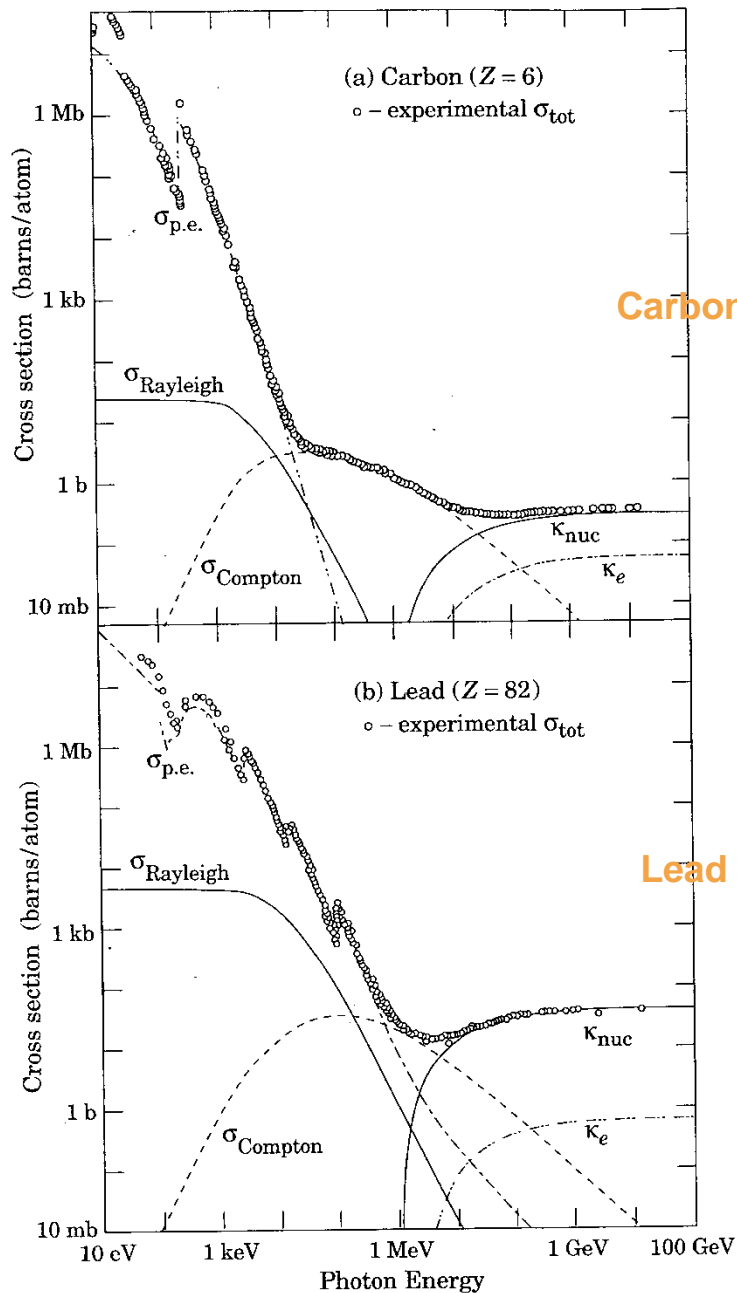
Energy-independent cross section

\Rightarrow can define **nuclear-interaction-length**

for $E > 1$ GeV reactions

E-M interaction

Cross section of photon



Carbon

Lead

Photo-electron emission (p.e.) $\propto Z^5$

Compton scattering (Compton) $\propto Z$

Pair creation (K_{nuc}) $\propto Z^2$

Effect of Compton scattering is large for light material around the energy of MeV.

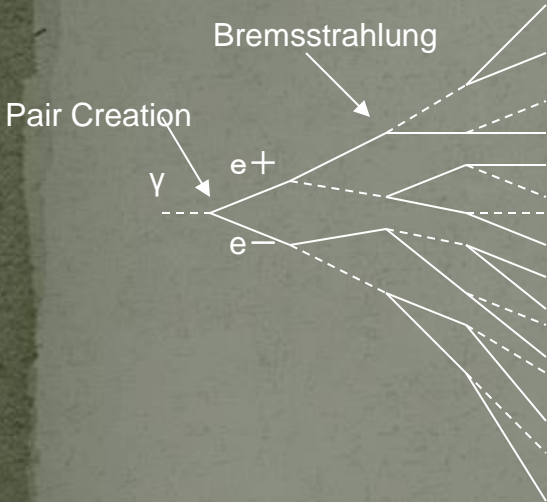
Pair creation is dominant for $E > 10\text{MeV}$ and its cross section is energy independent. \Rightarrow can define radiation-length

More exactly, the definition of radiation length comes from the facts:

1. Pair-creation ($\gamma + A \rightarrow e^+ e^- + A$) is dominant and the cross section is constant with energy above 10MeV.
2. Pair creation from photon ($\gamma + A \rightarrow e^+ e^- + A$) and bremsstrahlung of electron (positron) ($e + A \rightarrow e + \gamma + A$) are the same process.

Equal mean-free-path (\sim radiation length $[X_0]$) for γ and e^\pm of any energy.

Cascade shower in a medium



When the thick medium ($>10 X_0$) is a detector, it is calorimeter.

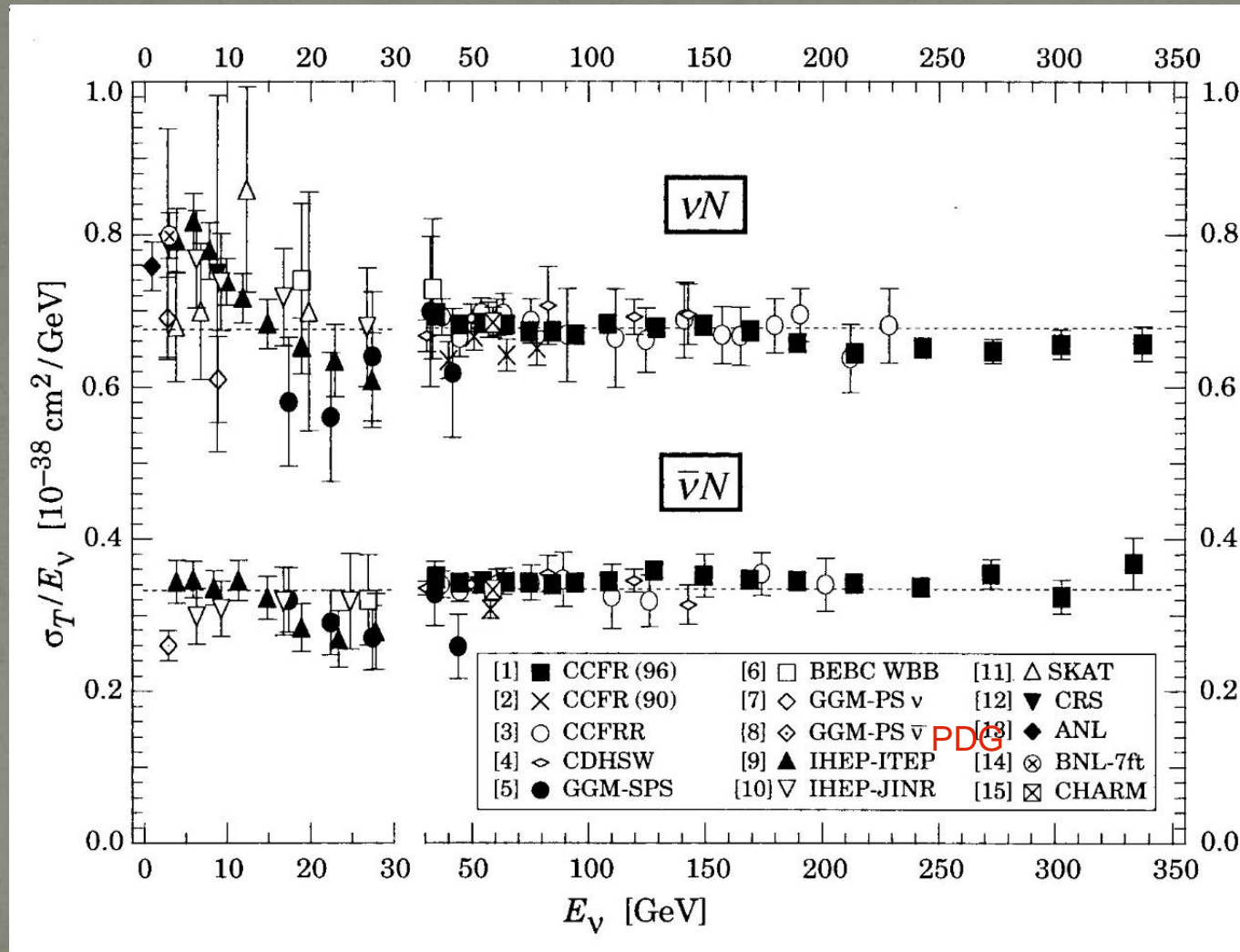
Incident energy (E) \propto Sum of deposit energies of e^\pm in the detector \propto Total track length of e^\pm because of the energy independent dE/dx \propto The number of PC and B processes (N_{proc}) because of equal mean-free-path

Fluctuation $\Delta E/E \propto 1/\sqrt{N_{proc}} \propto 1/\sqrt{E}$

Preference of heavy material :

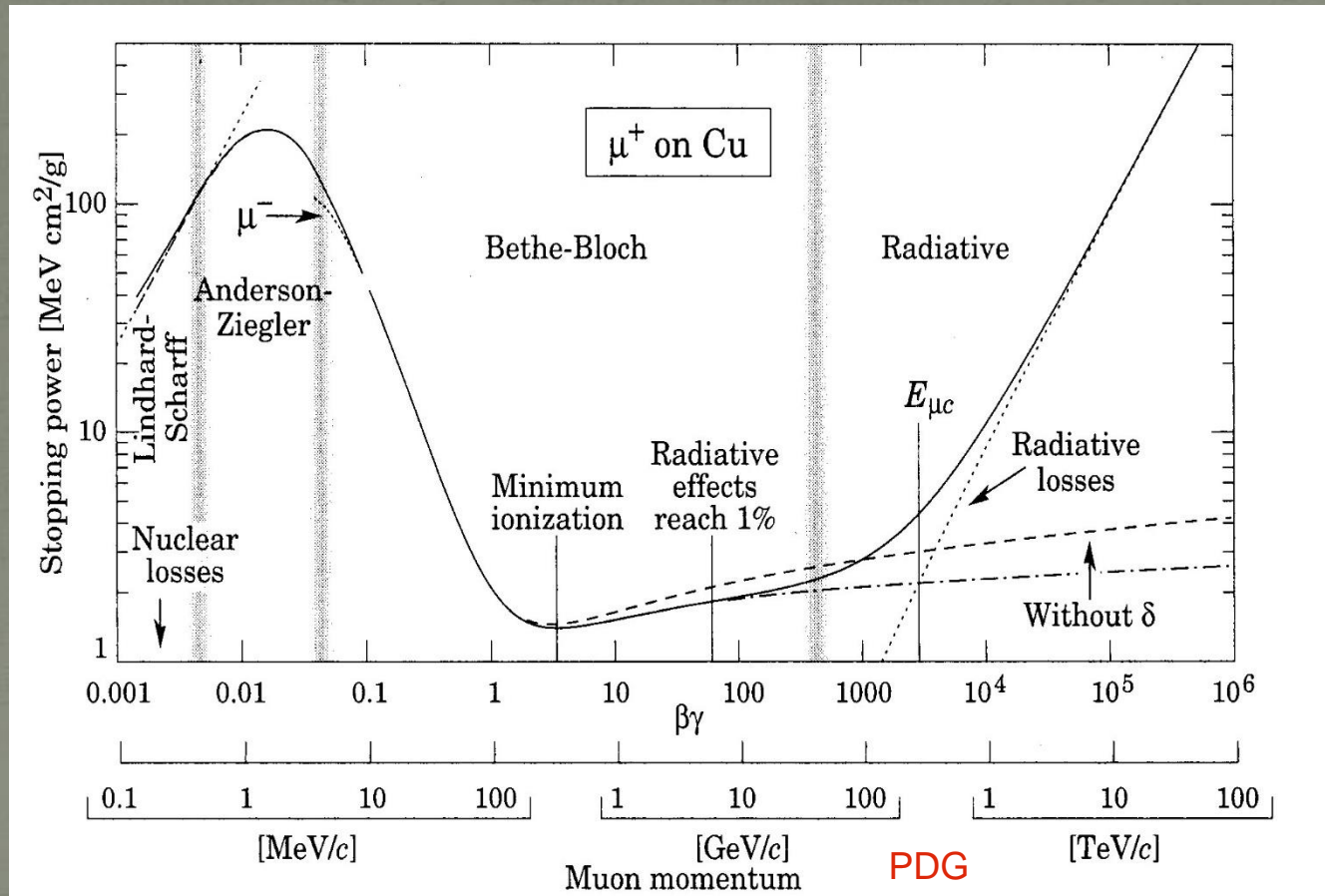
1. Small size due to shorter radiation length.
2. More chance of PC and B processes because heavy material is productive down to low energy.

Weak interaction: Charged-current cross section of $\nu_\mu p$



Charged-particle interaction with material

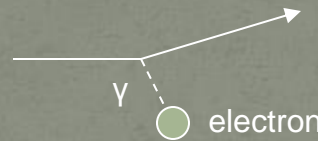
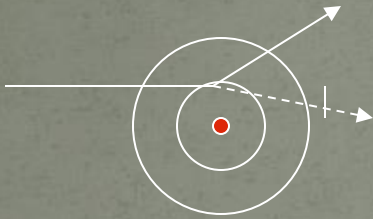
which basically determines detector response



No particle dependence and single function of β and γ (velocity) in Bethe-Bloch region. The dE/dx is almost flat in the region of $\beta\gamma=1\sim 1000$ with the minimum of $dE/dx\sim 2 \text{ MeV}/(\text{g}/\text{cm}^2)$.

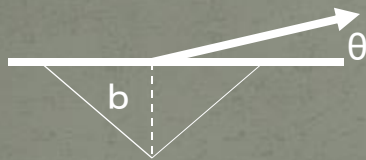
Bethe-Bloch formula : well-reproduce the dE/dx of the particle in the velocity region of particle nuclear physics.

$$-dE/dx = Kz^2(Z/A)(1/\beta^2)[1/2 \ln\{2mc^2\gamma^2\beta^2 T_{\max} / I\} - \beta^2 - \delta/2]$$



Rutherford scattering

Number of target electrons in 1 gr/cm²: $N_A \cdot Z / A$



b ; impact parameter

$$\Delta p = \int F dt = ze^2 / (4\pi\epsilon_0 b^2) \cdot 2b / v$$

$$\Delta p = p \cdot \theta$$

$$b = ze^2 / (2\pi\epsilon_0 v p) \cdot 1/\theta$$

$$db = ze^2 / (2\pi\epsilon_0 v p) \cdot 1/\theta^2 d\theta$$

$$d\sigma = 2\pi b db$$

$$= 2\pi \{ ze^2 / (2\pi\epsilon_0 v p) \}^2 \cdot 1/\theta^3 d\theta$$

$$T_e = (\Delta p)^2 / 2m = (p^2 / 2m) \theta^2$$



Bethe-Bloch formula (continued)

$$-dE/dx = Kz^2(Z/A)(1/\beta^2)[1/2\ln\{2mc^2\gamma^2\beta^2 T_{\max} / I\} - \beta^2 - \delta/2]$$

Energy loss in 1 gr /cm²

$$-dE / dx = NA Z / A \int_{\theta_{\min}}^{\theta_{\max}} T(\theta) (d\sigma / d\theta) d\theta$$

$$= K z^2 (Z / A) (1/\beta^2) \ln (\theta_{\max} / \theta_{\min})$$

$$K/A = 4\pi NA re^2 mc^2 / A = 0.307075 \text{ MeV}/(\text{g}/\text{cm}^2)$$

for A=1 g/mol

$$re = e^2 / (4\pi\epsilon_0^2 mc^2) ; \text{ electron (classical) radius} \\ = 2.817940325(28) \text{ fm}$$

$$\Theta = (2mT)^{1/2} / p$$

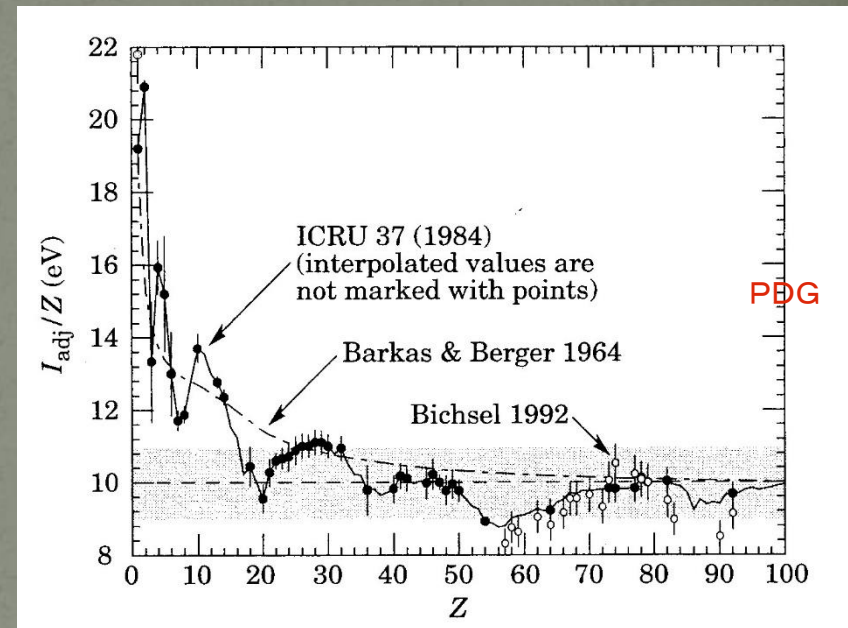
$$\ln (\theta_{\max} / \theta_{\min}) = (1/2) \ln (T_{\max} / T_{\min})$$

$$T_{\min}; I = p^2 / 2m - (p - \Delta p_{\min})^2 / 2M = (p / m) \Delta p_{\min}$$

$$T_{\min} = (\Delta p_{\min})^2 / 2m = (m^2 / p^2) (I / m)$$

$$p = \beta \gamma m c$$

$$\ln (\theta_{\max} / \theta_{\min}) = (1/2) \ln (2mc^2 \beta^2 \gamma^2 T_{\max} / I)$$



Cosmic ray flux with the altitude

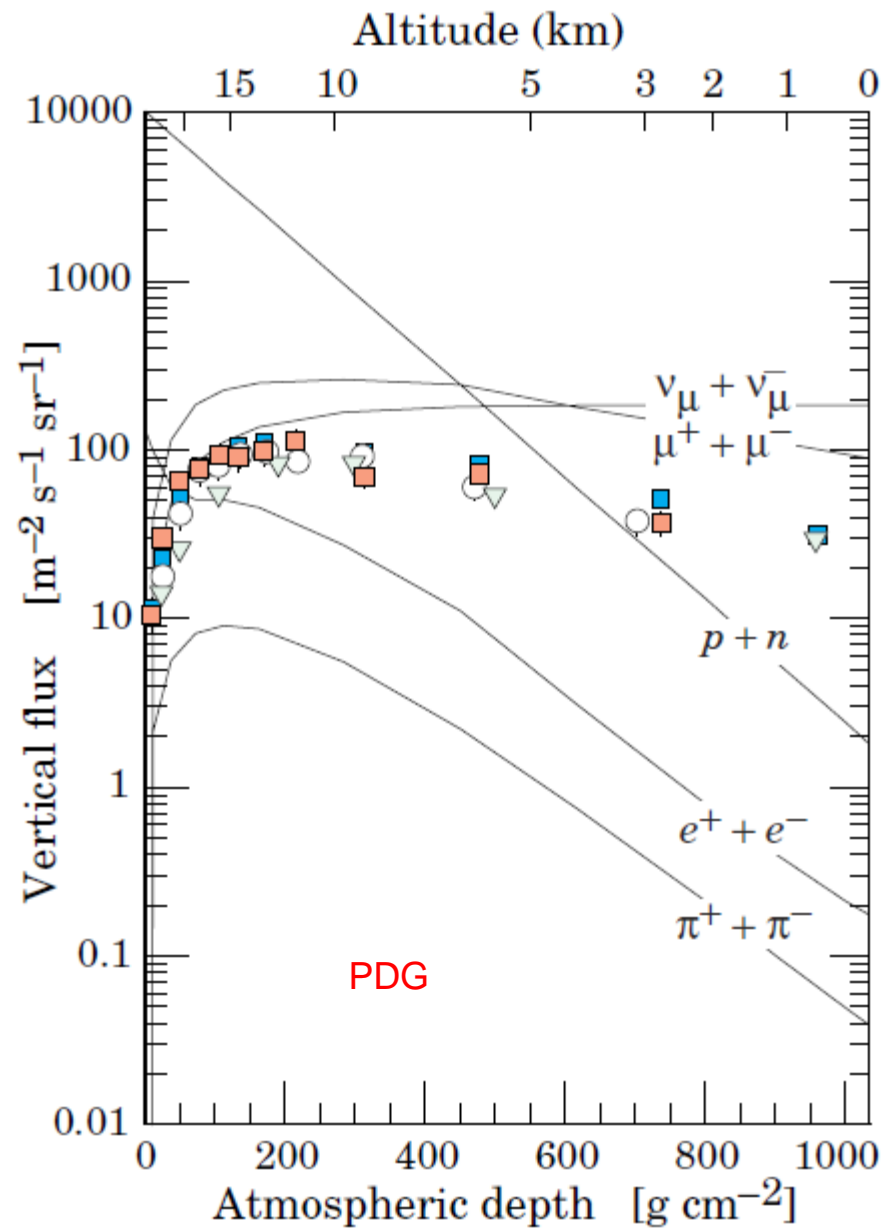


Figure 30.4: Vertical fluxes of cosmic rays in the atmosphere with $E > 1$ GeV estimated from the nucleon flux of Eq. (30.2). The points show measurements of negative muons with $E_\mu > 1$ GeV [41–45].

2. Track measurement

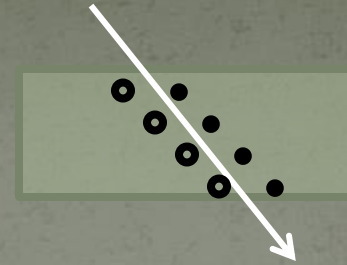


Gas chamber

Contents

- Seeds and multiplication
- Gas selection
- Drift velocity
- Example
- Problems: positive ion, diffusion,
- TPC

Seed



Seed: electron-ion pairs in the gas.

The Number of seed = deposit energy in the gas / W

- W is the required energy deposit for one pair: it is not so varied with incident particles and gas. It is around **30 eV**.

- Deposit energy in Argon gas of 1 cm thick

$$\text{energy loss} = 2 \text{ MeV}/(\text{gr}/\text{cm}^2)$$

$$\text{material thickness} : 40 \text{ g} / (22.4 \times 10^3) \text{cm}^3 \times 1 \text{ cm}$$

$$= 1.8 \times 10^{-3} \text{ gr}/\text{cm}^2$$

$$= 2 \text{ MeV}/(\text{gr}/\text{cm}^2) \times 1.8 \times 10^{-3} \text{ gr}/\text{cm}^2 = \mathbf{3.6 \text{ keV}}$$

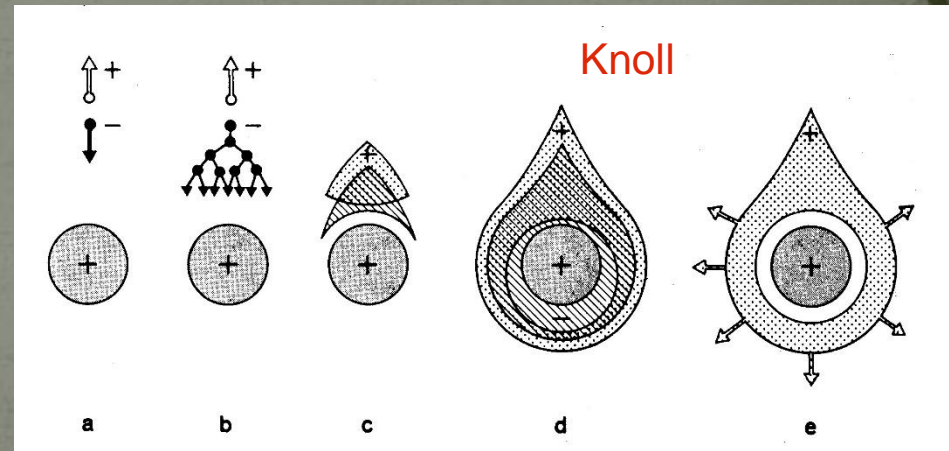
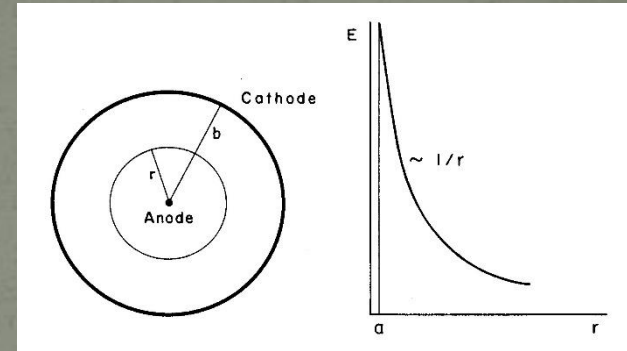
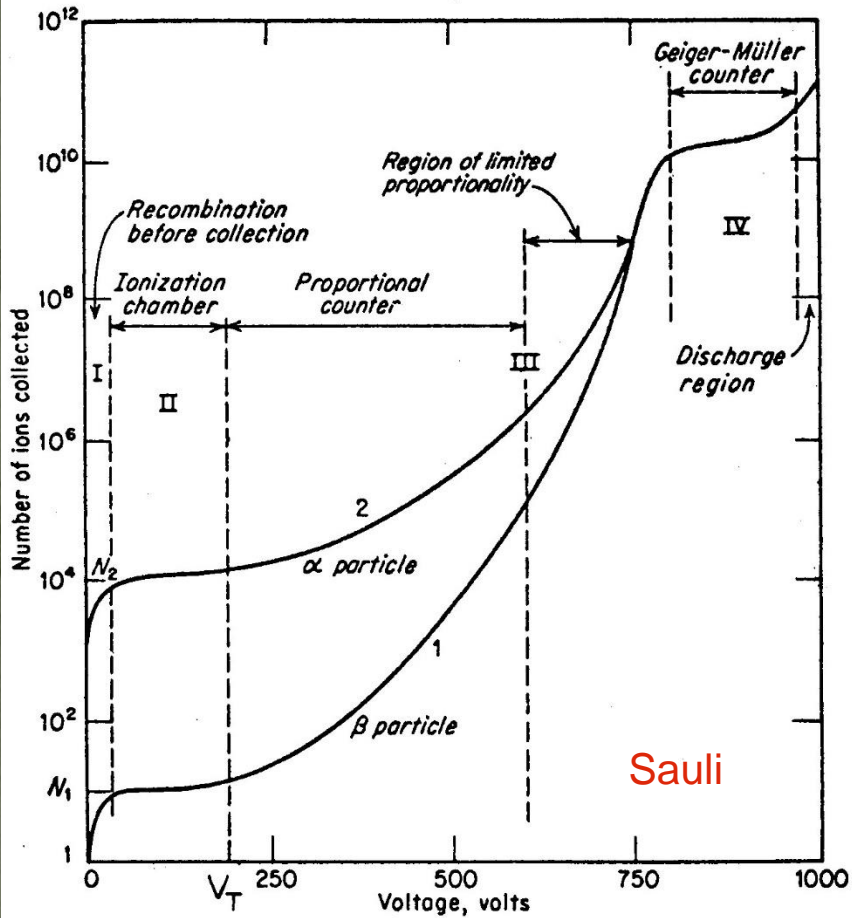
Then, the number of seed = **120**

$$\text{Capacitive readout with } 100 \text{ pF} \quad 120 \times 1.6 \times 10^{-19} / (100 \times 10^{-12}) = 1.9 \times 10^{-7} \text{ V}$$

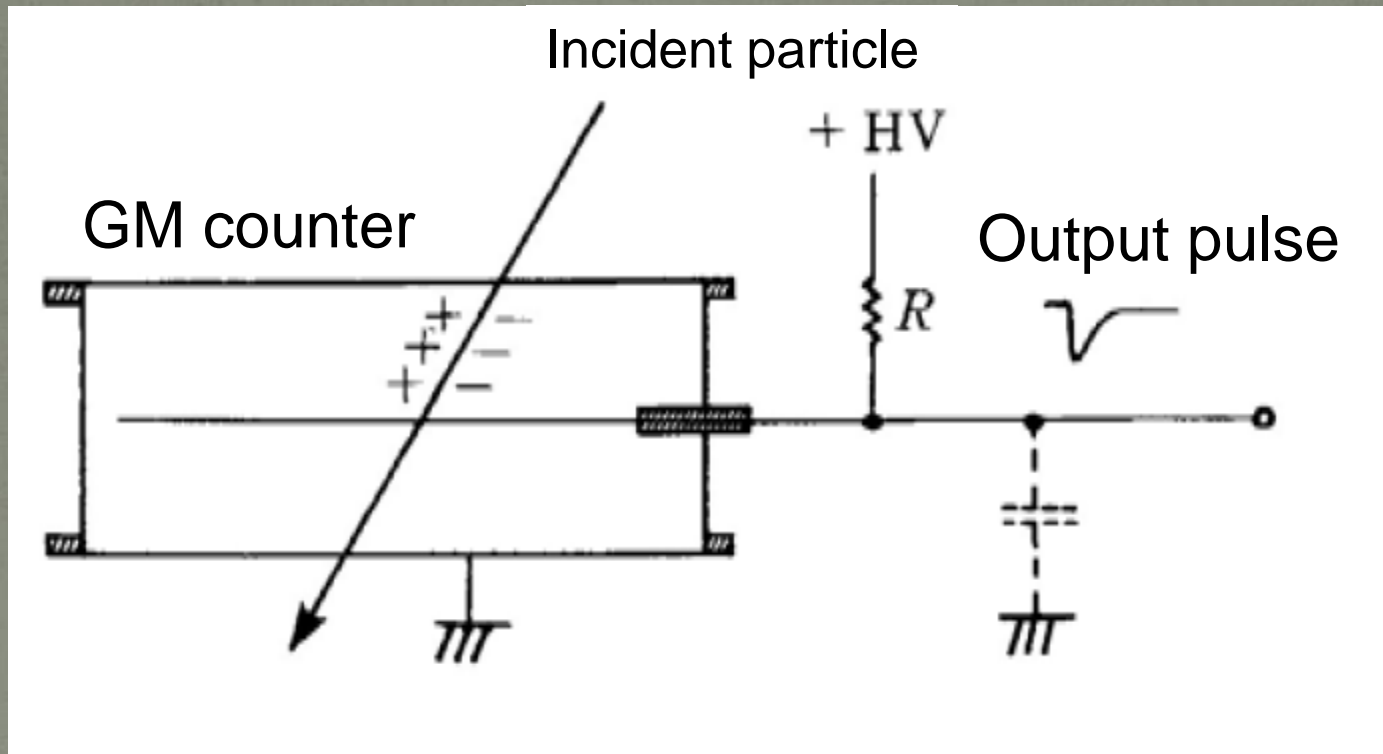
$$\text{Current through } 0.1 \text{ } \mu\text{sec propagation} \quad 120 \times 1.6 \times 10^{-19} / (1 \times 10^{-7}) = 1.9 \times 10^{-10} \text{ A}$$

Too small. Necessary for signal amplification

Multiplication in gas



Giger-Muller counter



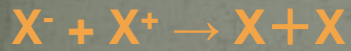
Self quenching type

Choice of gas

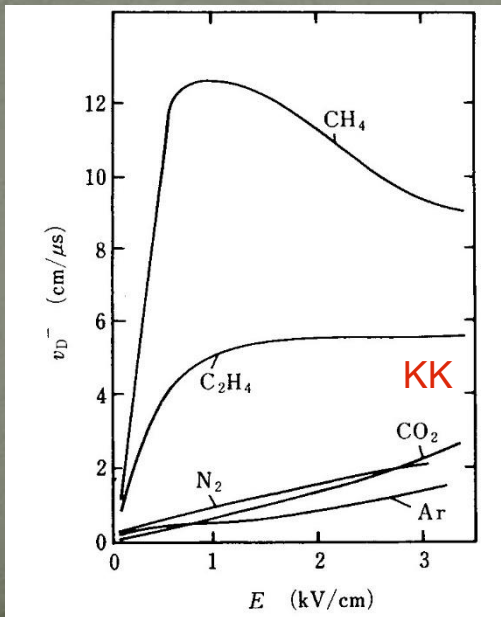
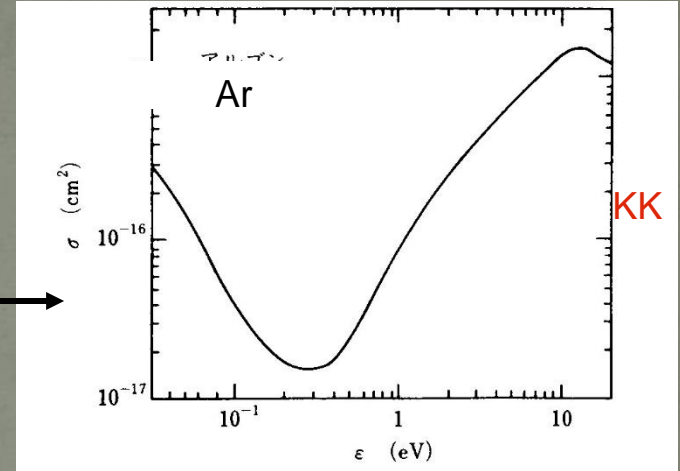
Little recombination for inert gas or nitrogen.

How does a recombination happen?

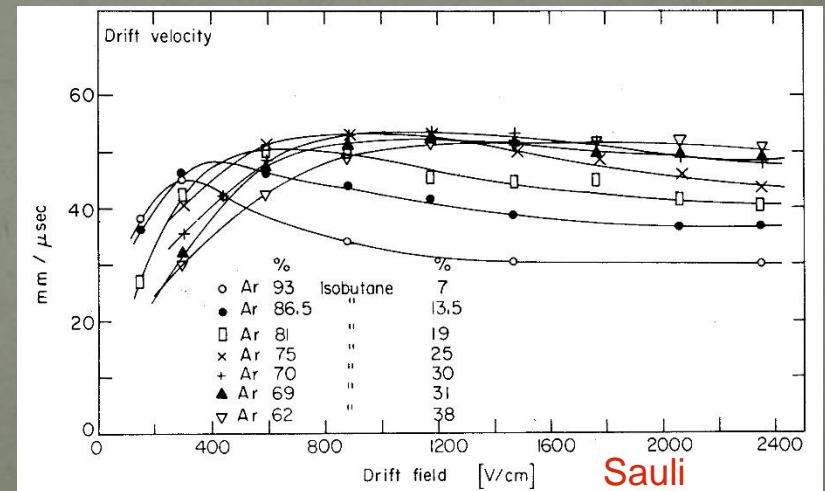
For ion pair: e^- , X^+ ,



Ramsauer effect:
Cross section of e^-X^+ reaction

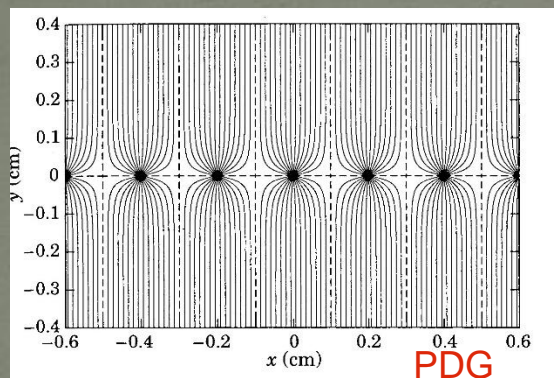


Gas mixture

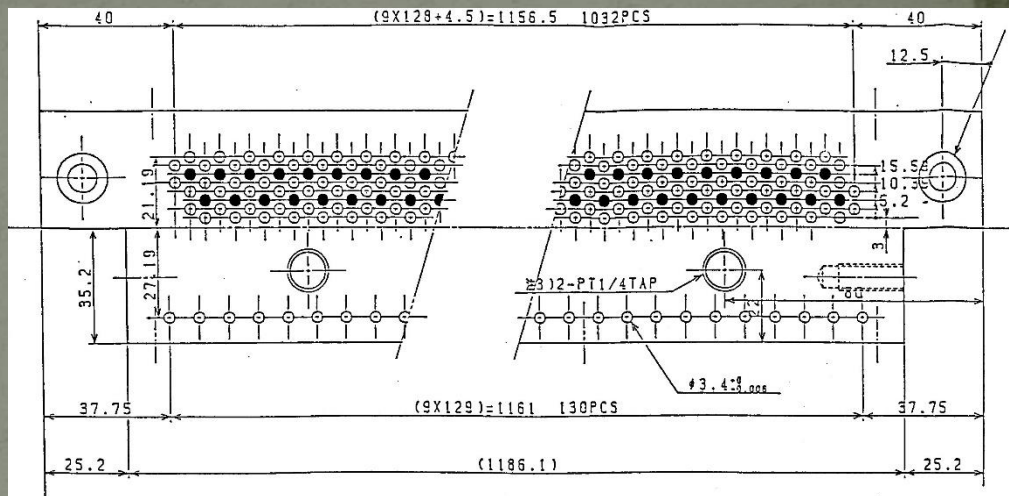


Drift velocity does not depend on the electric field

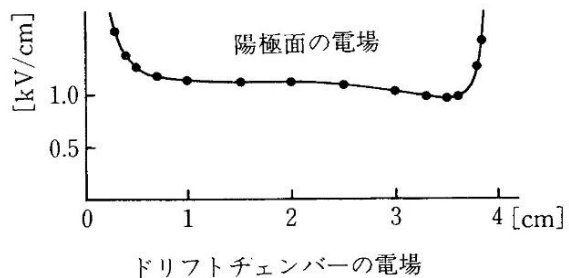
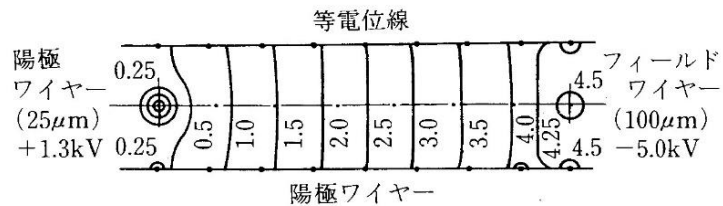
Examples



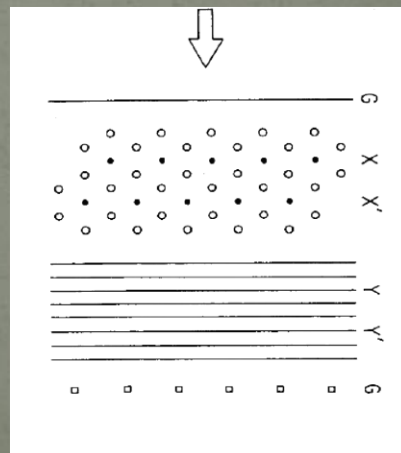
MWPC



E137



Drift chamber at early time



Problems

- Problems caused by slow movement of positive ions
 - 1 . Long tail of the signal
 - ⇒ Signal shaping is done with outside circuit
 - 2 . Electric shield effect which causes a rate effect
 - ⇒ TPC with grid is an answer to these problems of positive ions.
- Problem caused by large size molecules of positive ions
 - 3 . Aging : caused by adhering molecules to the cathode
 - ⇒ Thick wire or flat sheet for cathode (prevent local adherence)
 - ⇒ Mixing of quench gas: alcohol, ether, halogen-gas
- Limit of position resolution
 - 4 . Determined by diffusion during drift of electrons
 - $\gtrsim 100 \mu\text{m}$
 - inevitable effect because of gas filling

TPC

Fig. 3.18. Sketch of time projection chamber (TPC) for the PEP4 experiment [MA 78].

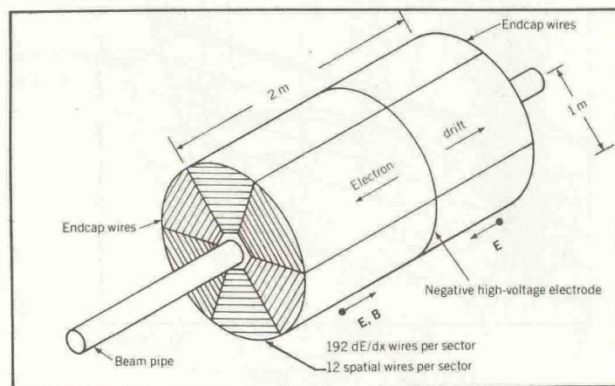
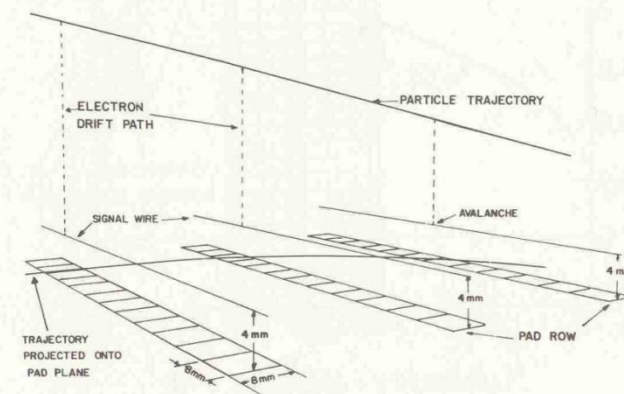


Fig. 3.19. Principle of track measurement by cathode pad readout in a TPC [FA 79].



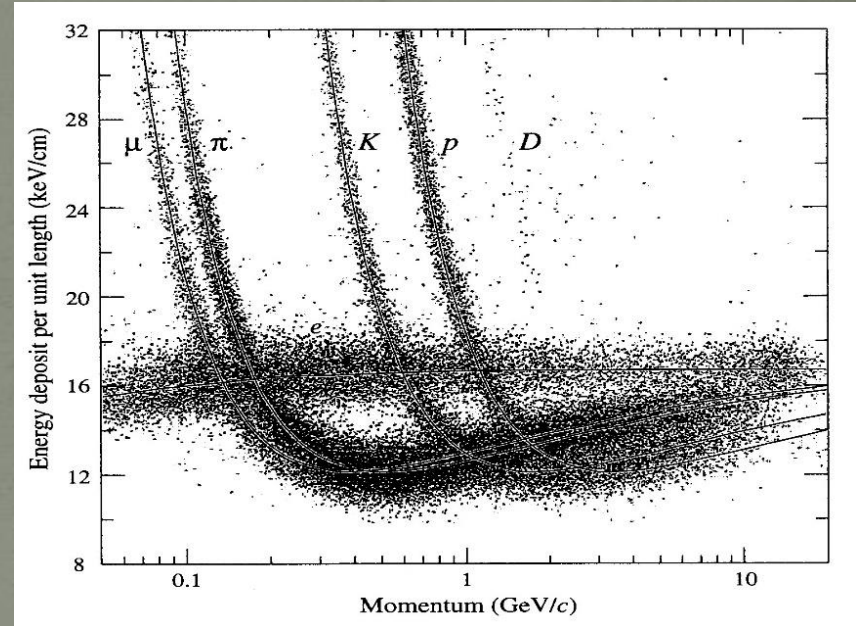
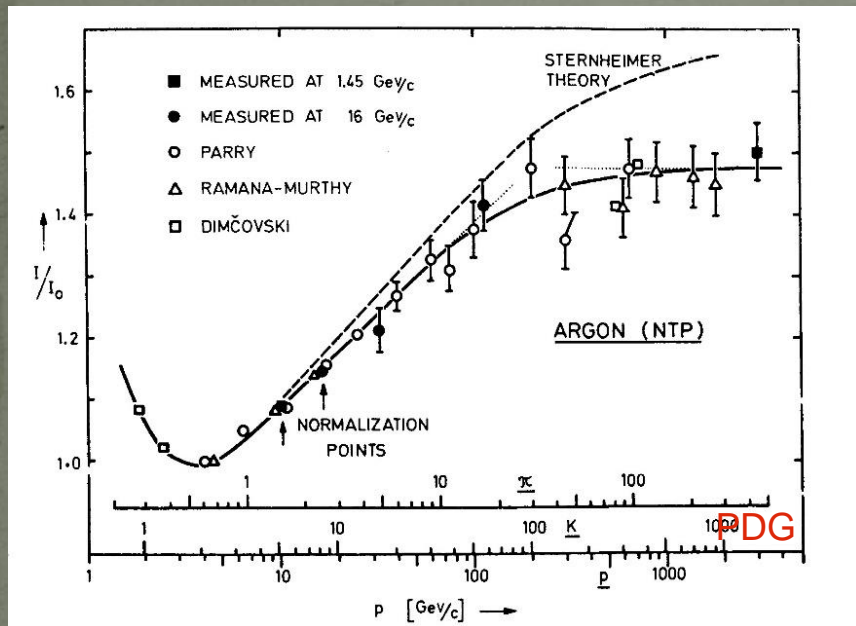
- Measure the track in three dimensions by using sense-wire position, drift-time and cathode pads. **3d-readout**
- Avoid a large positive-ion problem by narrowing the avalanche region near the sense wire. **Reduce positive ion problem**
- Minimize a diffusion by winding drift-electrons around a magnetic line of force. **Reduce the diffusion effect**

Ultimate gas chamber

KK

TPC (cont)

Particle identification

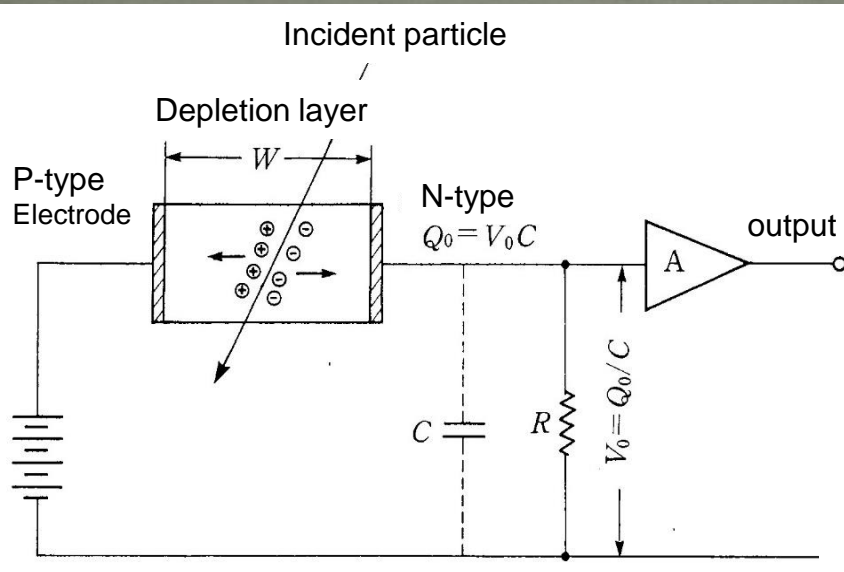


Semiconductor detector

Contents

- Properties of semiconductor
- p-n junction
- Reverse biasing
- Remarkable features

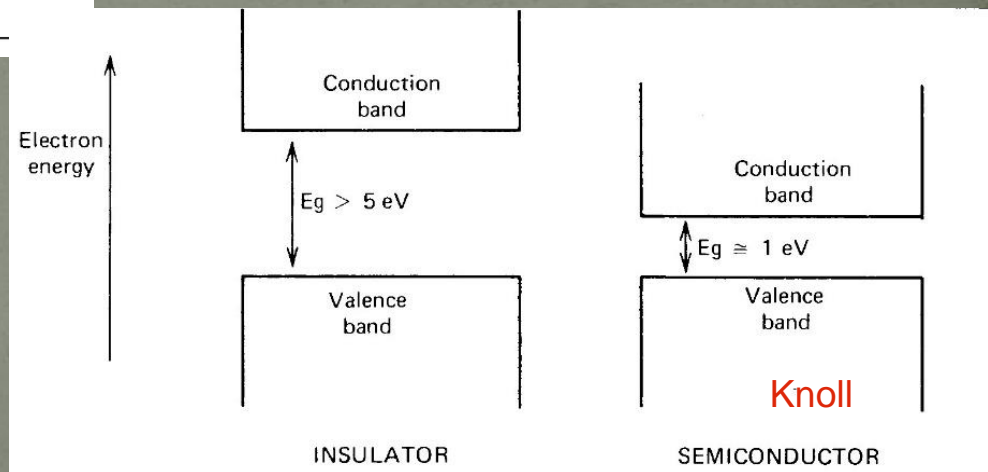
Properties of semiconductor



Same principle with a gas chamber (ionization chamber).

However, the carriers in solid state are electron and hole pairs in stead of free electron and positive ion pairs in gas.

Energy levels of solid state
narrow gap between valence and
conduction bands



How we can get high resistance ???

TABLE 11-1. Properties of Intrinsic Silicon and Germanium

	Si	Ge
Atomic number	14	32
Atomic weight	28.09	72.60
Stable isotope mass numbers	28-29-30	70-72-73-74-76
Density (300 K); g cm ⁻³	2.33	5.33
Atoms cm ⁻³	4.96 × 10 ²²	4.41 × 10 ²²
Dielectric constant	12	16
Forbidden energy gap (300 K); eV	1.115	0.665
Forbidden energy gap (0 K); eV	1.165	0.746
Intrinsic carrier density (300 K); cm ⁻³	1.5 × 10 ¹⁰	2.4 × 10 ¹³
Intrinsic resistivity (300 K); Ωcm	2.3 × 10 ⁵	47
Electron mobility (300 K); cm ² /V-s	1350	3900
Hole mobility (300 K); cm ² /V-s	480	1900
Electron mobility (77 K); cm ² /V-s	2.1 × 10 ⁴	3.6 × 10 ⁴
Hole mobility (77 K); cm ² /V-s	1.1 × 10 ⁴	4.2 × 10 ⁴
Energy per hole-electron pair (300 K); eV	3.62	2.96
Energy per hole-electron pair (77 K); eV	3.76	2.96
Fano factor (77 K)	0.143 (Ref. 7) 0.084 (Ref. 8) 0.085 } (Ref. 12) to 0.137 }	0.129 (Ref. 9) 0.08 (Ref. 10) < 0.11 (Ref. 11) 0.057 } (Ref. 12) 0.064 } 0.058 (Ref. 13)

From G. Bertolini and A. Coche, Eds., "Semiconductor Detectors," Elsevier-North Holland, Amsterdam (1968), except where noted.

Knoll

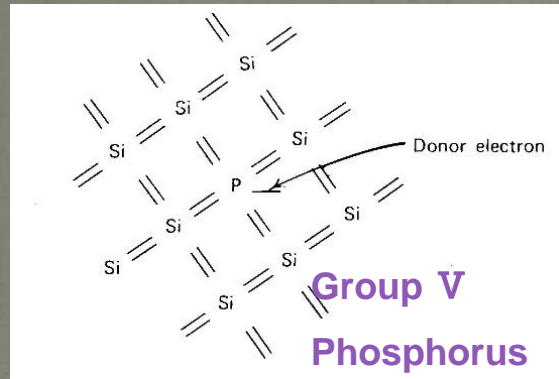
A pair can be produced by 3-4 eV energy. The density of solid state is higher than that of gas.

Seed will be much more than that of gas chamber, and amplification like gas amplification won't be necessary.

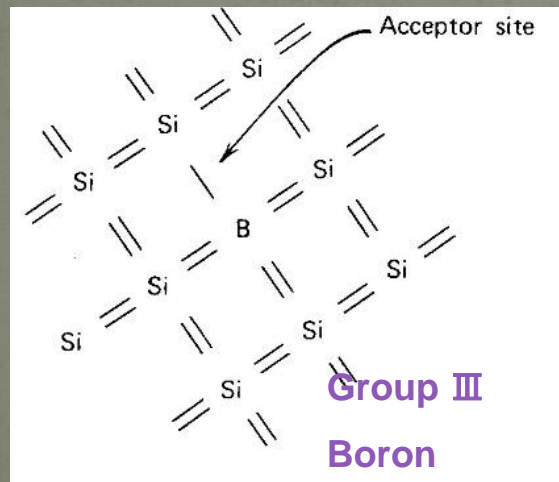
Small difference between velocities of electrons and hole unlike the gas case.

Still, high carrier density. How to realize no-carrier (higher resistance) world.

p - n junction

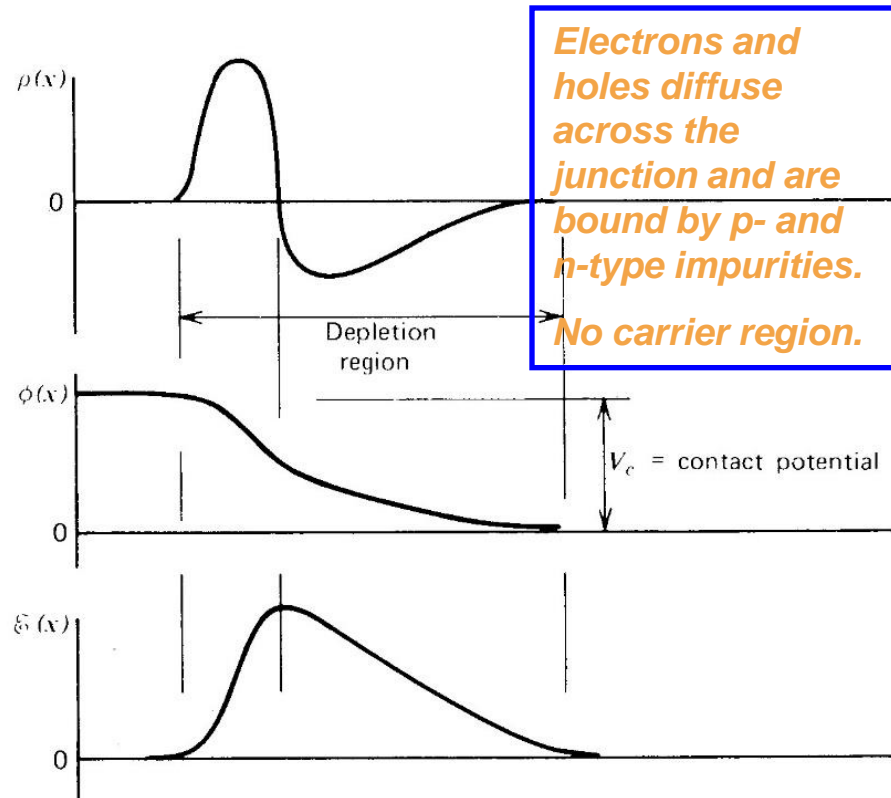
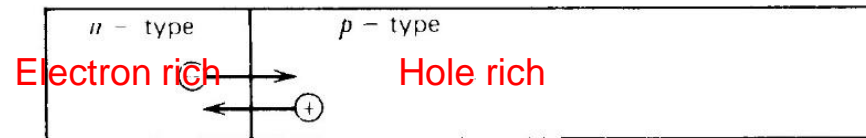


n-type silicon



p-type silicon

Knoll

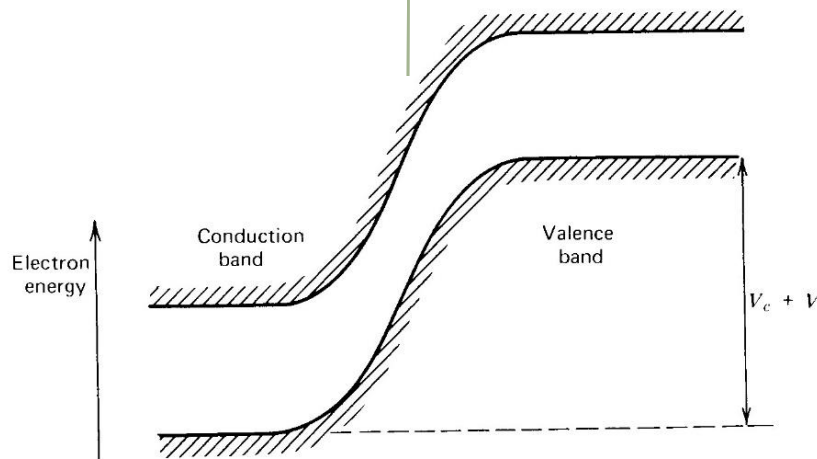
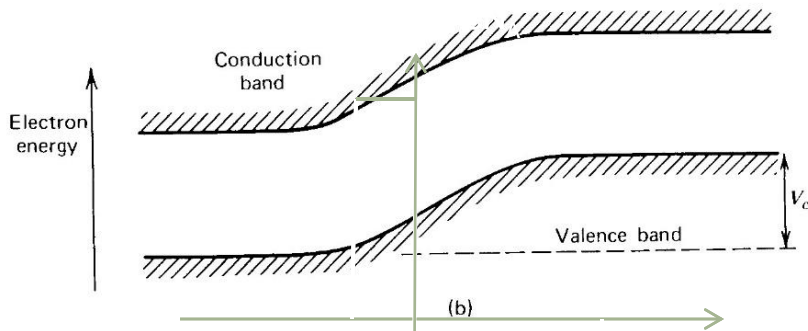
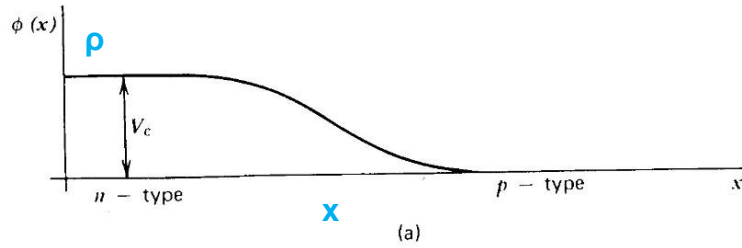


However,

$V_c \leq 1 \text{ V}$ and thin depletion layer due to a space charge effect

Thin depletion layer \rightarrow large capacitance (C) \rightarrow small signal due to q/C

Reverse Biasing

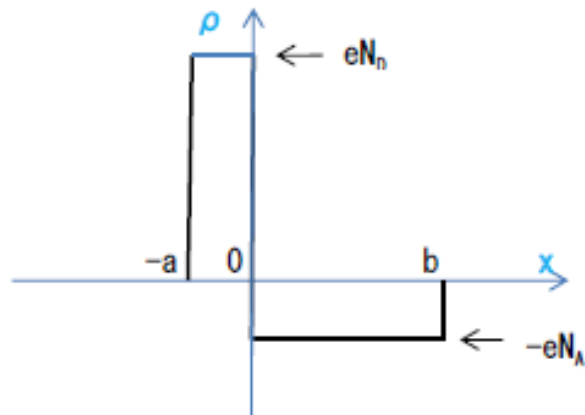


Reverse biasing: supply of external voltage, in the reverse direction, which is the direction to increase the contact potential, expands the depletion layer.

To prevent discharge,
 $E \leq 10^6 - 10^7 \text{ V/m}$

Simple model in one-dimension

Gauss's theorem: $\Delta \phi = -\rho / \epsilon$



$$\begin{aligned}d^2 \phi / dx^2 &= -eN_0 / \epsilon \quad (-a < x < 0) \\ &= eN_a / \epsilon \quad (0 < x < b)\end{aligned}$$

Boundary conditions

$$d\phi / dx \big|_{x=-a, b} = 0$$

$$\phi(-a) = V, \quad \phi(b) = 0$$

ϕ for either side must match at $x = 0$

$$N_0 a = N_a b$$

$$a + b \equiv d, \quad a \ll b \Rightarrow b \approx d, \quad NA \equiv N$$

$$\text{Thickness of depletion layer: } d = [(2\epsilon V) / (eN)]^{1/2}$$

$$\text{Capacitance: } C = \epsilon / d = [(e\epsilon N) / (2V)]^{1/2}$$

$$\text{Field strength: } E = V/d = [(eNV) / (2\epsilon)]^{1/2}$$

Remarkable features of semiconductor detector

- Extremely good resolution of energy for low energy particles

Number of seed: $n = E_d / W$, where E_d and W are energy deposit and energy produce +/- pair

E_d is larger than gas due to higher density of solid by one thousand.

W is 3.62 eV for Si. It is very small.

Number of seed

semiconductor: $n = 10^6$

gas : $n = 10^2$

plastic scintillator : 10^3

crystal scintillator: 10^2

Best recode: Ge \rightarrow 0.054% for 8MeV γ , 0.71% 122keV γ

For this purpose, the thicker depletion layer is the better. Si-Li etc.

- Extremely good resolution of position for high energy particles

Large number of seeds with high density: RO from multi places

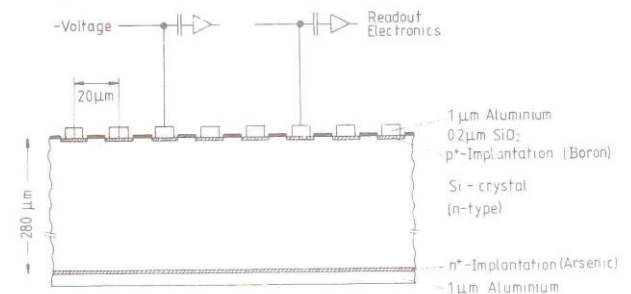
Small diffusion

Fine machining

Moreover, response is fast, due to thin layer of depletion and fast movement of hole.

Silicon Vertex detector is now a crucial detector for flavor tagging.

Fig. 3.34. Cross-section of silicon microstrip detector with capacitive charge division [HY 83].



Position is obtained from the measurement of induced current on the electrode (strip, pixel) . Highly-dense seed of electron-holes is crucial .

Table 35.1: Typical resolutions and deadtimes of common charged particle detectors. Revised November 2011.

Detector Type	Intrinsic Spatial Resolution (rms)	Time Resolution	Dead Time
Resistive plate chamber	$\lesssim 10$ mm	1 ns (50 ps ^a)	—
Streamer chamber	300 μm^b	2 μs	100 ms
Liquid argon drift [7]	$\sim 175\text{--}450$ μm	~ 200 ns	~ 2 μs
Scintillation tracker	~ 100 μm	100 ps/ n^c	10 ns
Bubble chamber	10–150 μm	1 ms	50 ms ^d
Proportional chamber	50–100 μm^e	2 ns	20-200 ns
Drift chamber	50–100 μm	2 ns ^f	20-100 ns
Micro-pattern gas detectors	30–40 μm	< 10 ns	10-100 ns
Silicon strip	pitch/(3 to 7) ^g	few ns ^h	$\lesssim 50$ ns ^h
Silicon pixel	$\lesssim 10$ μm	few ns ^h	$\lesssim 50$ ns ^h
Emulsion	1 μm	—	—

B meson tagging $\tau(B^+) \sim 1.6 \times 10^{-12}$ sec, $\tau(B^0) \sim 1.5 \times 10^{-12}$ sec
 $c\tau \sim 450$ μm

Belle II Detector

KL and muon detector:
Resistive Plate Counter (barrel)
Scintillator + WLSF + MPPC (end-caps)

EM Calorimeter:
CsI(Tl), waveform sampling (barrel)
Pure CsI + waveform sampling (end-caps)

electron (7GeV)

Particle Identification
Time-of-Propagation counter (barrel)
Prox. focusing Aerogel RICH (fwd)

Beryllium beam pipe
2cm diameter

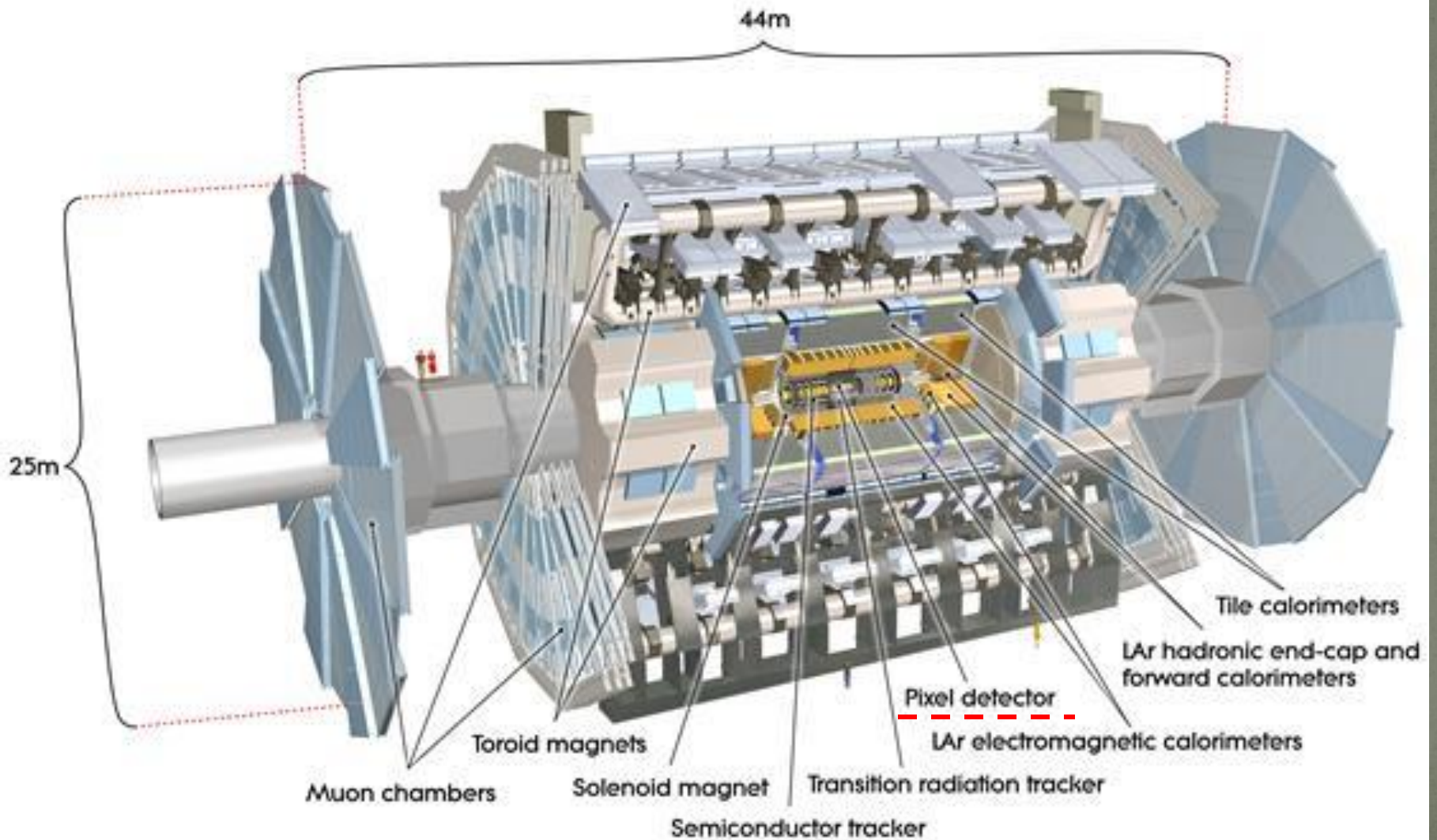
Vertex Detector
2 layers DEPFET + 4 layers DSSD

positron (4GeV)

Central Drift Chamber
He(50%):C₂H₆(50%), Small cells, long
lever arm, fast electronics



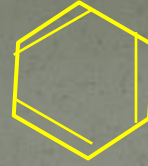
LHC-Atlas



dE/dx measurement

Detector using light

Plastic scintillator



Energy levels of an organic molecule with π -electron structure (phenyl)

S_0 - S_1 : 3 – 4 eV

S_0 - S_0 : 0.15 eV > 0.025 eV

Most of electrons stays at S_0 (ground state)

S_{ij} : vibrational states, transitions inside $\{S_0\}$ and $\{S_1\}$, $S_{ij} \rightarrow S_{i0}$, are radiationless, and their decay times are:

$\tau\{S_{10}\}$: nsec, $\tau\{T_1\}$: msec

Another route to the ground state

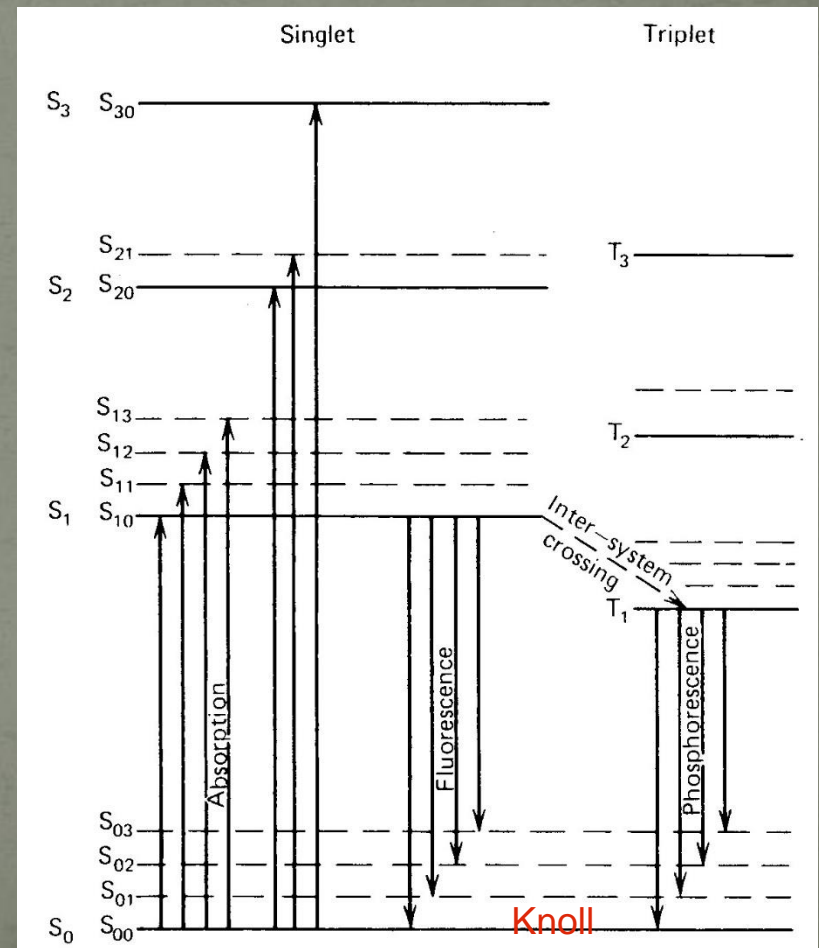
$T_1 + T_1 \rightarrow S_1 + S_0$

This is useful for PID, n/ γ separation.

PVT; poly-vinyl-toluene

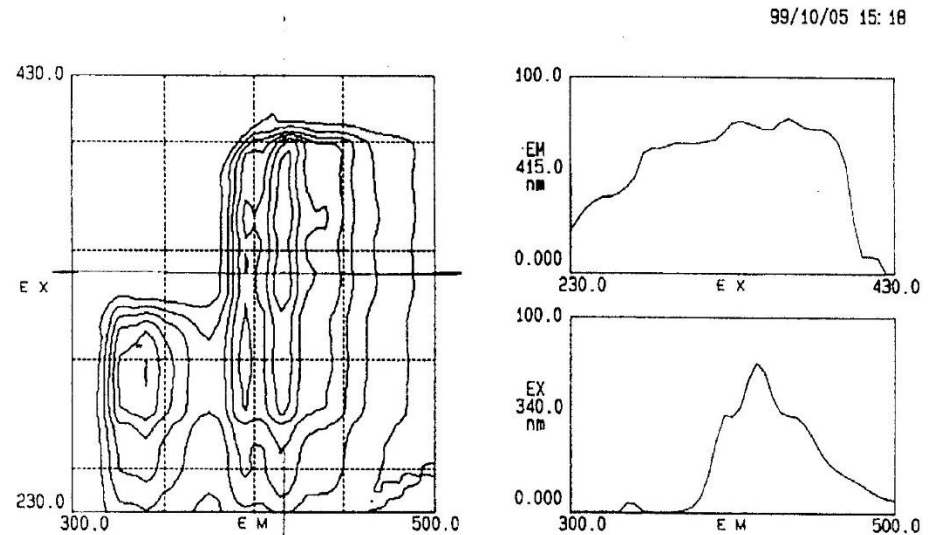
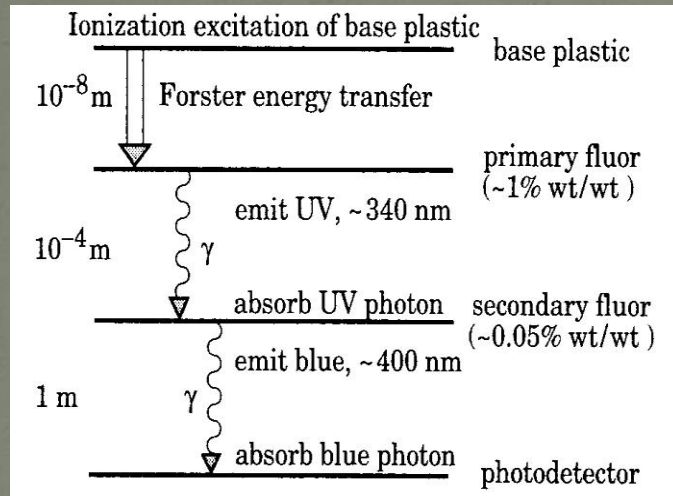
PS; poly-styrene

Liquid scintillators; xylene, etc



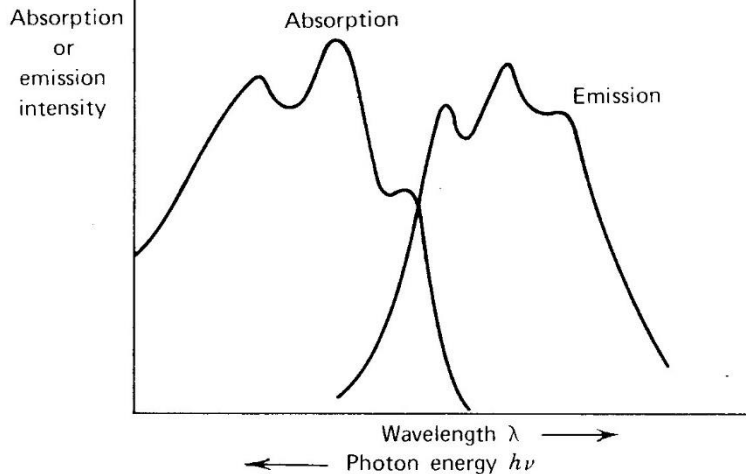
Wave length shift to visible light for better transmission

PDG



サンプル名 : EXT-MS-3
 コメント : TUTUNAKA: pTp 1.5%, POPOP 0.045%
 プログラム : 蛍光 スキャンスピード : 12000 nm/min
 励起開始波長 : 230.0 nm 励起終了波長 : 430.0 nm サンプリグ間隔 : 5.0 nm
 発光開始波長 : 300.0 nm 発光終了波長 : 500.0 nm サンプリグ間隔 : 5.0 nm
 等高線間隔 : 10.00 スリット (EX/EM) : 2.5 nm / 2.5 nm
 ネットワーク電圧 : 400 V レスポンス : 自動 シャッター制御 : スペクトル補正

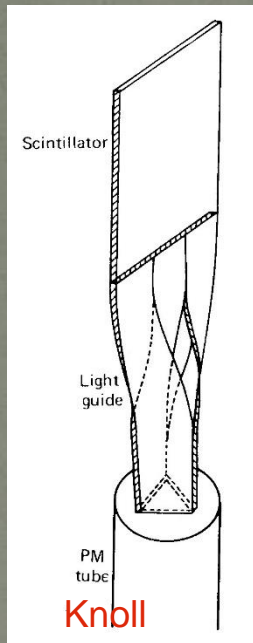
E391a



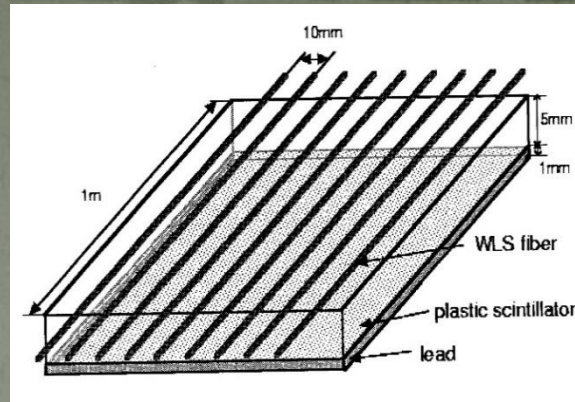
Knoll

Fig. 2.4: 押し出し成形法で製造したMS樹脂シンチレーター (PTP 1.5% + POPOP 0.045) の励起発光スペクトル。Fluorescence Spectrometer HITACHI F-4500を用いて測定した。左図は2次元の励起発光スペクトルで、横軸は発光波長、縦軸は吸光(励起)波長である。右上図は発光波長410nmに対する励起波長スペクトル、右下図は励起波長340nmに対する発光波長スペクトルである。

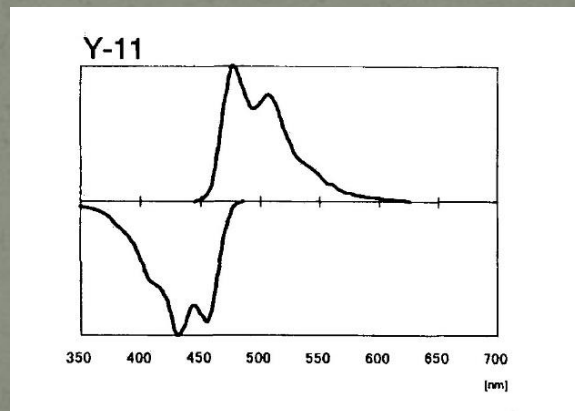
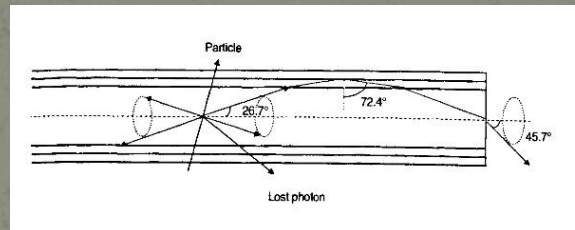
Readout method



Through light guide
(direct RO)



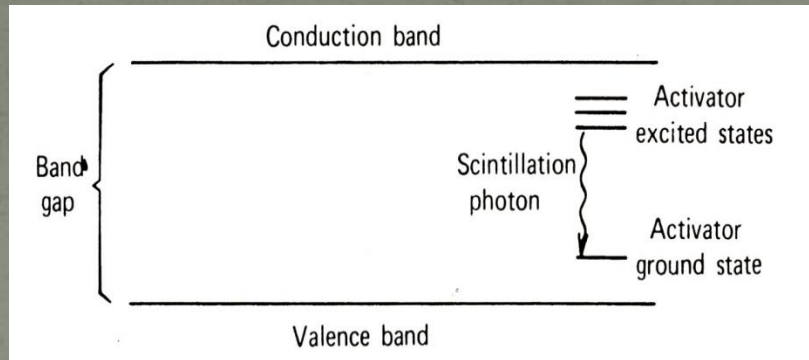
Clad structure



Through WLS-fibers

Attenuation is smaller than that of the direct RO at a long distance. We can reduce the area of photo cathode.

Inorganic (Crystal) scintillators



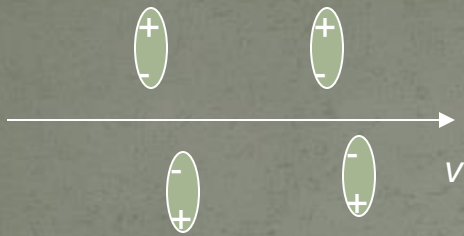
Knoll

Table 28.2: Properties of several inorganic crystal scintillators. Most of the notation is defined in Sec. 6 of this *Review*.

Parameter:	ρ	MP	X_0	R_M	dE/dx	λ_I	τ_{decay}	λ_{max}	n^*	Relative output [†]	Hygroscopic?	$d(LY)/dT$
Units:	g/cm^3	$^{\circ}\text{C}$	cm	cm	MeV/cm	cm	ns	nm				$\%/^{\circ}\text{C}^{\ddagger}$
NaI(Tl)	3.67	651	2.59	4.8	4.8	41.4	230	410	1.85	100	yes	~ 0
BGO	7.13	1050	1.12	2.3	9.0	21.8	300	480	2.15	9	no	-1.6
BaF ₂	4.89	1280	2.06	3.4	6.6	29.9	630 ^s 0.9 ^f	300 ^s 220 ^f	1.50	21 ^s 2.7 ^f	no	-2 ^s $\sim 0^f$
CsI(Tl)	4.51	621	1.85	3.5	5.6	37.0	1300	560	1.79	45	slight	0.3
CsI(pure)	4.51	621	1.85	3.5	5.6	37.0	35 ^s 6 ^f	420 ^s 310 ^f	1.95	5.6 ^s 2.3 ^f	slight	-0.6
PbWO ₄	8.3	1123	0.9	2.0	10.2	18	50 ^s	560 ^s 10 ^f 420 ^f	2.20	0.1 ^s	no	-1.9
LSO(Ce)	7.40	2070	1.14	2.3	9.6	21	40	420	1.82	75	no	-0.3
GSO(Ce)	6.71	1950	1.37	2.4	8.9	22	600 ^s 56 ^f	430	1.85	3 ^s 30 ^f	no	-0.1

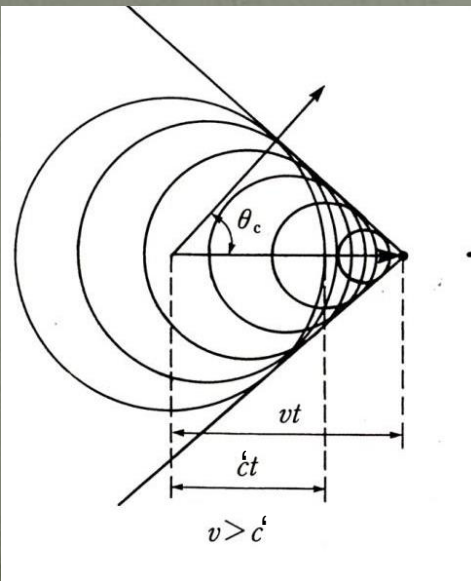
PDG

Other source of light : Cherenkov light



A particle cause polarization and the polarization returns to the state before. Very tiny, but coherence enhance the emission of light.

material	Refractive index (n)	Critical energy (E_c , MeV)			Emission angle θ_0 (degree, for $\beta=1$)
		proton	μ -on	electron	
Air	1.000284	38.5×10^3	4.3×10^3	61	1.4
water	1.34	450	50	0.25	42
Lucite	1.50	310	35	0.17	48
Lead glass	1.68	220	26	0.13	54



$$c' = c / n$$

$$\cos \theta_c = v / c' = 1 / n\beta$$

Critical energy:
 $n\beta > 1$, $\beta_c = 1/n$
 $E_c = (\gamma_c - 1)m$

Emission angle
 $\cos \theta_c > 1/n$
 $\theta_c < \theta_0$
 $= \cos^{-1}(1/n)$

Light yield : $d^2N/dxd\lambda = 2\pi\alpha z^2 \sin^2\theta / \lambda^2$

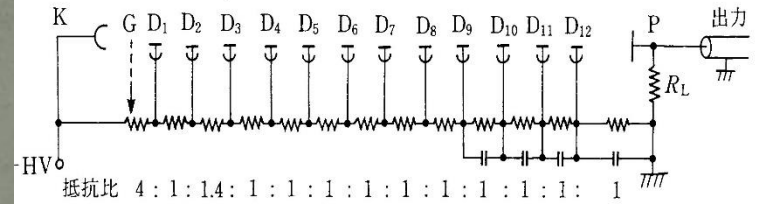
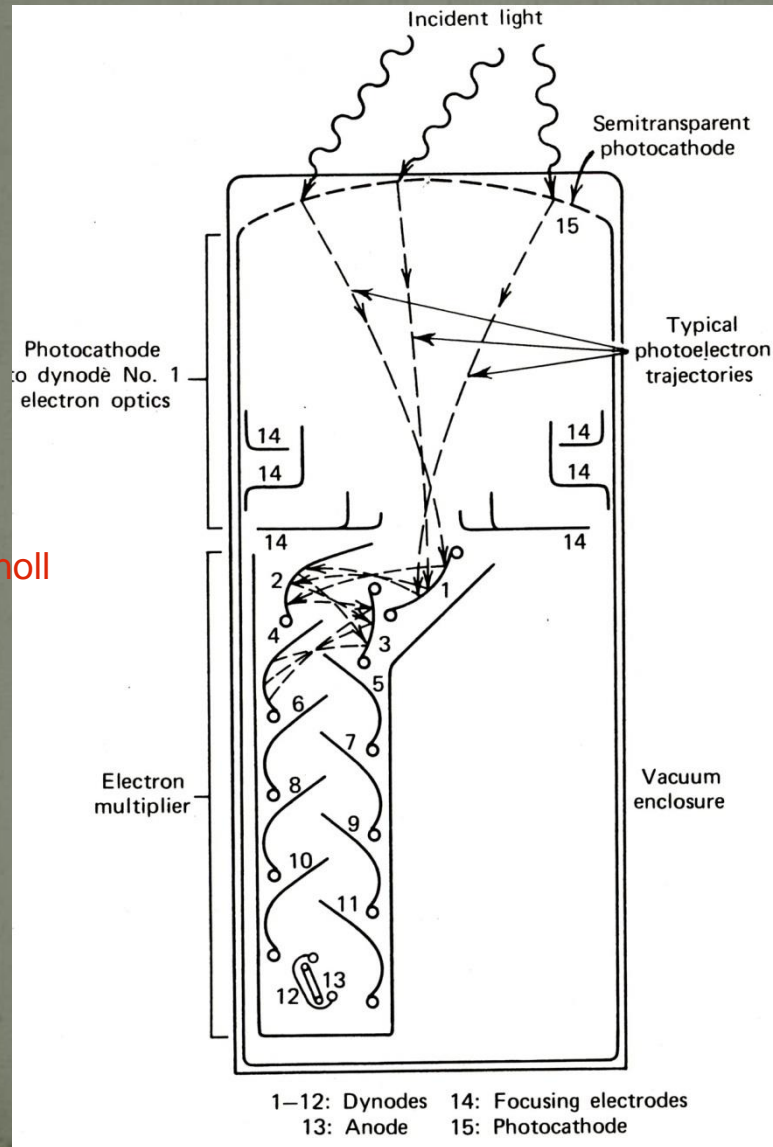
When electrons and protons of 2 GeV/c run through water, the emission angles are 41.25° , 33.84° , respectively. We can measure the particle direction

$dN/dx = 99.6, 71.0 \text{ cm}^{-1}$; $\lambda = 400\text{-}500 \text{ nm}$

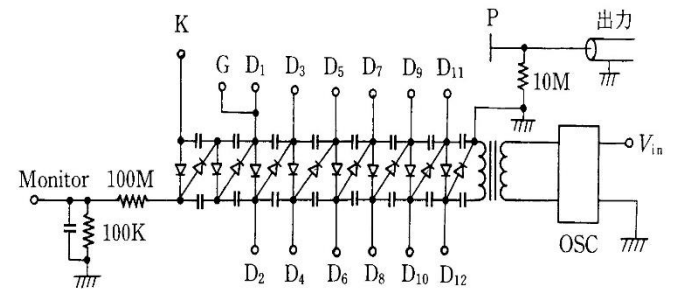
Transition radiation

$N \propto \gamma$

Photo-sensor Photo-Multiplier-Tube (PMT)



抵抗回路

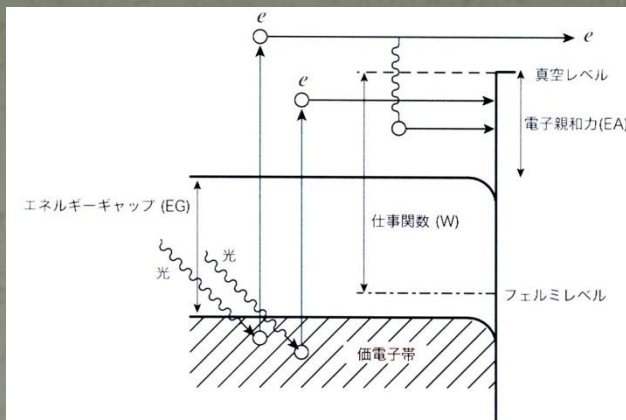


Cockcroft-Walton 回路

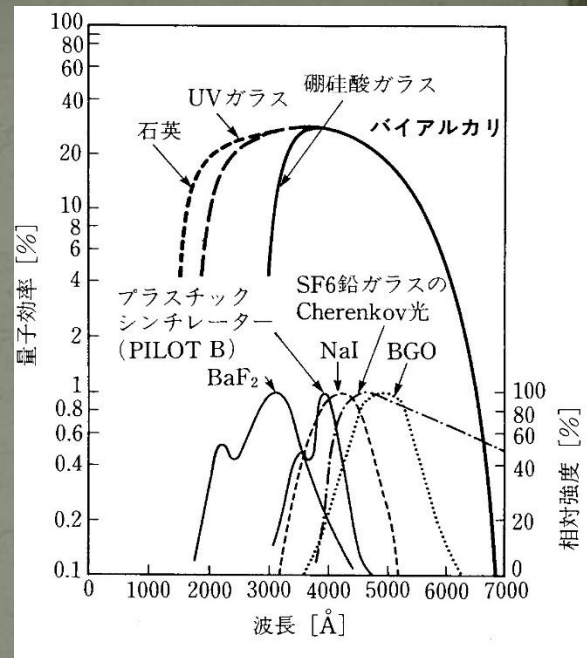
Hamamatsu R329 高圧回路

3-27 図 光電子増倍管の高電圧回路

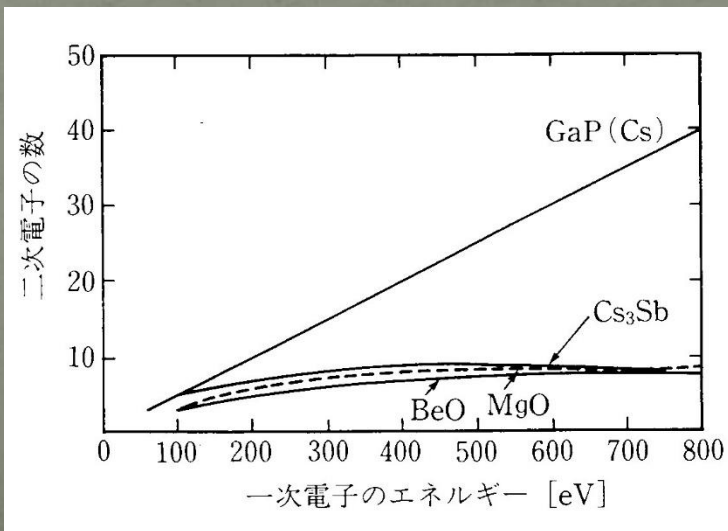
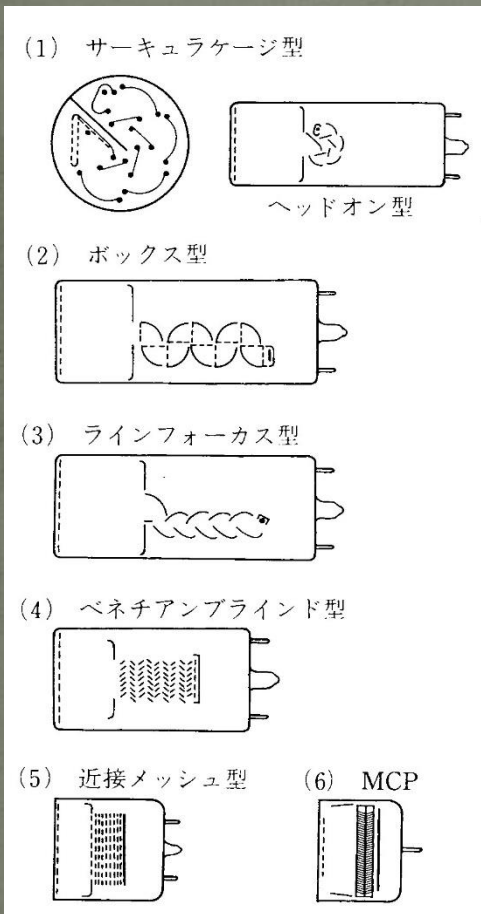
Cathode



Na / K / Rb / Cs + Sb



Dinode



Various photodetectors

Table 35.2: Representative characteristics of some photodetectors commonly used in particle physics. The time resolution of the devices listed here vary in the 10–2000 ps range.

Type	λ (nm)	$\epsilon_Q \epsilon_C$	Gain	Risetime (ns)	Area (mm ²)	1-p.e noise (Hz)	HV (V)	Price (USD)
PMT*	115–1700	0.15–0.25	10^3 – 10^7	0.7–10	10^2 – 10^5	10 – 10^4	500–3000	100–5000
MCP*	100–650	0.01–0.10	10^3 – 10^7	0.15–0.3	10^2 – 10^4	0.1–200	500–3500	10–6000
HPD*	115–850	0.1–0.3	10^3 – 10^4	7	10^2 – 10^5	10 – 10^3	$\sim 2 \times 10^4$	~ 600
GPM*	115–500	0.15–0.3	10^3 – 10^6	$O(0.1)$	$O(10)$	10 – 10^3	300–2000	$O(10)$
APD	300–1700	~ 0.7	10 – 10^8	$O(1)$	10 – 10^3	1 – 10^3	400–1400	$O(100)$
PPD	320–900	0.15–0.3	10^5 – 10^6	~ 1	1–10	$O(10^6)$	30–60	$O(100)$
VLPC	500–600	~ 0.9	$\sim 5 \times 10^4$	~ 10	1	$O(10^4)$	~ 7	~ 1

PMT: Photomultiplier tube, MCP: Microchannel plate, HPD: Hybrid photon detector
 GPM: Gaseous photon detector, APD: Avalanche photo diode,
 PPD: Pixelized photon detector, VLPC: Visible light photon counter

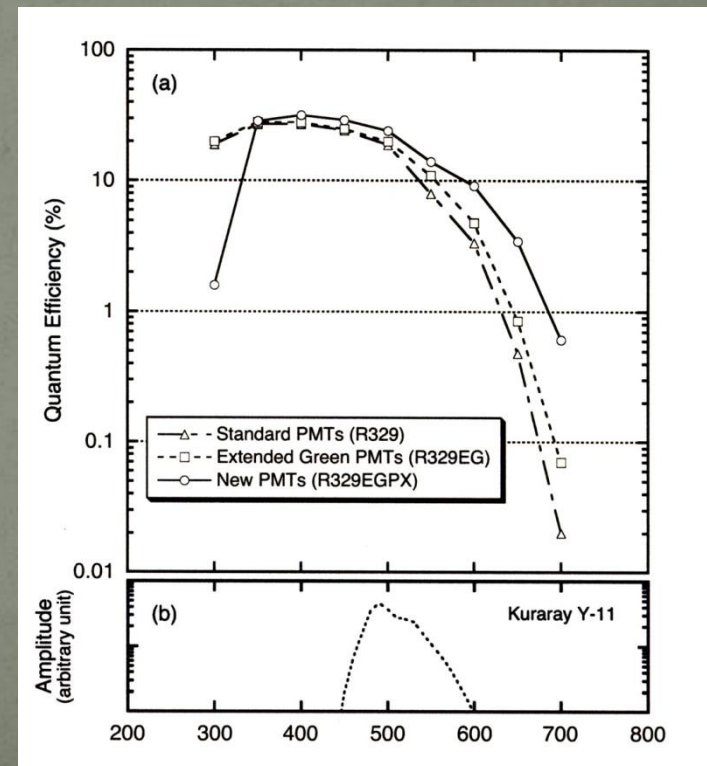
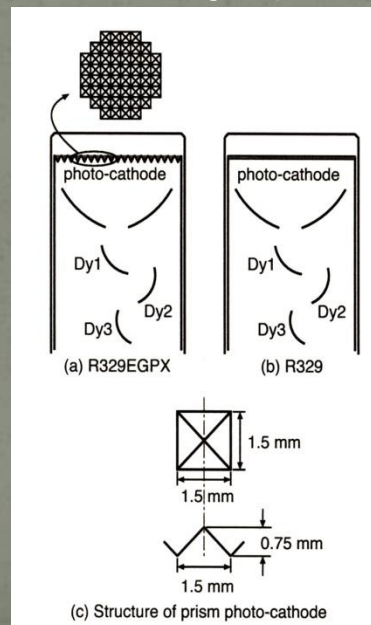
R&D in the E391a experiment

- **Scintillator : Extruded MS-resin**

Among three methods to make plastic sheet, cast, injection-mold, and extrusion, extrusion is the only method which has no limit in length, possible to use MS, which is mechanically strong, cheap for mass-production.

- **PMT : EGP**

Optimized for green light (WLSF)
improved quantum efficiency at 500 nm.



Electromagnetic calorimeters

for an energy measurement of photons and electrons

Table 28.5: Resolution of typical electromagnetic calorimeters.
 E is in GeV.

Technology (Experiment)	Depth	Energy resolution	Date
NaI(Tl) (Crystal Ball)	$20X_0$	$2.7\%/E^{1/4}$	1983
$\text{Bi}_4\text{Ge}_3\text{O}_{12}$ (BGO) (L3)	$22X_0$	$2\%/\sqrt{E} \oplus 0.7\%$	1993
CsI (KTeV)	$27X_0$	$2\%/\sqrt{E} \oplus 0.45\%$	1996
CsI(Tl) (BaBar)	$16\text{--}18X_0$	$2.3\%/E^{1/4} \oplus 1.4\%$	1999
CsI(Tl) (BELLE)	$16X_0$	1.7% for $E_\gamma > 3.5$ GeV	1998
PbWO_4 (PWO) (CMS)	$25X_0$	$3\%/\sqrt{E} \oplus 0.5\% \oplus 0.2/E$	1997
Lead glass (OPAL)	$20.5X_0$	$5\%/\sqrt{E}$	1990
Liquid Kr (NA48)	$27X_0$	$3.2\%/\sqrt{E} \oplus 0.42\% \oplus 0.09/E$	1998
Scintillator/depleted U (ZEUS)	$20\text{--}30X_0$	$18\%/\sqrt{E}$	1988
Scintillator/Pb (CDF)	$18X_0$	$13.5\%/\sqrt{E}$	1988
Scintillator fiber/Pb spaghetti (KLOE)	$15X_0$	$5.7\%/\sqrt{E} \oplus 0.6\%$	1995
Liquid Ar/Pb (NA31)	$27X_0$	$7.5\%/\sqrt{E} \oplus 0.5\% \oplus 0.1/E$	1988
Liquid Ar/Pb (SLD)	$21X_0$	$8\%/\sqrt{E}$	1993
Liquid Ar/Pb (H1)	$20\text{--}30X_0$	$12\%/\sqrt{E} \oplus 1\%$	1998
Liquid Ar/depl. U (DØ)	$20.5X_0$	$16\%/\sqrt{E} \oplus 0.3\% \oplus 0.3/E$	1993
Liquid Ar/Pb accordion (ATLAS)	$25X_0$	$10\%/\sqrt{E} \oplus 0.4\% \oplus 0.3/E$	1996

Similar features for
hadron calorimeter

Decomposition of energy resolution

$\Delta E/E = C_1/\sqrt{E} + C_2 + C_3/E$; just an empirical formula, but convenient

S: signal from the calorimeter

Total absorption type detector $\equiv S \propto E$; $E = a \cdot S$; proportionality

C_1 term: main term of resolution.

A particle loses its energy through an ionization process along charged tracks, and the ionization energy will be converted to an electronic signal. In the case of PMT readout, the smallest number, which makes the largest statistical fluctuation through this processing, is number of photo-electron, N_{pe} , before the large electron multiplication in PMT tube. E is proportional to N_{pe} and the error ΔE fluctuates as $\sqrt{N_{pe}}$, then $\Delta E/E \propto 1/\sqrt{N_{pe}} \propto 1/\sqrt{E}$. It is similar with other readout. In the case of sampling calorimeter, consisting of active and non-active layers, the fluctuation of the sampling is also proportional to \sqrt{E} .

C_2 term: $\Delta E \propto E$; Just as an ambiguity of calibration of the coefficient of a linear function.

C_3 term ; ΔE is energy-independent like a fluctuation given by electronic noise at the measurement.

For the ideal condition, noiseless operation and perfect calibration, the resolution is uniquely determined by C_1 term.

5. Examples and discussions

- 5.1 Spectrometer

Momentum measurement by a magnetic spectrometer is better for low energy particles, while at high energy a calorimeter can measure the particle energy with a better resolution than at low energy.

Momentum measurement

Combination of a magnetic field and the track measurement

Particle motion in the magnetic field

Lorentz force $dp/dt = q(\mathbf{v} \times \mathbf{B})$; MKSA (Coulomb, Volt, Tesla)

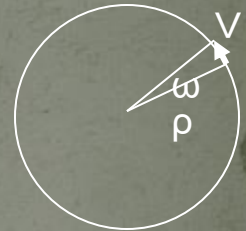
; just change the direction no gain of energy

For $\mathbf{B} \perp \mathbf{v}$ $p d\theta/dt = q v B$

$$\rho \omega = v$$

$$f = 2\pi / \omega ;$$

Cyclotron frequency



Non-relativistic

$$p = mv$$

$$d\theta/dt \equiv \omega = qB/m$$

(Energy independent)

$$\rho = v / \omega = mv / qB = p / qB$$

equation !!

Relativistic

$$p = mv\gamma$$

$$\omega = qB / m\gamma$$

(Energy dependent)

$$\rho = v / \omega = mv\gamma / qB = p / qB$$

; Same

$$p = 0.3BL\rho, \quad \text{for } q=e, \text{ where } [p] = \text{GeV}/c, [B] = \text{Tesla and } [\rho] = \text{m}$$

$$\text{Magnet depth: } L \quad \rho \sin\theta = L$$

$$p = 0.3BL / \sin\theta$$

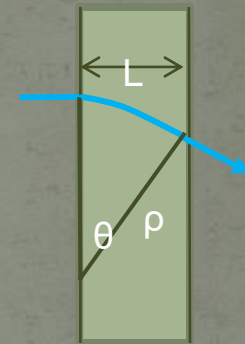
$$dp/p = (p / 0.3BL) d\theta :$$

$$= 3 \times 10^{-3} p \quad ; \text{for } BL=1 \text{ Tm, } d\theta=1 \text{ mradian}$$

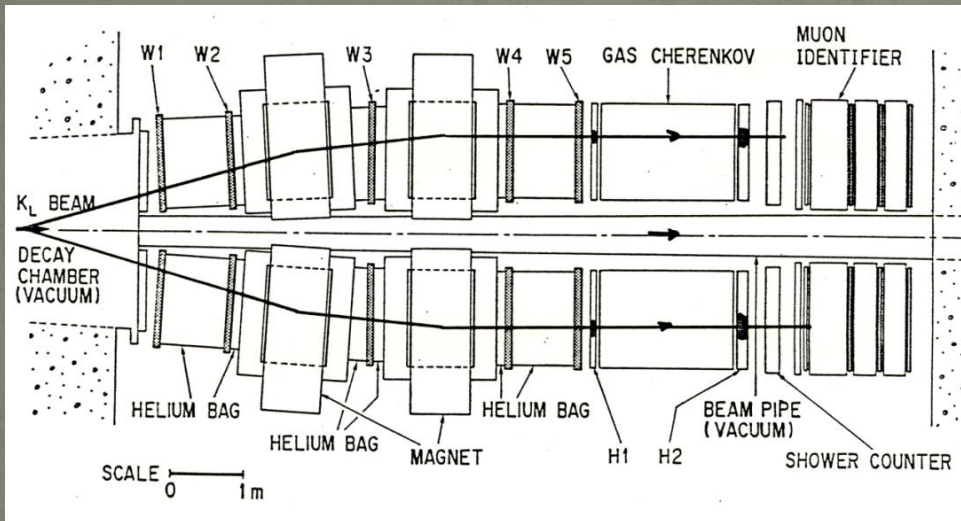
Resolution is proportional to momentum; worse at the higher energy!!

Clear contrast with calorimeter: resolution shows

$1/\sqrt{E}$ dependence



Magnetic spectrometer of E137



$$p = 0.3BL / \sin\theta$$

$$P\sin\theta = P_T = 0.3BL ; \text{ magnet gives } P_T \text{ kick}$$

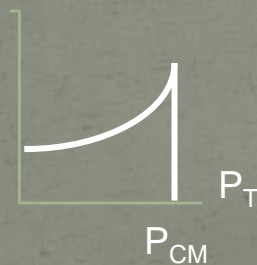
By setting magnetic field around 220 MeV/c kick, we can remove most of three-body decays and select four two-body decays with almost equal efficiency by the parallel trigger at downstream. The four modes were collected simultaneously.

This is true for KL decay at beam axis of any energy.

Two body decay
in KL rest frame



In laboratory frame



$$P_{CM} \text{ (KL} \rightarrow \pi\pi, \mu\mu, \mu e, ee)$$

$$= 206, 225, 238, 249 \text{ MeV/c}$$

Such a simple trigger is possible due to low energy of larger opening angle.

We also achieved similar mass resolution with the BNL competitor with less DC position resolution of 300 μm . They have to operate DC at 150 μm .

We can operate DC at low voltage. It brought us a big margin in high-rate environment.

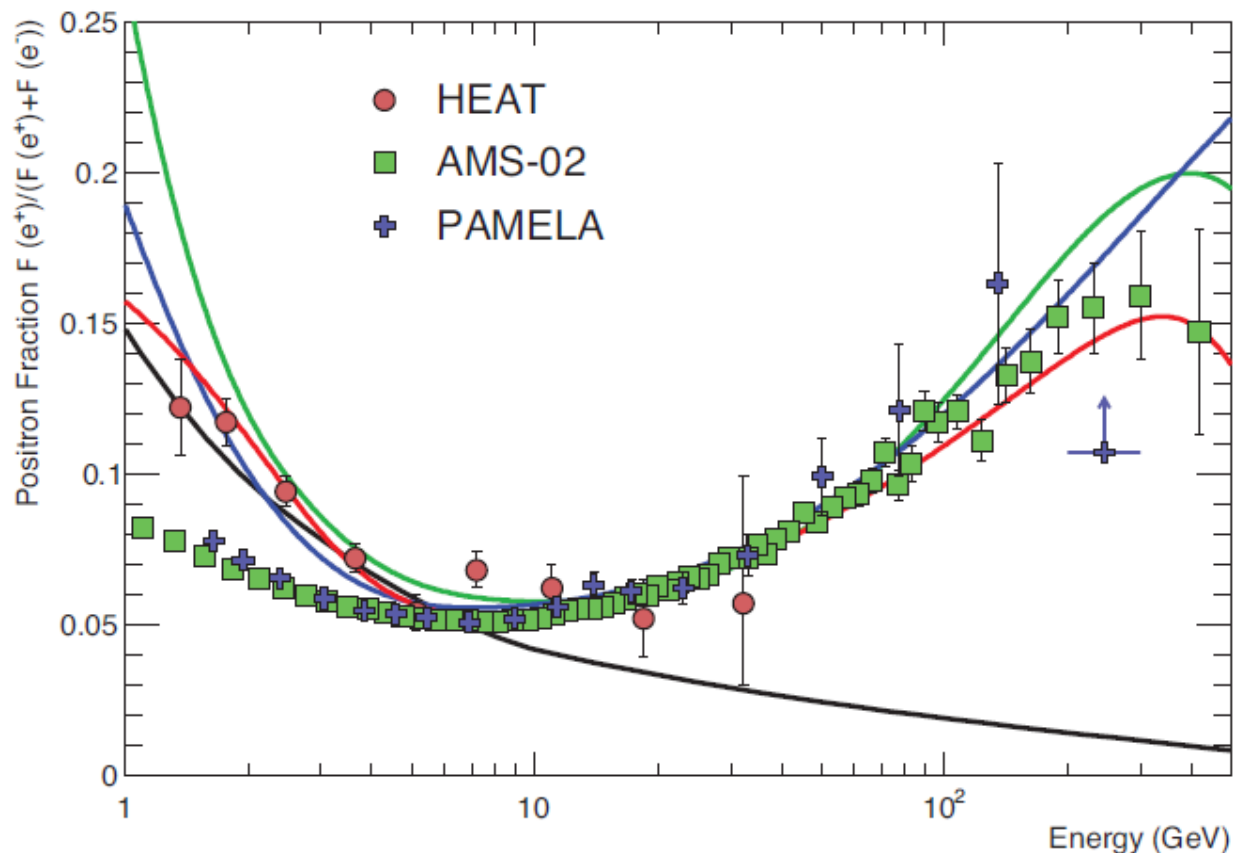


Figure 30.3: The positron fraction (ratio of the flux of e^+ to the total flux of e^+ and e^-) [26,24,30]. The heavy black line is a model of pure secondary production [28] and the three thin lines show three representative attempts to model the positron excess with different phenomena: green: dark matter decay [29]; blue: propagation physics [32]; red: production in pulsars [40]. The ratio below 10 GeV is dependent on the polarity of the solar magnetic field.

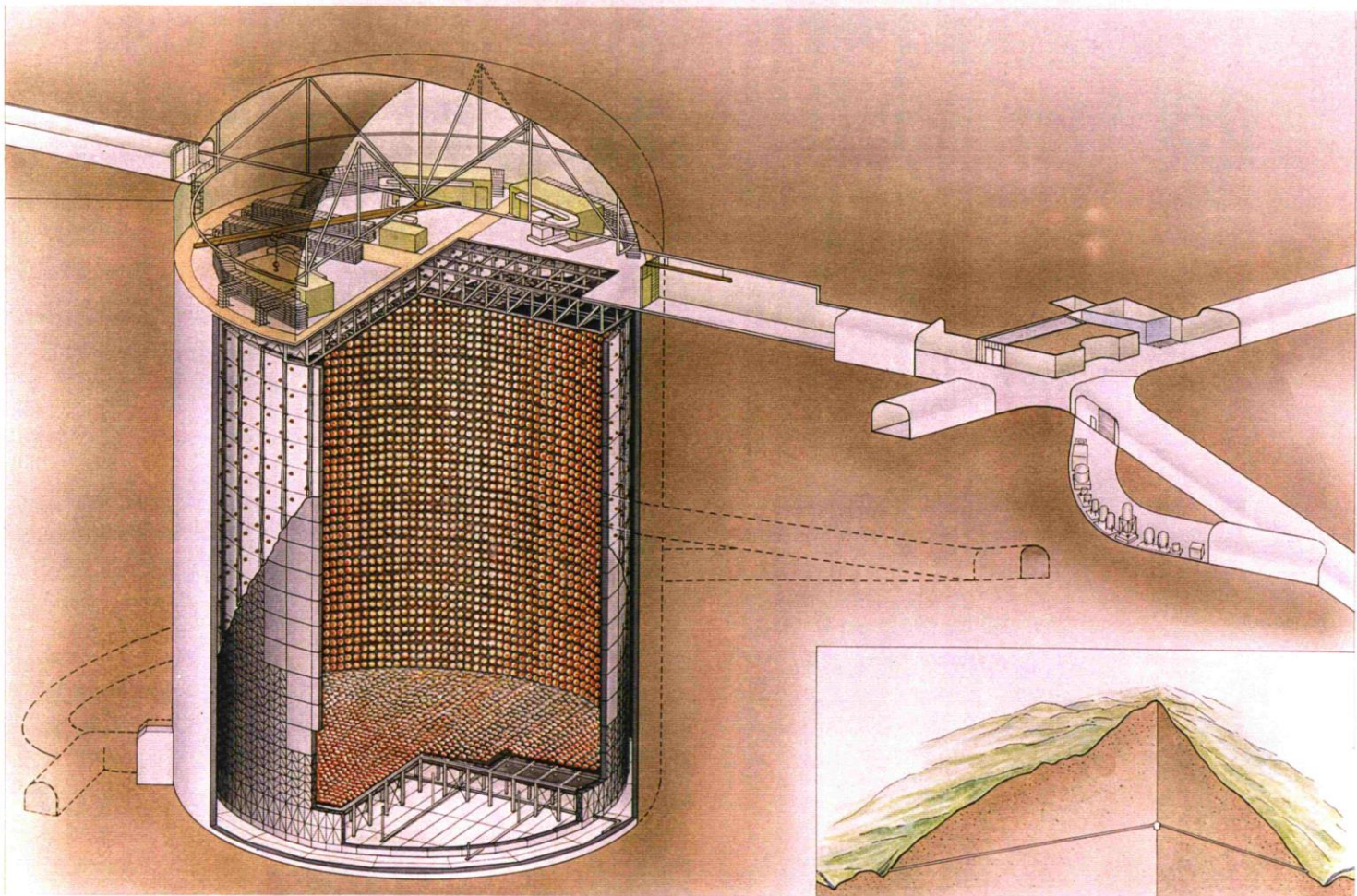
AMS could not deliver a super
conducting magnet to the ISS



Examples and discussions

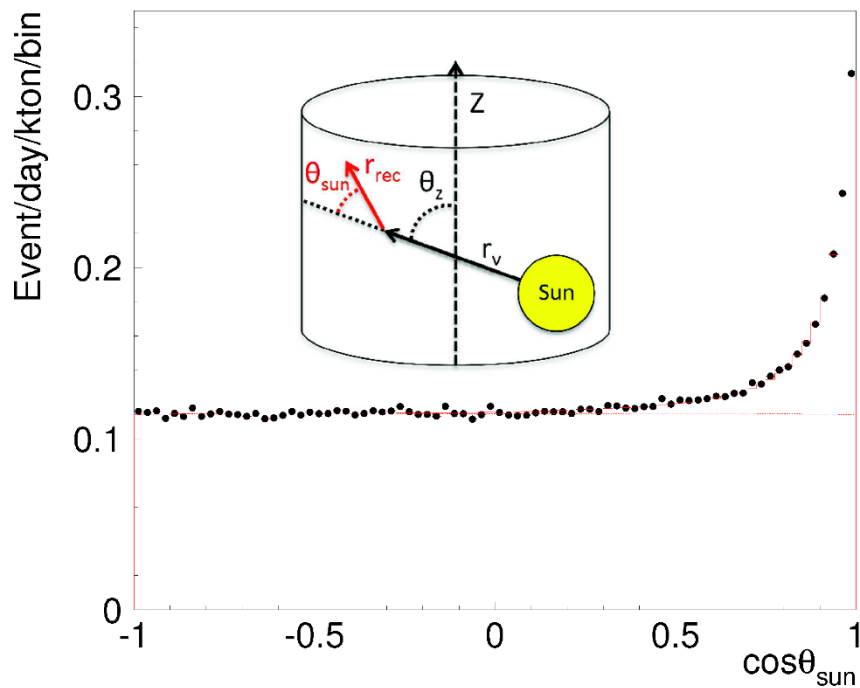
ν detectors

Super Kamiokande

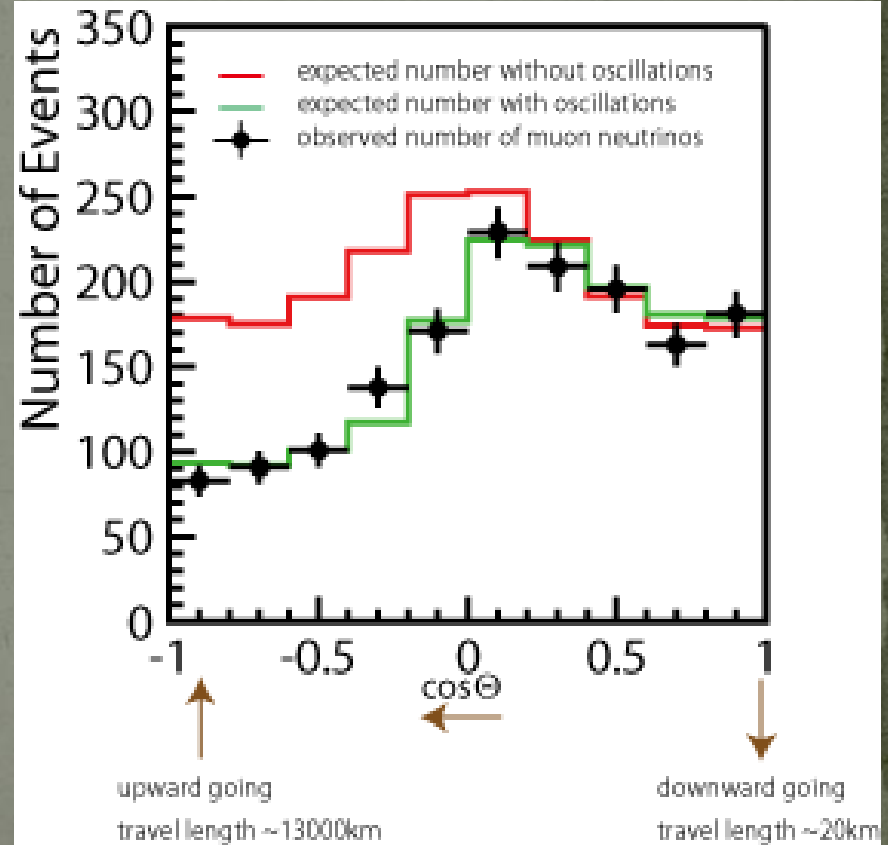


SK use electron scattering and see the Cerenkov light, and measure ν direction

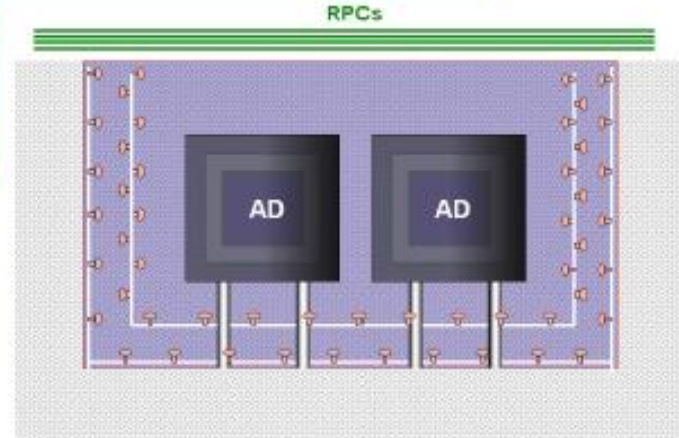
Solar ν



Atmospheric ν



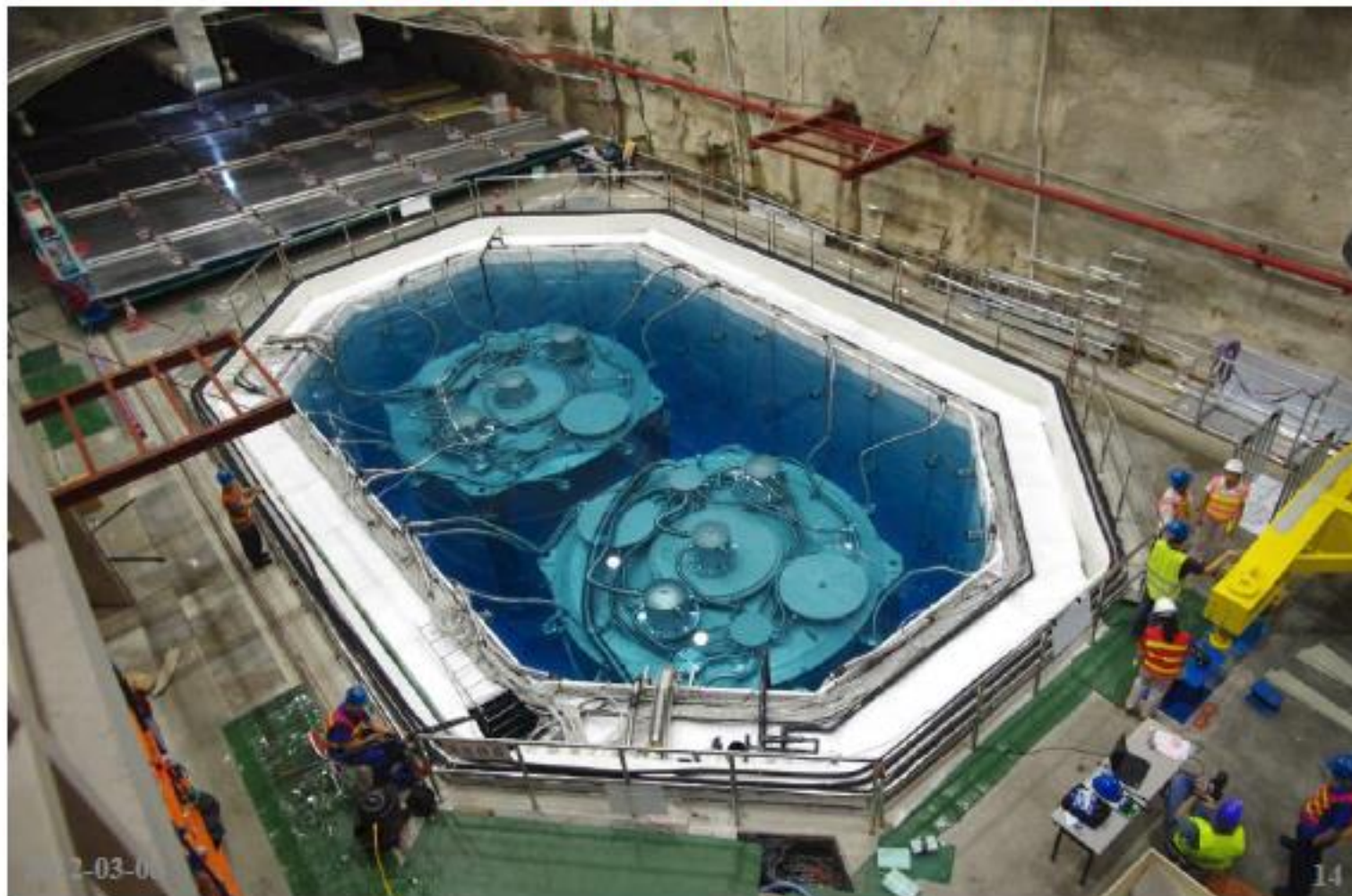
Daya Bay Experiment: Layout



- ◆ Relative measurement to cancel **Corr. Syst. Err.**
 - ⇒ 2 near sites, 1 far site
- ◆ Multiple AD modules at each site to reduce **Uncorr. Syst. Err.**
 - ⇒ Far: 4 modules, near: 2 modules
- ◆ Multiple muon detectors to reduce **veto eff. uncertainties**
 - ⇒ Water Cherenkov: 2 layers
 - ⇒ RPC: 4 layers at the top + telescopes



Two ADs Installed in Hall 1



Final comments

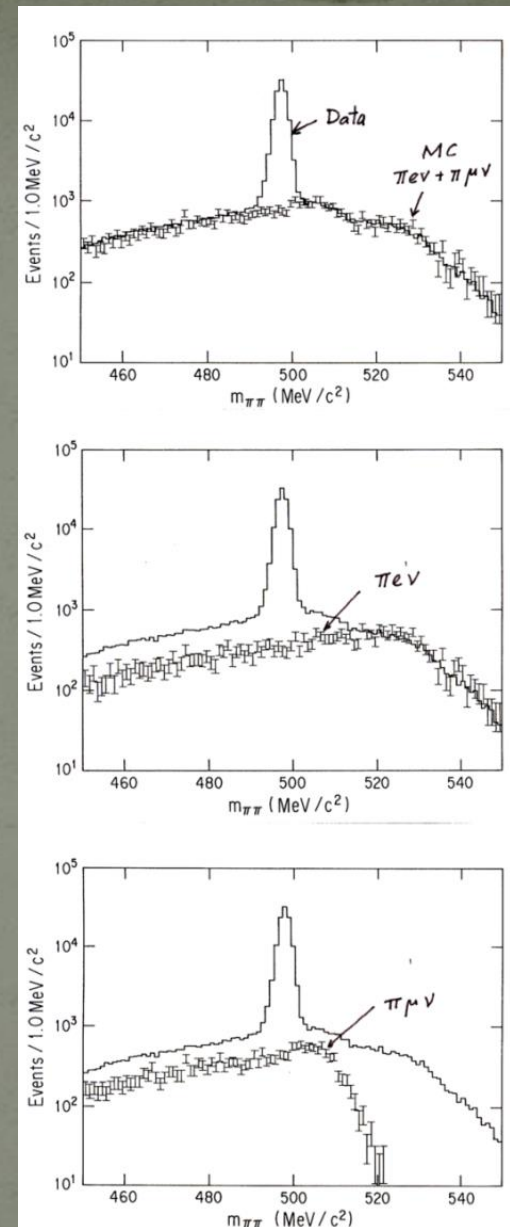
Simulations for detector response as well as for physics results is quite important, although I haven't included them in the present lecture.

I would really recommend and ask you to train you easily carry these simulations.

An example of a simulation of physics results

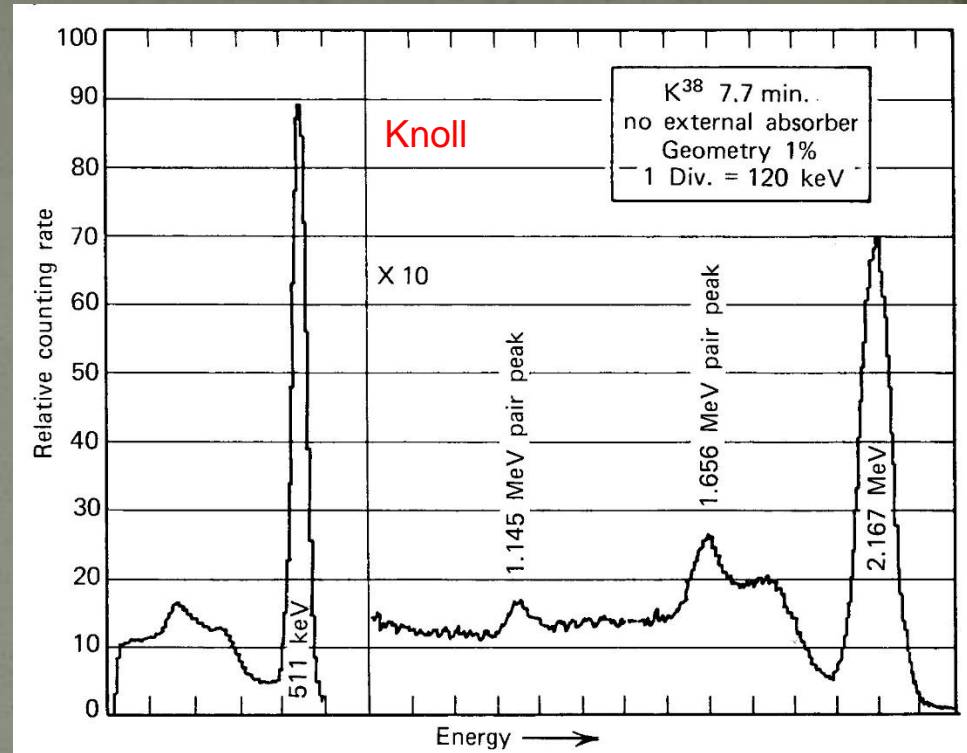
In E137, invariant mass distribution of two tracks assumed to $\pi\pi$, for the event sample of the summed momentum directing to the production target.

- Simulation well reproduced shape of the tail, even for a small structure around 600 MeV.
- This got us confirm that we were doing a real KL measurement.
- This provided us pure π , μ , e samples by taking a specific mass region, and the sample s were quite useful for calibrations of PID detectors.
- The peak is on the KL mass, and was used for the normalization of other modes.



Simulation is also crucial for a detector design

Spectrum obtained from a 5.62 cm-squared NaI(Tl) crystal using 2.167 MeV photons from ^{38}K . Not simple, but can be perfectly reproduced by Giant.



Training for a simulation code such as Giant must be fruitful for your future.