



Quarks and Compact Stars 2019

Sep. 26 ~ 28, 2019, Haeundae, Busan, Korea



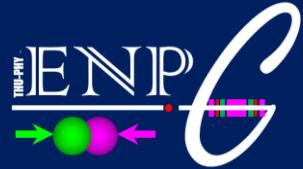
Isospin Dynamics in Heavy Ion Reactions and Constraining of Nuclear Symmetry Energy

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TSINGHUA UNIVERSITY DEPARTMENT OF PHYSICS



Outline

1 Introduction: Nuclear Symmetry Energy from Heavy ion collisions

2 Transport of Isospin DOF in HIC

2.1 Isospin Dependent Hierarchy of Particle Emission

2.2 Extraction of $E_{\text{sym}}(\rho)$

2.3 HIRA^{TU}: Isospin chronology study

3 Future: Isovector orientation effect of deuteron-induced reaction

4 Summary

Symmetry Energy as a function of density

$$B(Z, A) = B_v + B_s + B_c + B_a + B_p$$

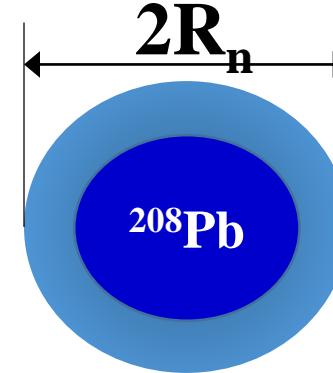
$$= a_v A - a_s A^{2/3} - a_c Z^2 A^{-1/3} - \boxed{a_a (A/2 - Z)^2 A^{-1}} + a_p \delta A^{-1/2}$$

Symmetry Term

$$E(\rho, \delta) = E_0(\rho) + \delta^2 E_{\text{sym}}(\rho) = a_v + \frac{\kappa}{18} \varepsilon^2 + \frac{J}{162} \varepsilon^3 + \dots + \delta^2 \left(E_{\text{sym}} + \frac{L}{3} \varepsilon + \dots \right)$$

κ : Compressibility

$E_{\text{sym}}(\rho)$



(Neutron Star and NS Merge)

(Static or Resonant Properties of Nuclei)

(Heavy Ion Collisions)

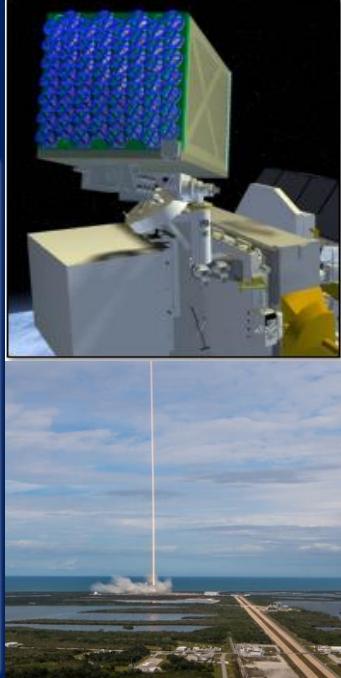
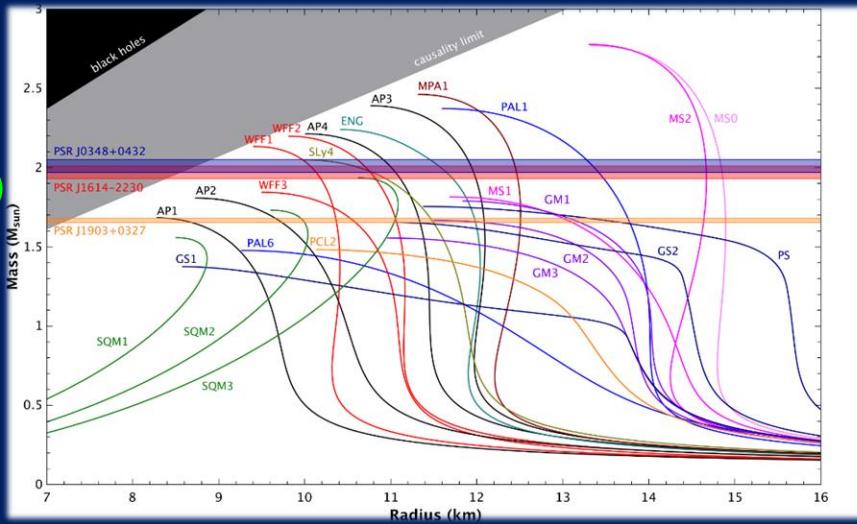


$E_{\text{sym}}(\rho)$ becomes a frontier in major Labs

Neutron Star Observatory:

Neutron Star Interior Composition Explorer (NICER)

To Constrain EOS of nuclear matter through precise M and R measurements of several neutron stars.



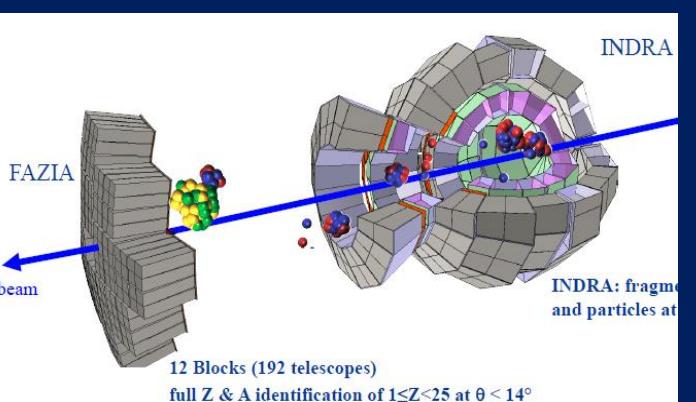
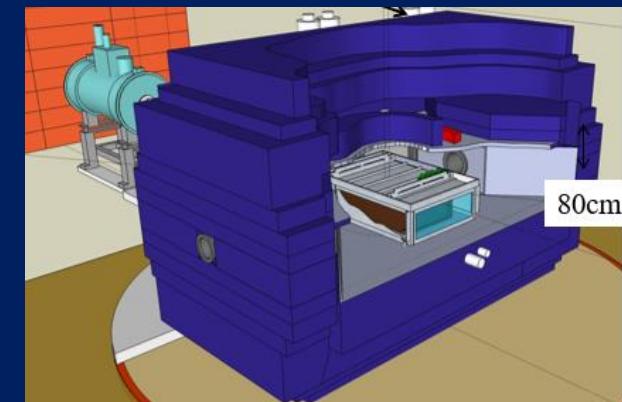
HI accelerator and RIB facilities:

SAMURAI-TPC@RIKEN

HIRA@NSCL, MSU

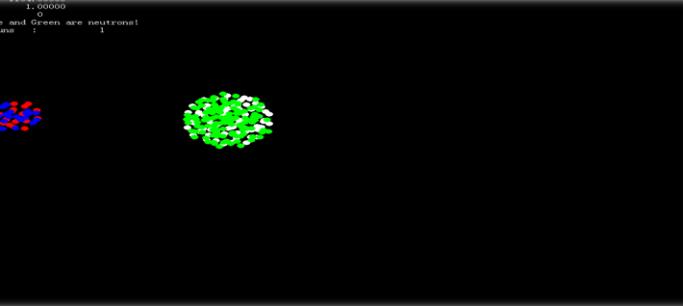
INDRA@GANIL

CHIMERA @ INFN



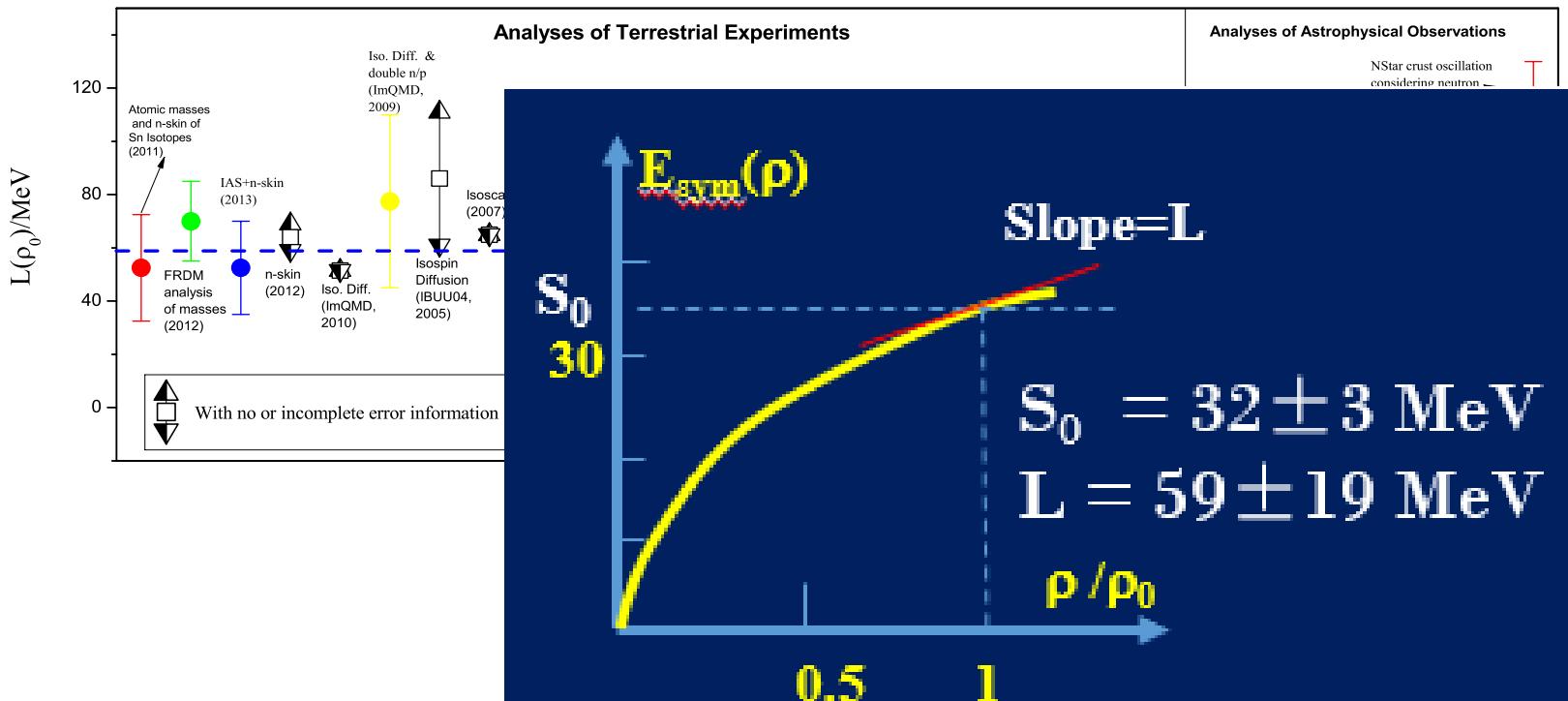
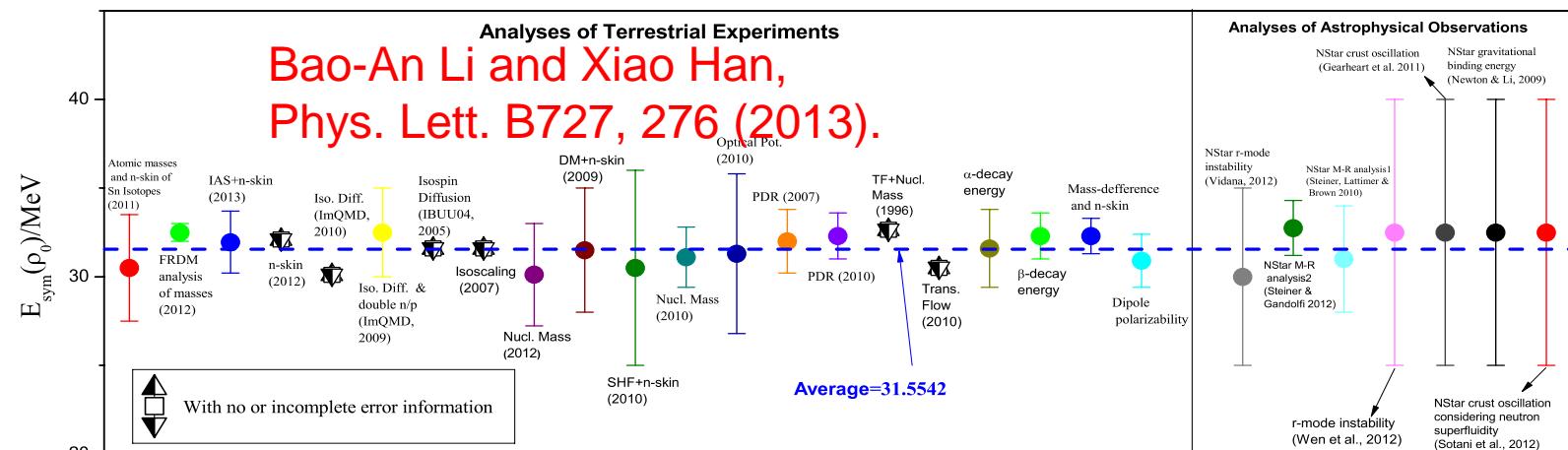
Isospin transport and the constraint of $E_{\text{sym}}(\rho)$

At sub-saturation densities



List extends:

- Isospin diffusion (MSU ...)
- Isospin scalaring and isospin fractionaiton (MSU...)
- n/p ratio of fast and pre-equilibrium nucleons (MSU ...)
- N/Z of the emitted fragments (LNS, TAMU, MSU, HIRFL ...)
- GMR strength (ND ...)
- HBT correlation function (KVI, MSU, HIRFL ...)
-



Symmetry Energy and isospin transport in HIC

Mechanisms governs the transport of IDOF in nuclear collisions:

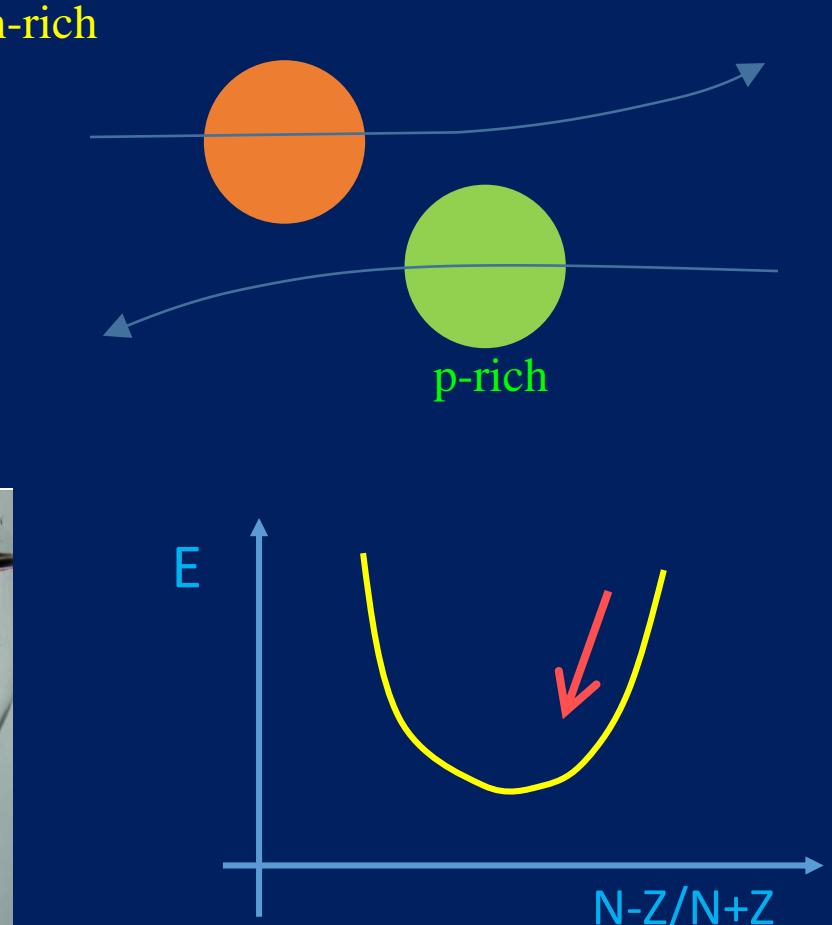
1. Isospin Diffusion :

$$j_{np} = j_n^I - j_p^I = -(D_n^I - D_p^I) \nabla I$$

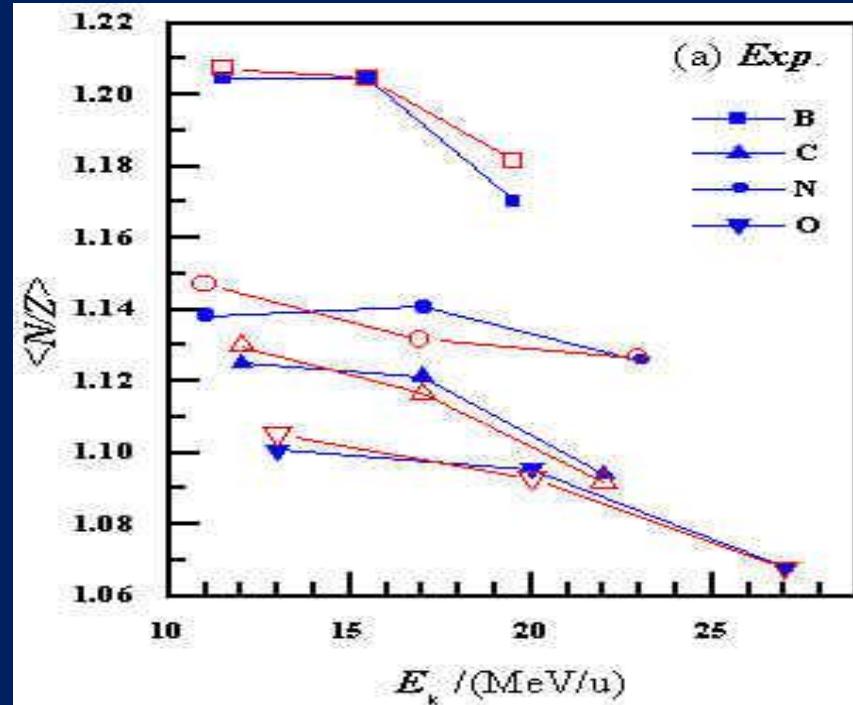
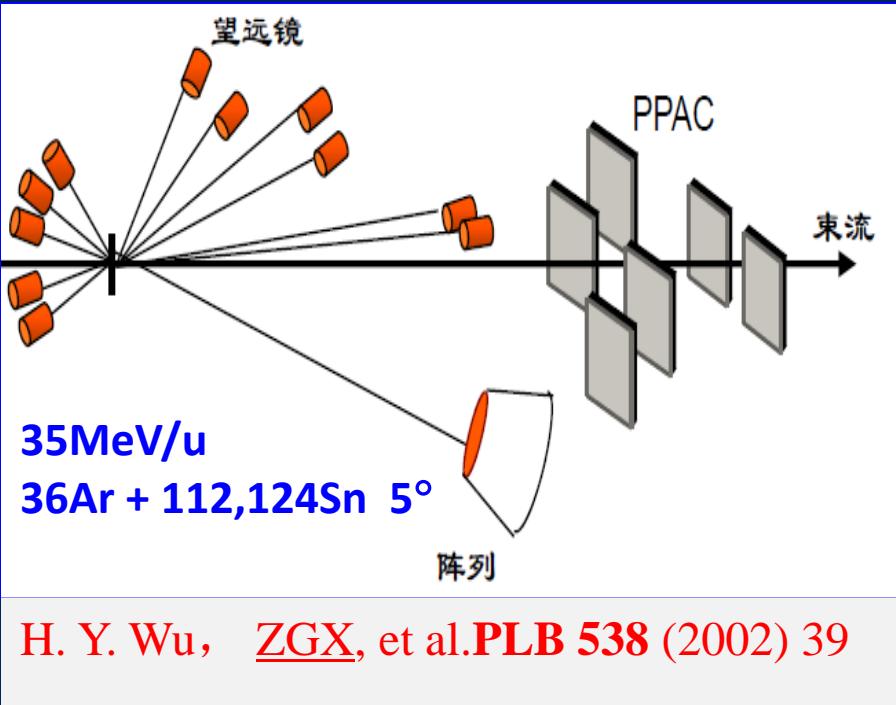
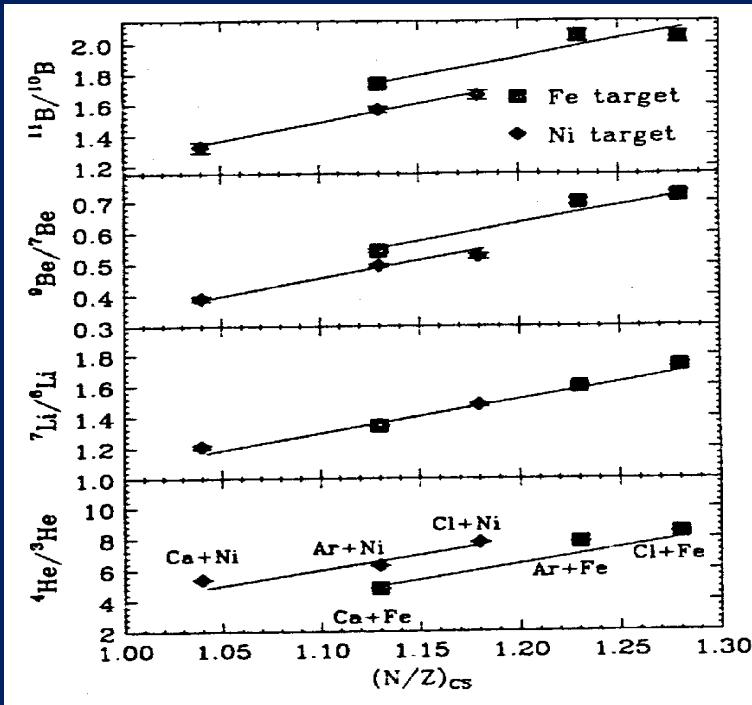
$$D_n^I - D_p^I \propto 4\rho E_{sym}(\rho)$$

Likely terminated when P-T separated.

A everyday-life analog of isospin diffusion



Isospin Diffusion



- Bao-An Li et al., PRC 57, 2065 (1998).
- S. Yennello et al., PLB 321, 15 (1994).
- LW Chen et al., JPG 23, 211 (1997).
- ZY Sun et al., PRC 82, 051603 (2010).

Using the kinetic of the p-like residues as a clock, We found that,
 → in Peripheral collision, N/Z of the projectile increases with lowering
 the kinetic energy, showing the transport process of IDOF.

Confirmed in later experiments :

- G. A. Souliotis et al., PRC90, 064612 (2014).
- G. A. Souliotis et al., PLB588, 35 (2004).

Symmetry Energy and isospin transport in HIC

Mechanisms governs the transport of IDOF in nuclear collisions (II)

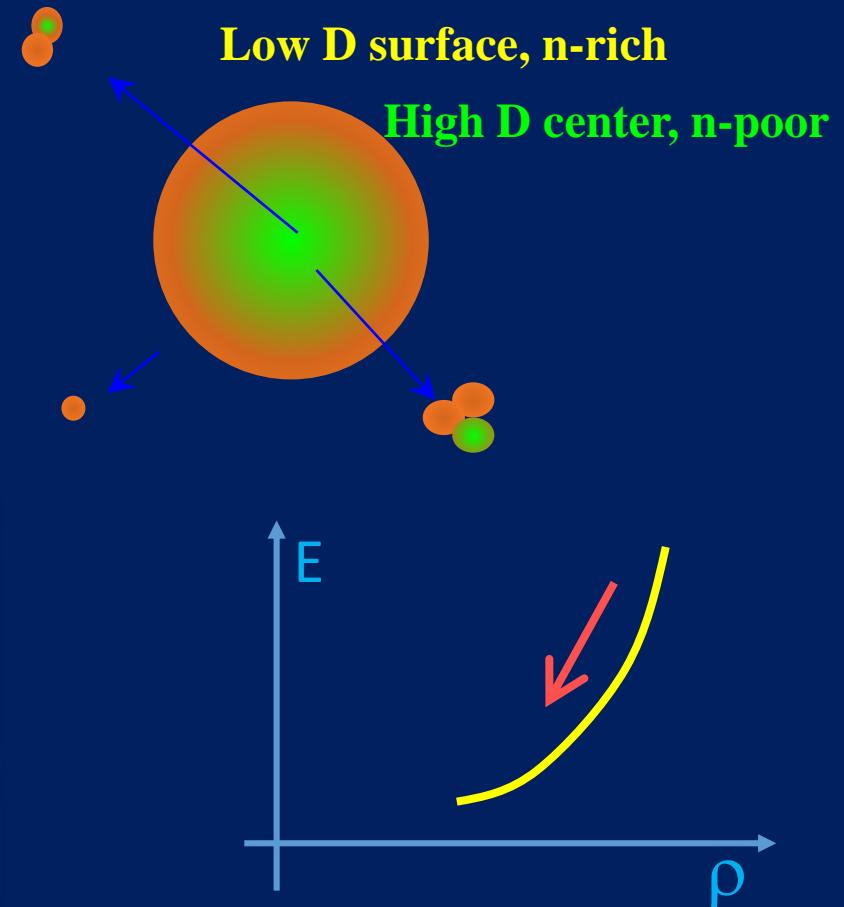
2. Isospin Drift :

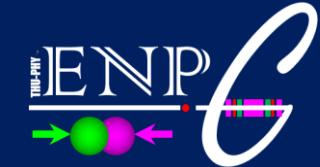
$$j_{np} = j_n^\rho - j_p^\rho = (D_n^\rho - D_p^\rho) \nabla \rho$$

$$D_n^\rho - D_p^\rho \propto 4I \frac{\partial E_{sym}(\rho)}{\partial \rho}$$

Likely persists for longer time.

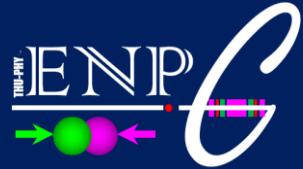
A everyday-life analog of isospin drift





What is our Motivations with HIC?

- 1) **Look for new $E_{\text{sym}}(\rho)$ ($\rho < \rho_0$) probes in slow process for the enhanced sensitivity.**
 - Neck Emission in Fission reactions is characterized by low density and neutron-richness.
 - Transport of isospin degree of freedom (IDOF) involving the neck emission helps to identify a probe.
- 2) **To measure quantitatively the time scale of the transport of IDOF.**
- 3) **To develop new method to pin down the $E_{\text{sym}}(\rho)$ ($\rho < \rho_0$) .**



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1 Introduction: Nuclear Symmetry Energy from HIC

2 Transport of Isospin DOF in HIC

2.1 Isospin Dependent Hierarchy of Particle Emission

2.2 Extraction of $E_{\text{sym}}(\rho)$

2.3 HIRA^{TU}: Isospin chronology study

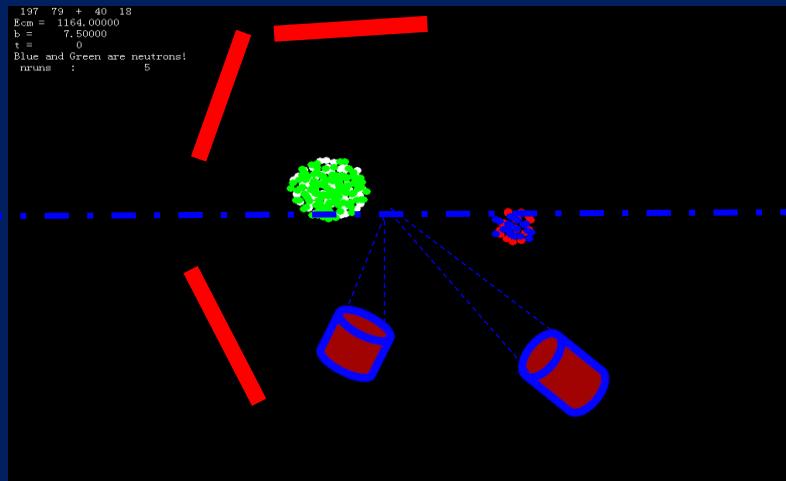
3 Future: Isovector orientation effect of deuteron-induced reaction

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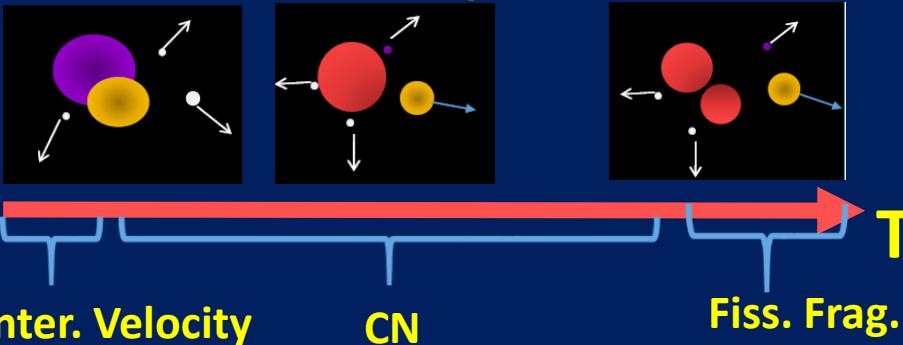
2.1 Isospin Dependent Hierarchy of Particle Emission

35 MeV/u Ar+ Au.

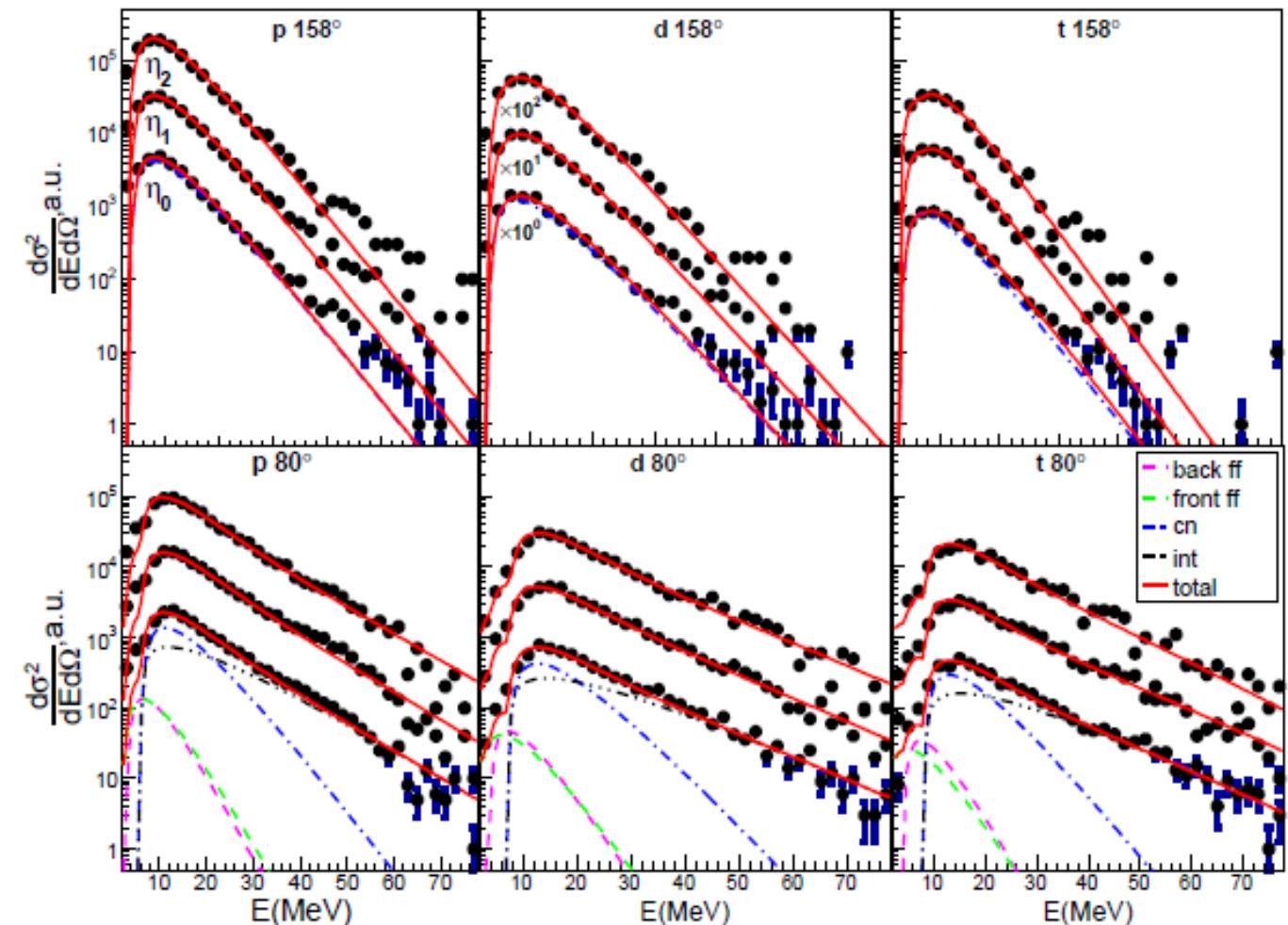
Trigger: 2 fission fragments .AND. 1 LCP



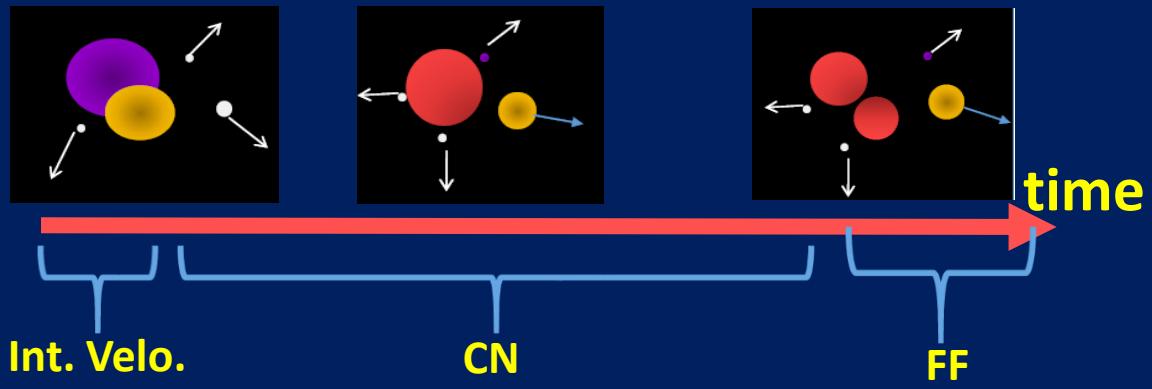
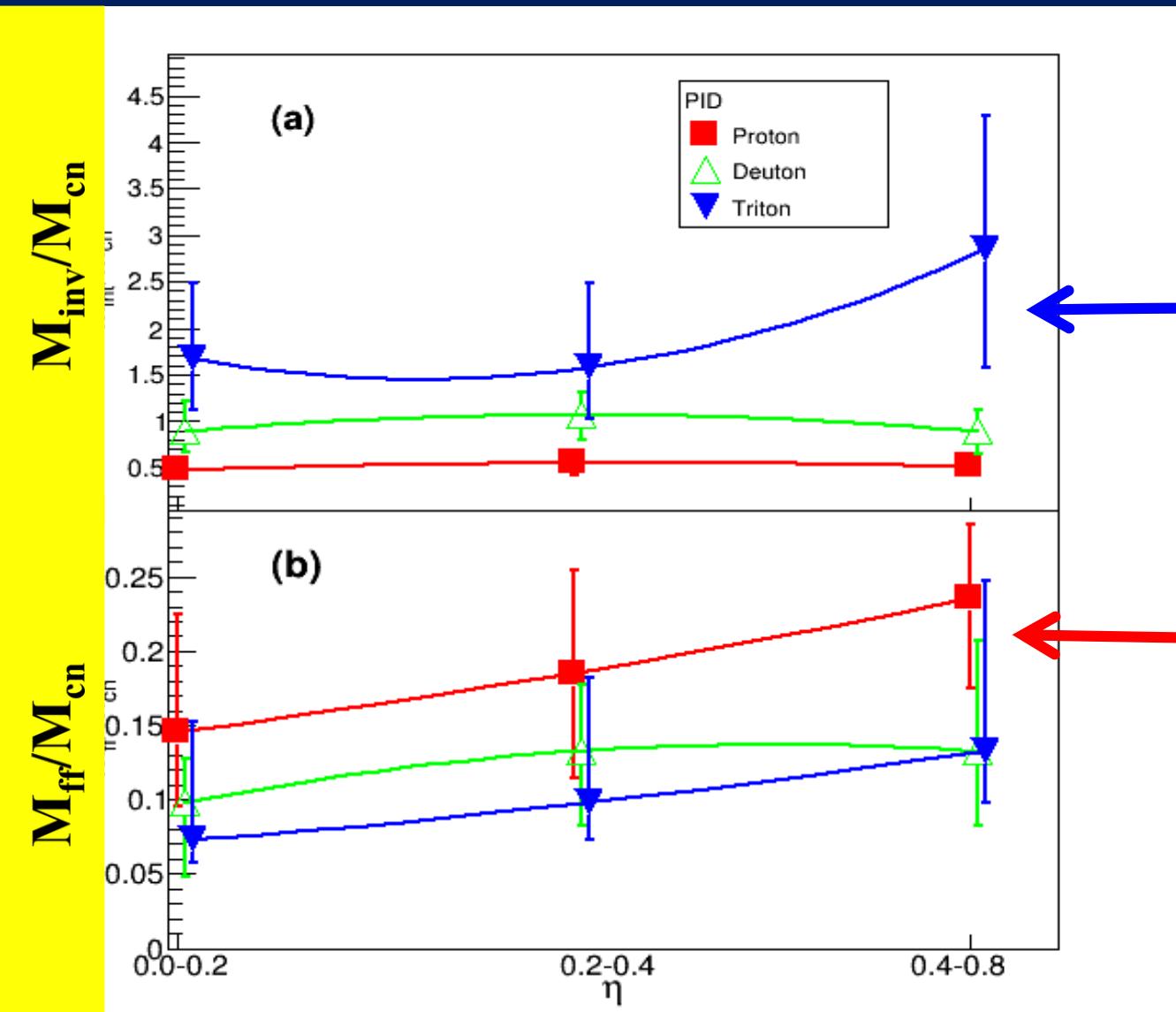
- Three Moving source:



$$\frac{d^2\sigma}{d\Omega dE} = \frac{N}{2(\pi T)^{3/2}} (E - E_c)^{1/2} \exp[-(E - E_c)/T]$$



Multi moving source analysis



More proton emission

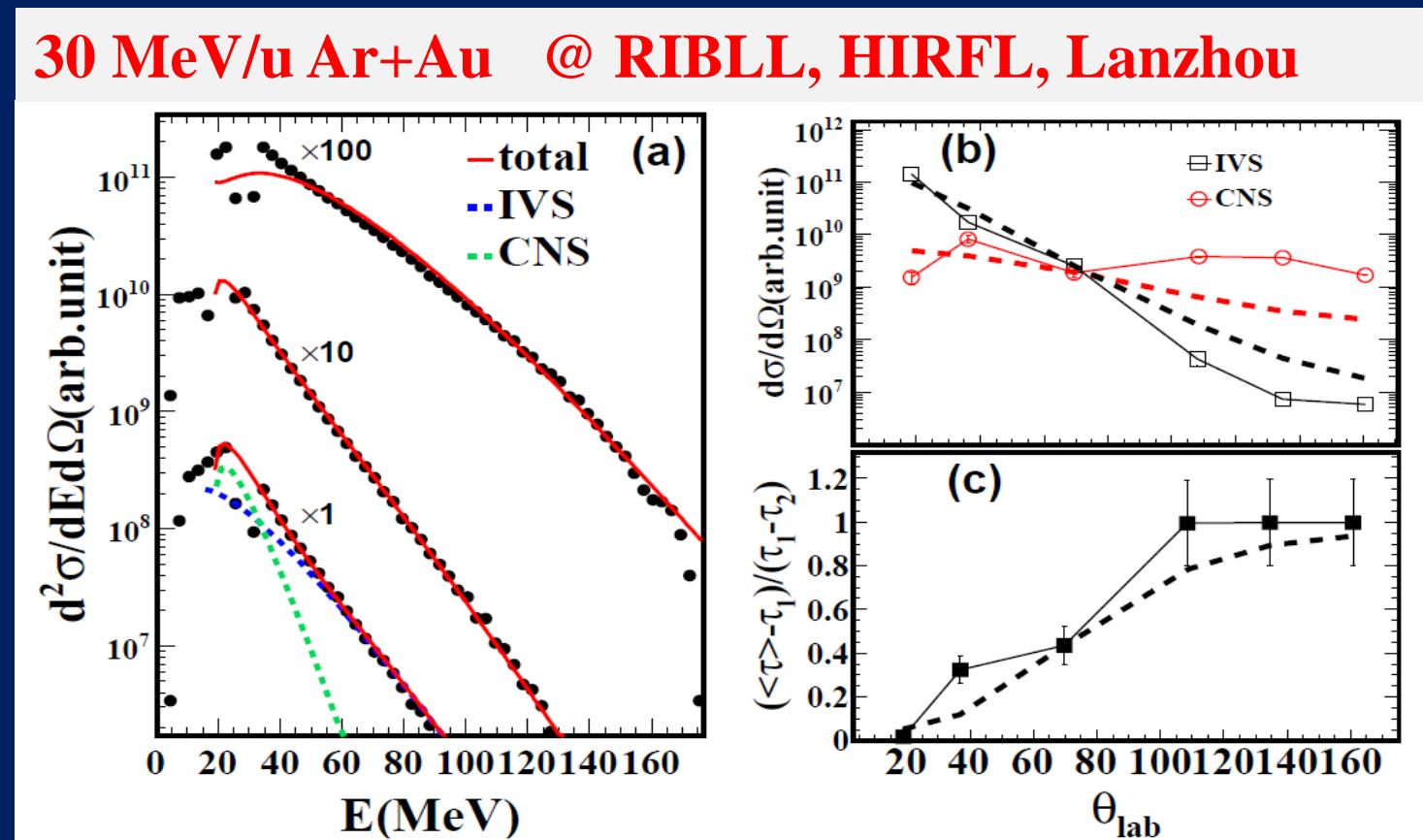
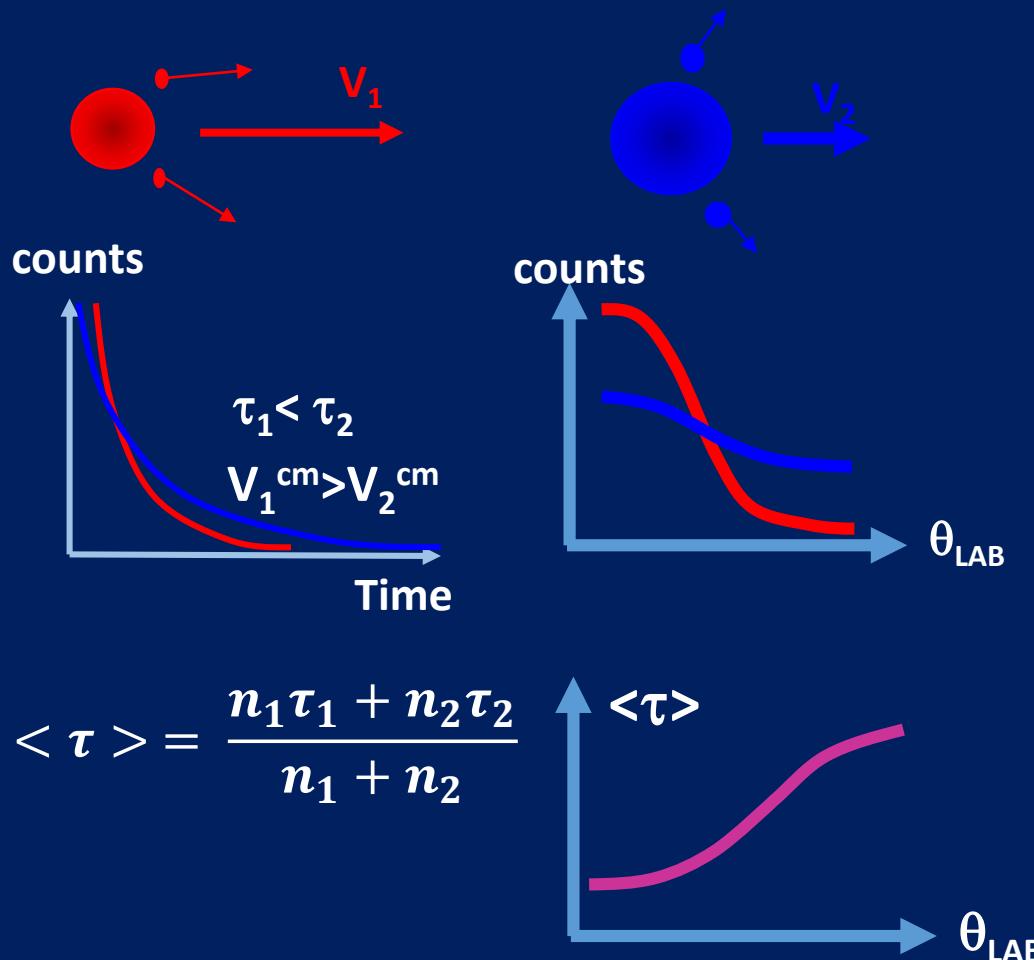
More triton emission

A isospin-dependent hierarchy of particle emission is observed.

R. S. Wang, Y. Zhang, XZG... et al.,
PRC89 (2014) 064613



2.2 Long-time feature of isospin drift



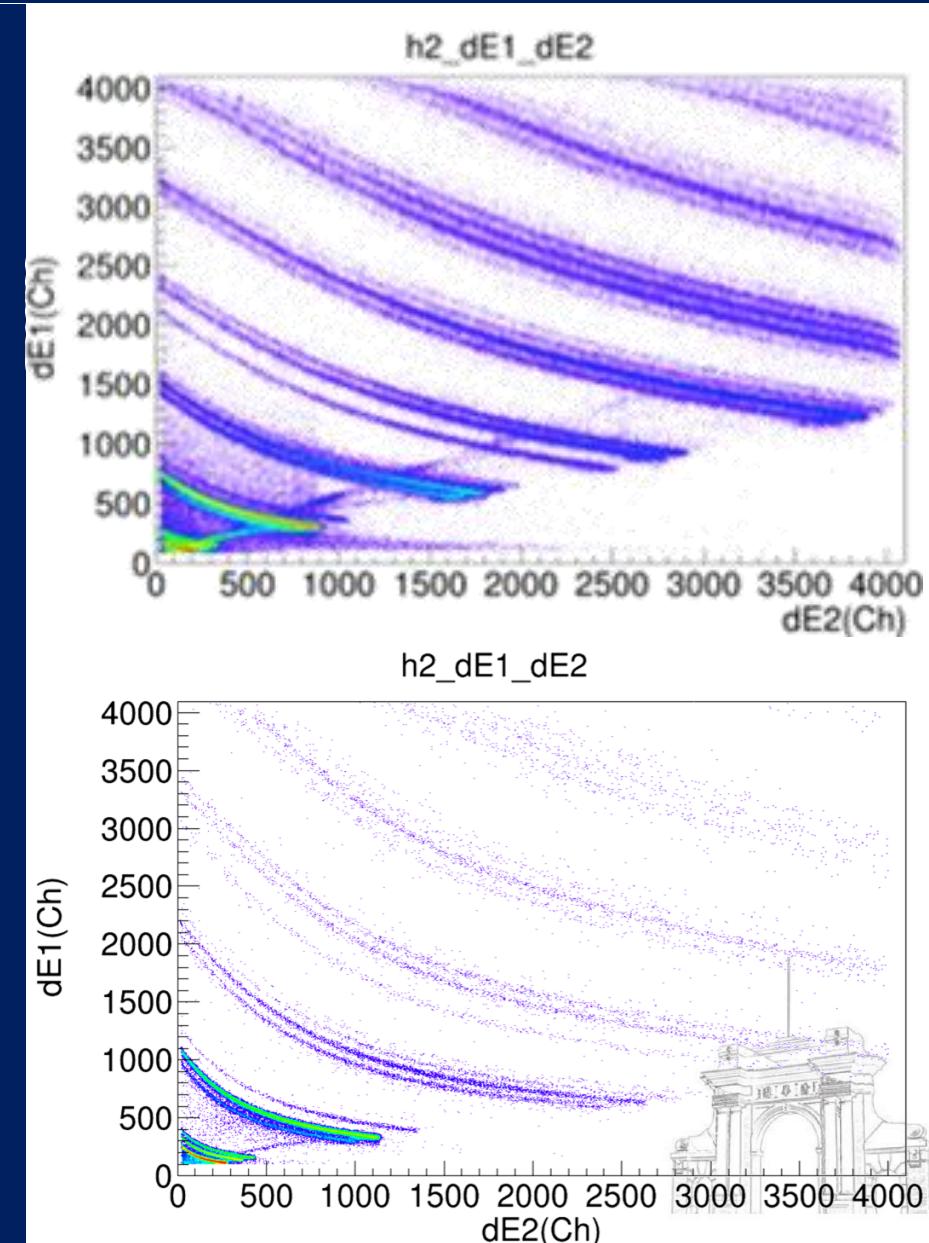
- moving-source analysis indicates that a qualitative relation between angular distribution and the average emission time exists
- The relationship shall holds, even though the real process is more complex.

Long time isospin drift and the constraint of $E_{\text{sym}}(\rho)$



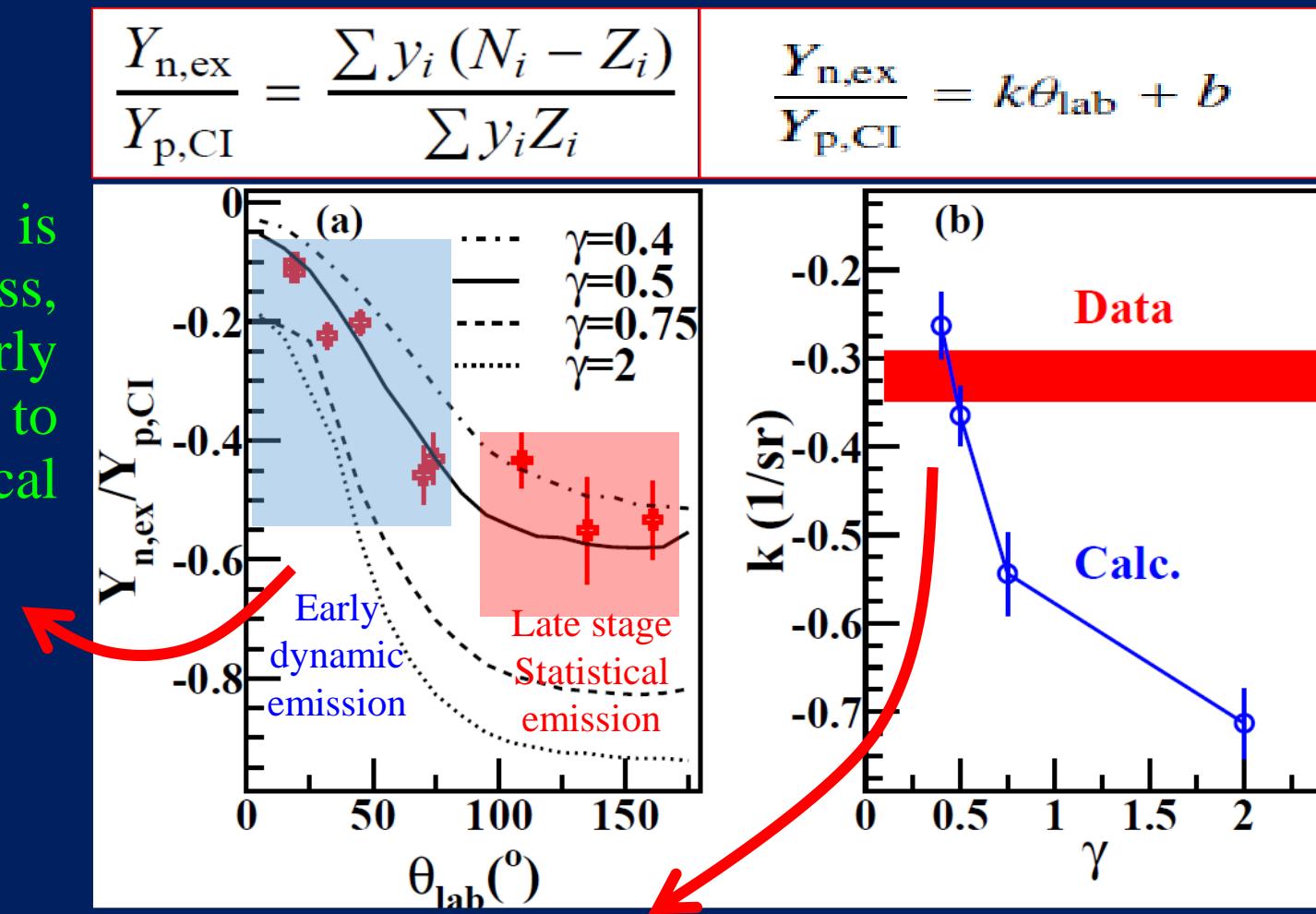
30 MeV/u Ar+Au @ RIBLL,
HIRFL, Lanzhou

Telescope	Silicon1 (μm)	Silicon2 (μm)	CsI(cm)	Position (θ, φ)
Telescope1#	150	200	2*2*3	(37,69)
Telescope2#	75	200	2*2*3	(19,39)
Telescope3#	75	200	2*2*3	(19,39)
Telescope4#	50	200	2*2*3	(45,170)
Telescope5#	30	200	2*2*3	(74,39)
Telescope6#	50	300	1.5*1.5*2	(70,13)
Telescope7#	25	300	1.5*1.5*2	(161,37)
Telescope10#	30	200	2*2*3	(109,196)
Telescope11#	50	300	1.5*1.5*2	(135,110)



Constraint of the $E_{\text{sym}}(\rho)$ with IMQMD+GEMINI

1) Isospin drift is long time process, persisting from early dynamic emission to late statistical emission



Y. Zhang , ...
ZGX , PRC 95,
041602(R) (2017)

2) $E_{\text{sym}}(\rho)$: $\gamma = 0.46 \pm 0.025$ (STDEV)
 $L = 47 \pm 14$ MeV (CL=95%)
with S_0 fixed at 28.3 MeV.

GO Potential Fit:
 $L = 53 \pm 23$ MeV
PRC 82, 054607 (2010)
Proton Emission:
 $L = 52 \pm 7$ MeV
PRC 94, 044322 (2016)
GW170817 QMF18:
 $L = 40$ MeV
APJ, 862, 98 (2018)
H. Sagawa et al., :
 $L = 42 \pm 14$
Custipen 2019
H. Shen et al., TM1e
 $L = 40$ MeV

- How long is long?
- How short is short?
- How do we measure?

2.3 HIRATU : Isospin Chronology



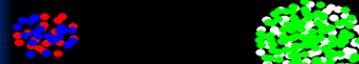
- How long is long? How short is short?

- **Isospin Chronology:** A chronology is an account or record of the times and the order in which a series of past events took place.

10^{-2} s



```
a = 1164.0000  
b = 1.0000  
t = 0  
Blue and Green are neutrons!  
runns : 1
```



10^{-21} s

$\tau \sim 10^{-21} \text{ s}$

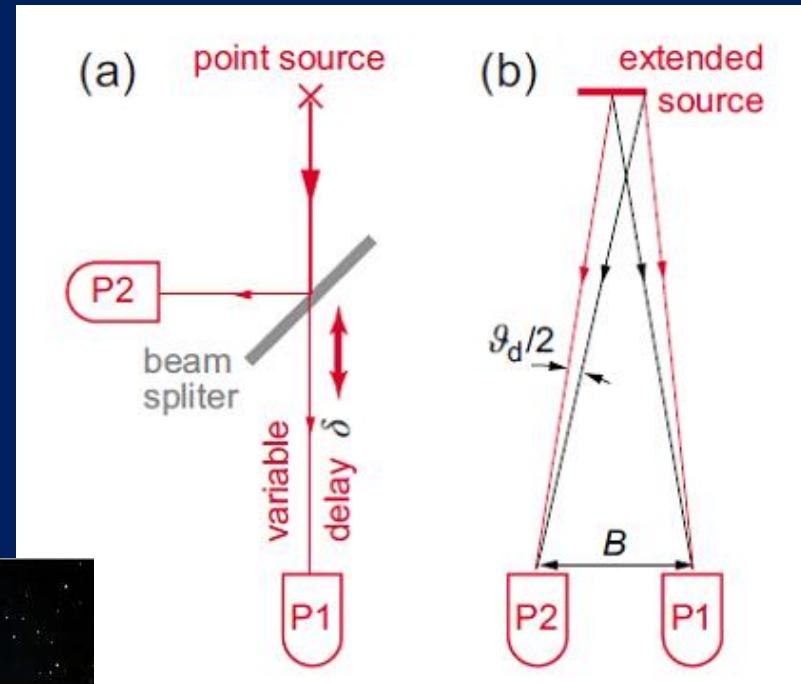
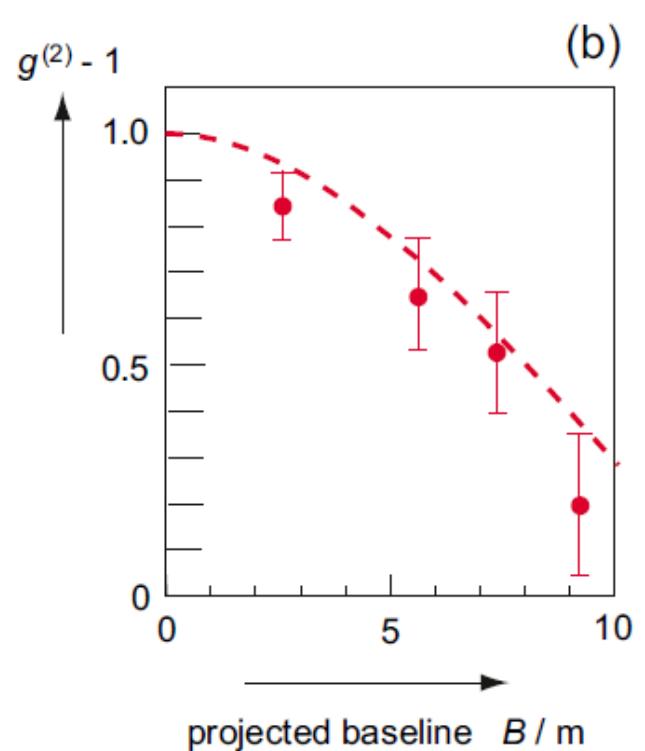
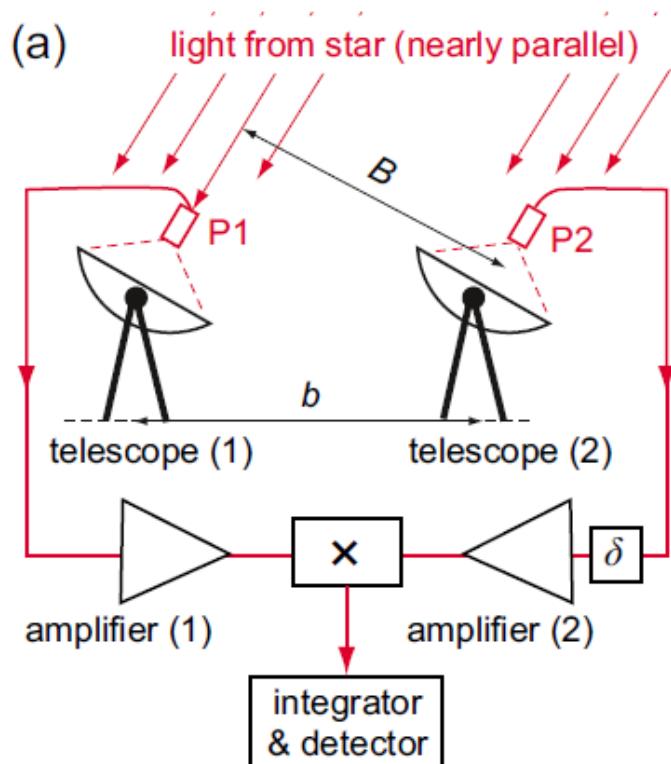
How?



Hanbury Brown-Twiss Method

- 1950s, Hanbury Brown and Twiss propose a intensity interferometry to measure the size information of the stellar object.

Hanbury Brown and Twiss, **Nature 177**, 27 (1956)



- HBT is invented to measure the space information

Hanbury Brown and Twiss,
Nature 178, 1046 (1956)

HBT correlation

Unlike the amplitude interference! HBT correlation is intensity interferometry, referring the correlation of the two intensities. It is the second order interference.

In a classic picture: the spherical waves emitted from a and b are :

$$\alpha e^{ik|\vec{r} - \vec{r}_a| + i\varphi_a} / |\vec{r} - \vec{r}_a| \quad \beta e^{ik|\vec{r} - \vec{r}_b| + i\varphi_b} / |\vec{r} - \vec{r}_b|$$

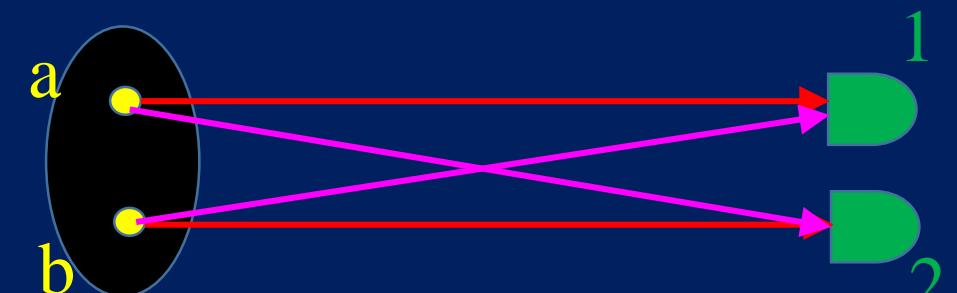
The amplitude of the signal seen in Detector 1:

$$A_1 = \frac{1}{L} [\alpha e^{ikr_{1a} + i\varphi_a} + \beta e^{ikr_{1b} + i\varphi_b}]$$

Do the average over time, one has: $\langle e^{i(\varphi_b - \varphi_a)} \rangle = 0$

One get the light intensity is:

$$\langle I_1 \rangle = \langle I_2 \rangle = \frac{1}{L^2} [\alpha^2 + \beta^2]$$



HBT correlation

Finally, One arrive at : $\langle I_1 I_2 \rangle = \frac{1}{L^4} \left[L^4 \langle I_1 \rangle \langle I_2 \rangle + 2\alpha^2 \beta^2 \cos((\vec{k}_2 - \vec{k}_1) \cdot \vec{R}) \right]$

The Correlation function is defined as :

$$C(\vec{d}, k_1, k_2) = \frac{\langle I_1 I_2 \rangle}{\langle I_1 \rangle \langle I_2 \rangle} = 1 + 2 \frac{\langle \alpha^2 \rangle \langle \beta^2 \rangle}{(\alpha^2 + \beta^2)^2} \cos((\vec{k}_2 - \vec{k}_1) \cdot \vec{R})$$

Approximately, it reads :

$$C(\vec{d}, k_1, k_2) \approx 1 + \frac{1}{2} \cos((\vec{k}_2 - \vec{k}_1) \cdot \vec{R})$$

Considering a source with density distribution $\rho(r)$, the correlation function is written as

$$C(\vec{d}, k_1, k_2) - 1 = \left| \int \rho(r) e^{i(\vec{k}_1 - \vec{k}_2) \cdot \vec{r}} d^3 r \right|^2$$

Obviously, C is as a function of d via Δk , d is the base line of the two detectors.

$C(\vec{d}, k_1, k_2)$ is the Fourier transformation of the density distribution of the source.

HBT in nuclear physics

- 1960s, Goldhaber Analyzed the $\pi\pi$ correlation in $\bar{p}p$ annihilation
- 1977, S. Koonin extended the HBT to pp correlation in heavy ion reactions

Distribution of proton in the fireball

$$\frac{1}{\sigma} \frac{d\sigma}{dp_1 dp_2} = \int_{-\infty}^{\infty} dt_1 dt_2 \int dr_1 dr_2 D(r_1 t_1, \mathbf{p}) D(r_2 t_2, \mathbf{p})$$

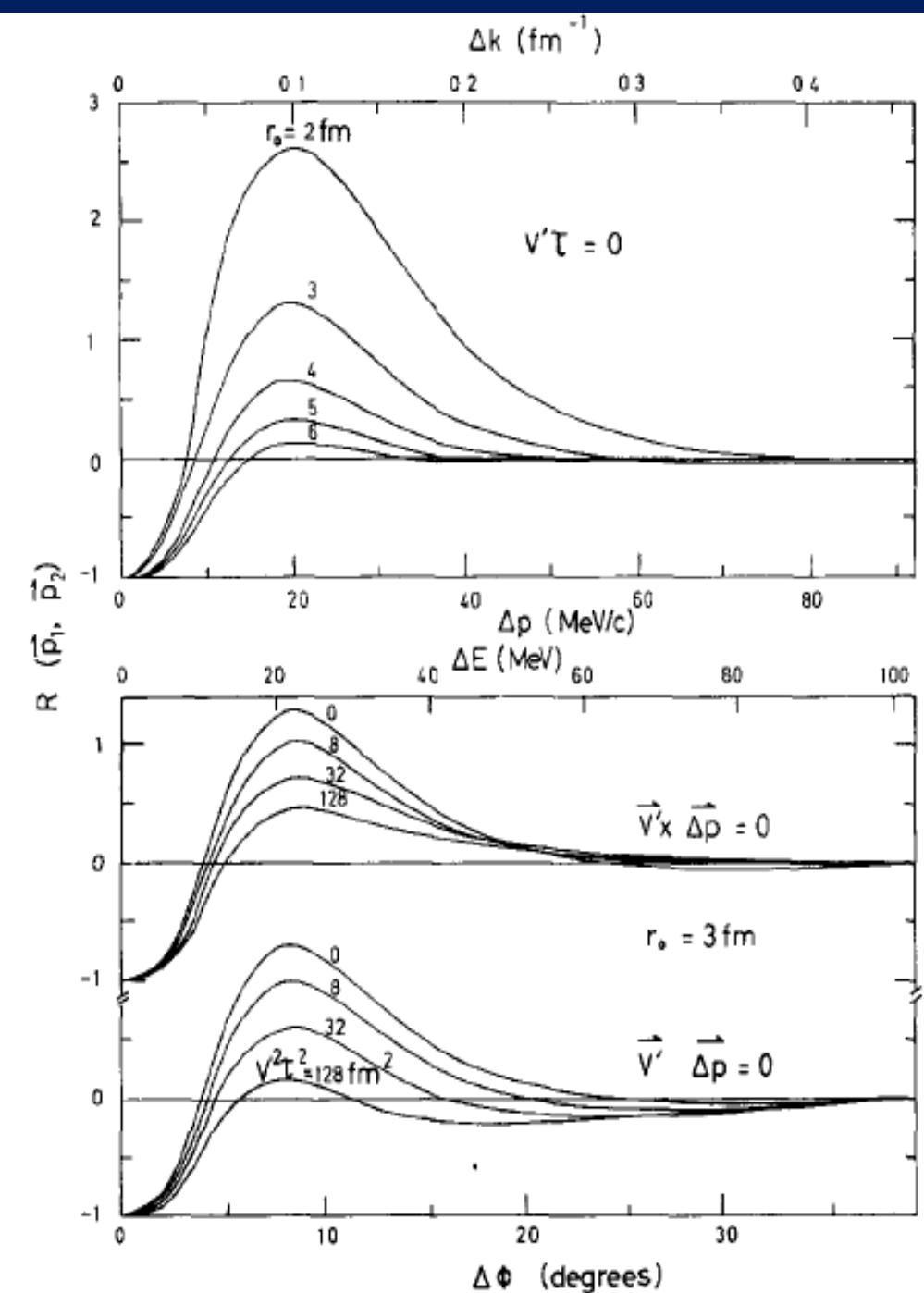
$$\times \left\{ \frac{1}{4} |{}^1\Psi_{\mathbf{p}_1 \mathbf{p}_2}(r'_1, r'_2)|^2 + \frac{3}{4} |{}^3\Psi_{\mathbf{p}_1 \mathbf{p}_2}(r'_1, r'_2)|^2 \right\}. \quad (1)$$

Plane wave multiplying the pp relative motion wave function.

$$D(rt, \mathbf{p}) = \frac{1}{\sigma} \frac{d\sigma}{d\mathbf{p}} \left(\frac{1}{\pi^{3/2} r_0^3} e^{-(r - V_0 t)^2/r_0^2} \right) \left(\frac{1}{\pi^{1/2} \tau} e^{-t^2/\tau^2} \right) \quad (2)$$

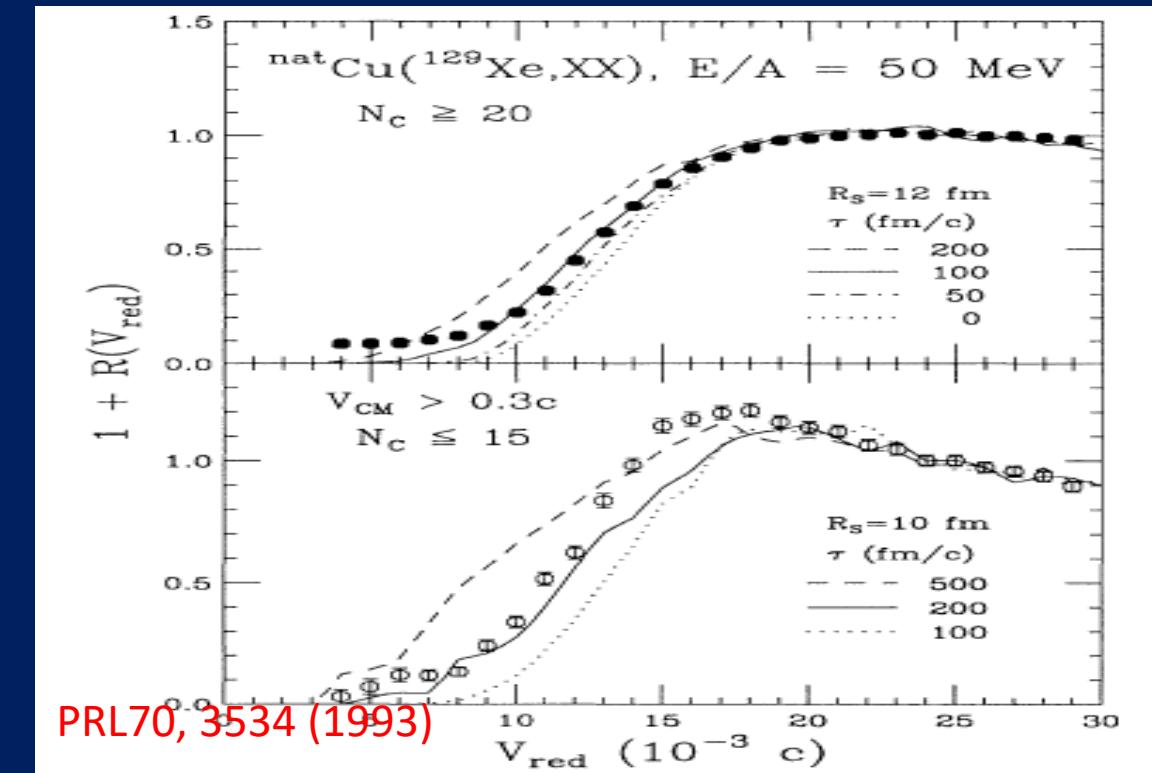
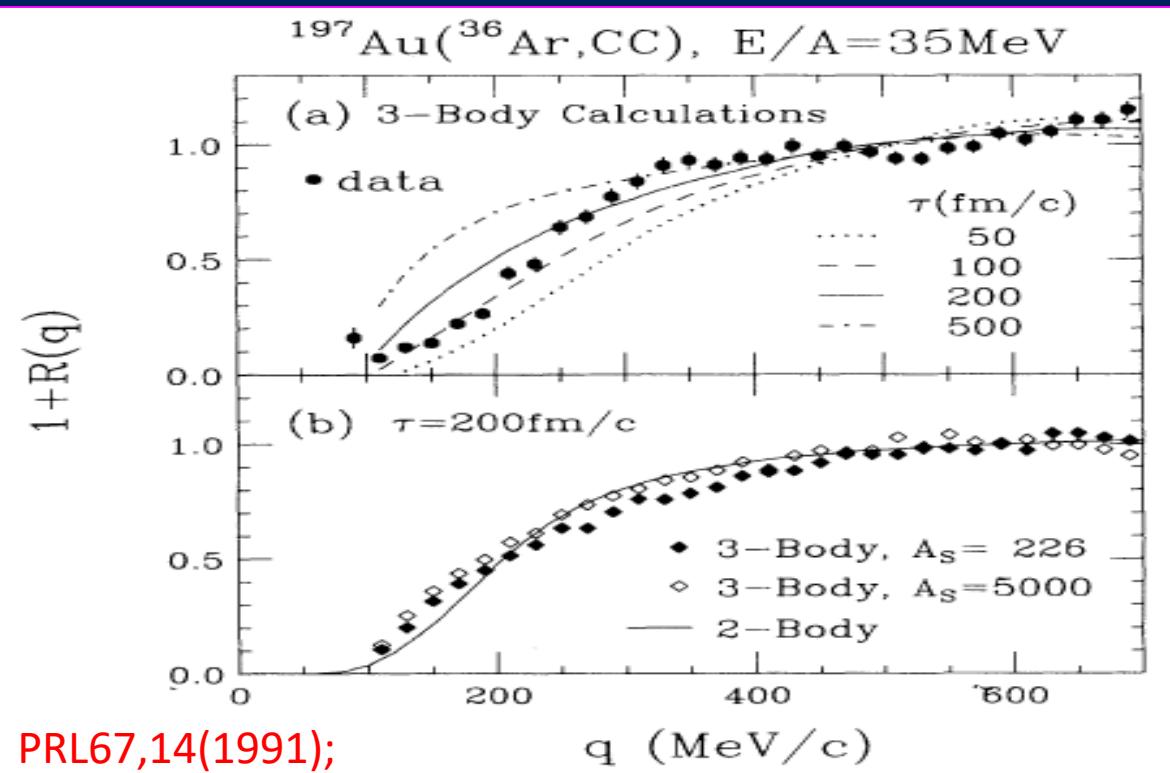
PROTON PICTURES OF HIGH-ENERGY NUCLEAR COLLISIONS

Steven E. KOONIN¹ PLB70, 43(1977)
The Niels Bohr Institute, Copenhagen, Denmark



Since 1990s HBT widely applied in nuclear reactions

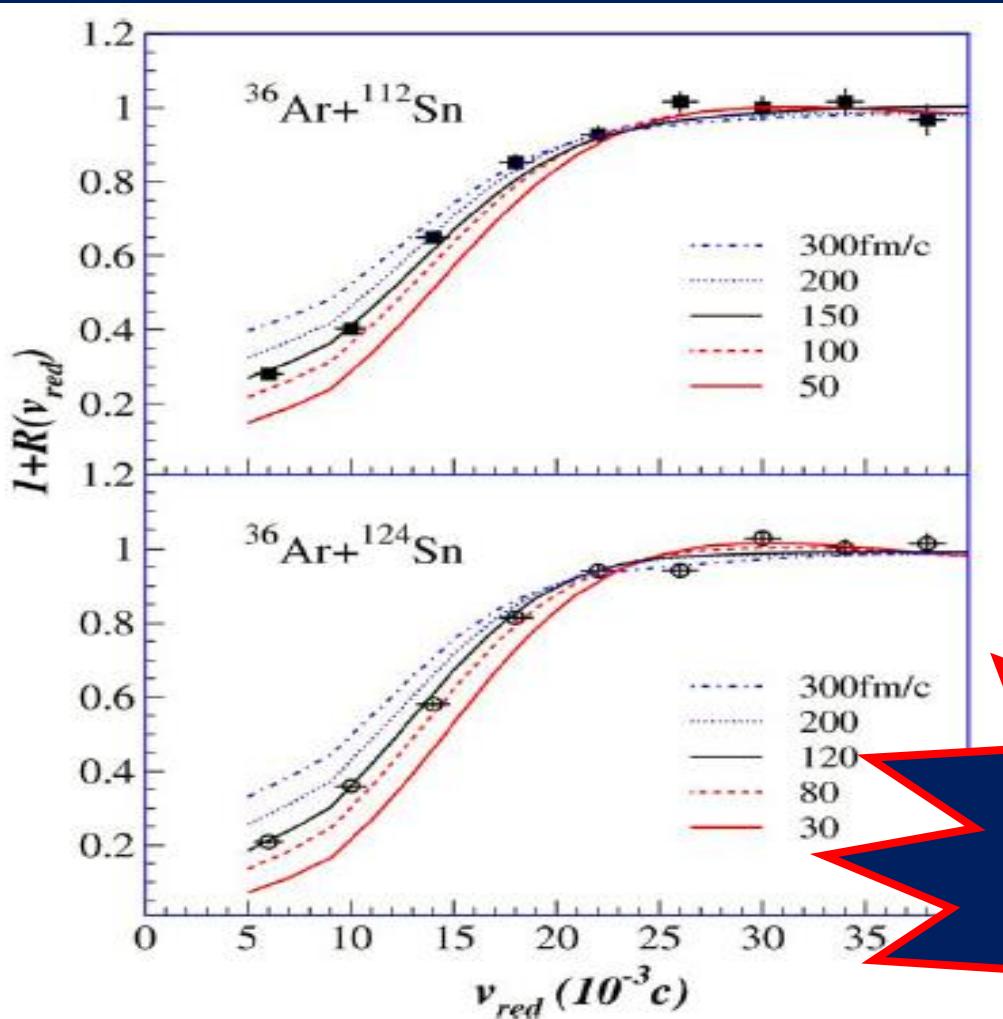
PLB70,43(1977), PRL67,14(1991); PRC51,1280(1995); PRC,69,031605R(2004); NPA620,214(1997); PRL 77,4508(1997) ; PRL70, 3534 (1993).....



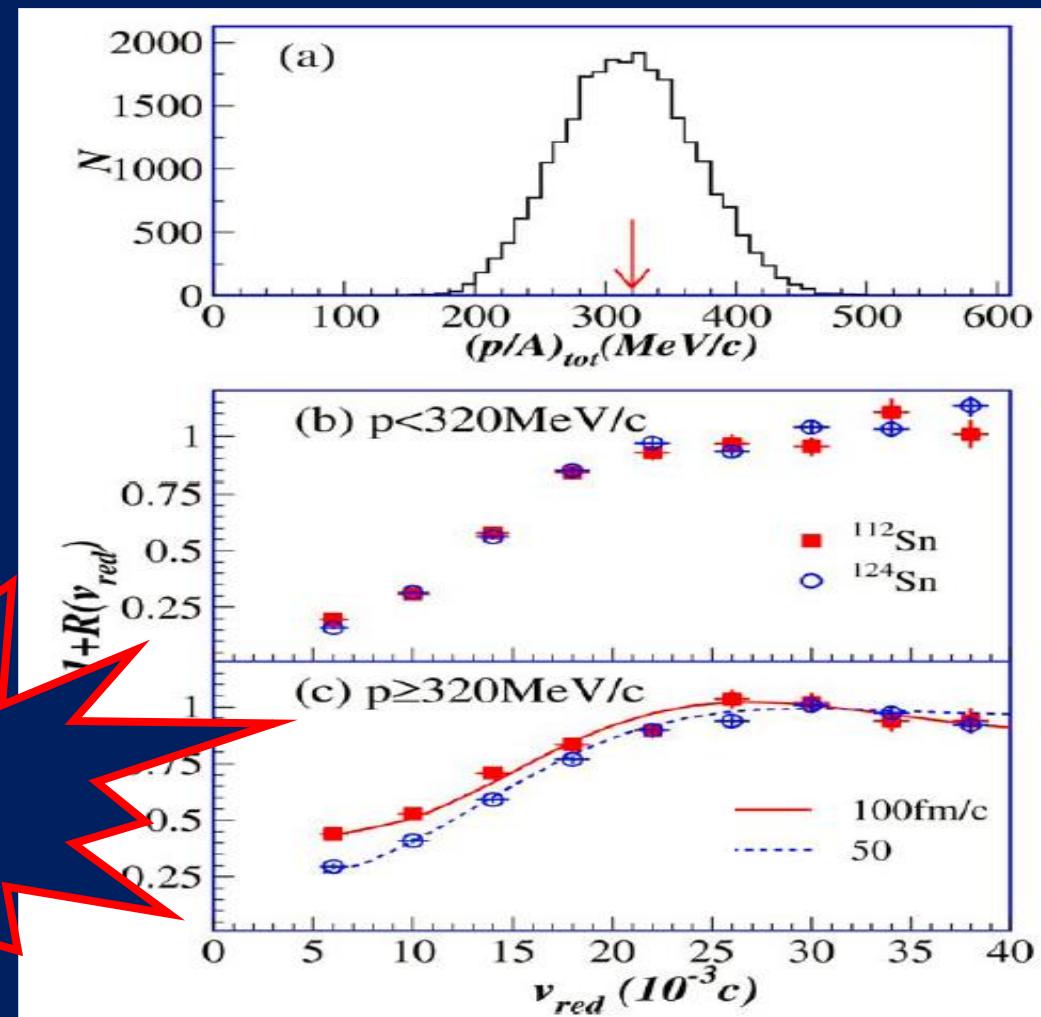
Y. D. Kim , IMF correlation function in 35 MeV/u Ar+Au ,
IMF emission time scale: 100-200 fm/c.

D. Bowman , 50 MeV/u Xe+Cu, IMF correlation
function at different centrality, time scale confirmed at
100 fm/c.

Isospin Effect in HBT Correlation Function



~50 fm/c time
resolution
achievable



ZGX, R. J. Hu, H. Y. Wu et al., PLB 639, 436 (2006) ; R. J. Hu, ZGX et al., HEPNP 31, 350 (2007)

- Stronger Coulomb anti-correlation is observed in $\text{Ar} + ^{124}\text{Sn}$, this difference arises from the isospin difference of the two system.

HIRA^{TU}: A future array for Isospin chronology in HIC

- Heavy Ion Research Array at Tsinghua University (**HIRA^{TU}**)

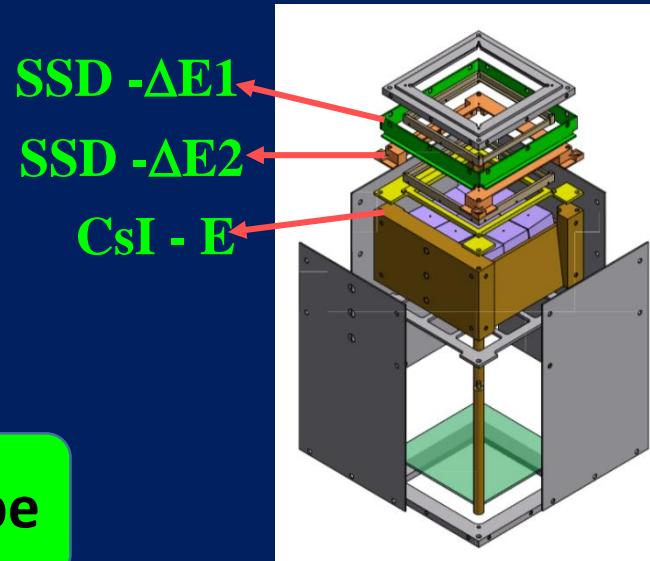
Technique Features:

Fission Fragments: PPAC

LCP in coincidence: SSD-SSD-CsI Telescope

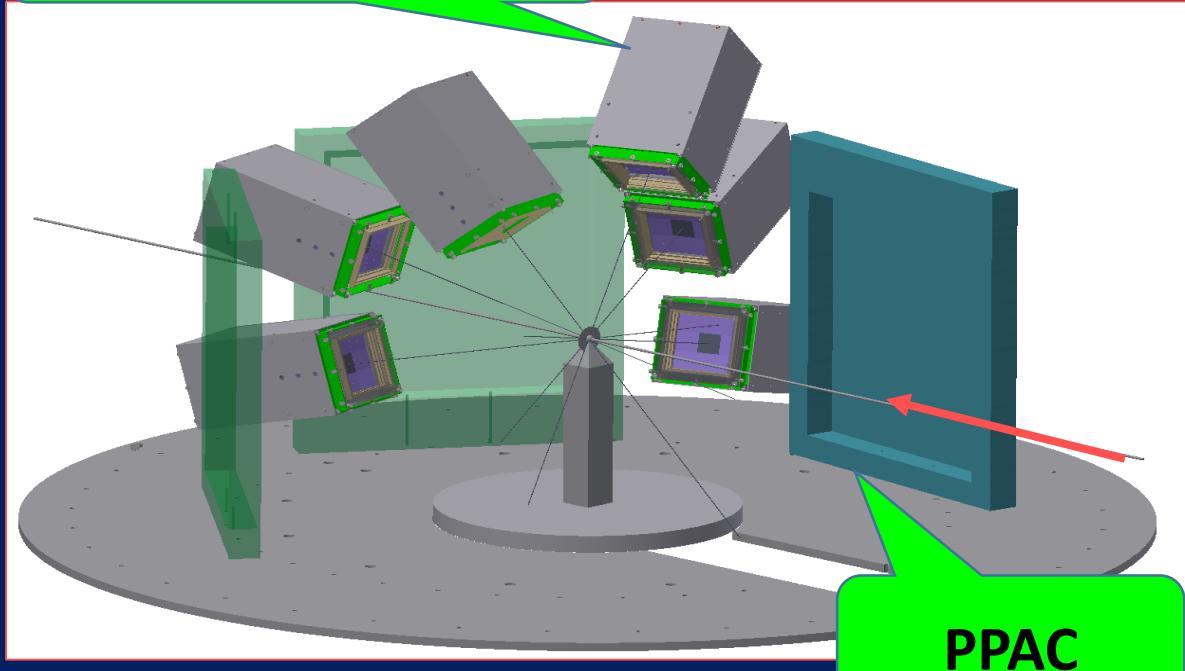
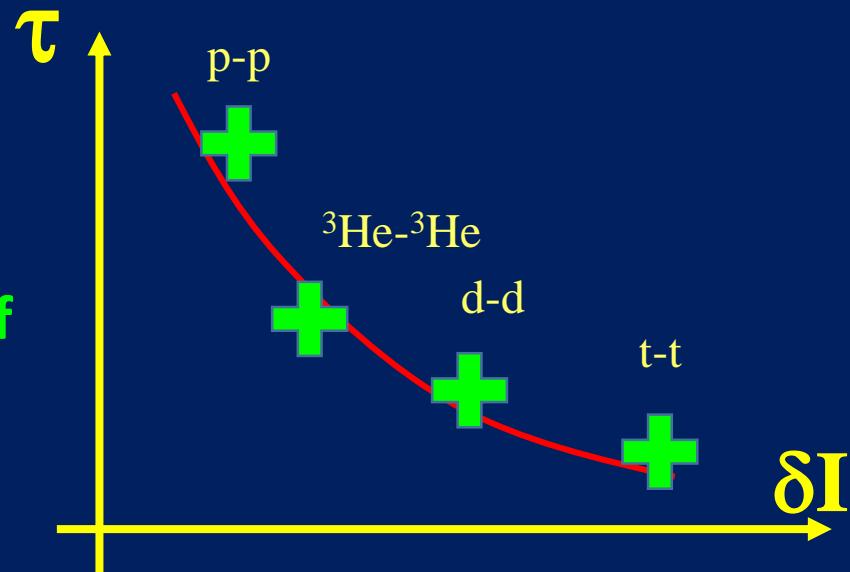
Total Channels: 700

Position/Energy Resolution: 2mm / 1%



HIRA type Telescope

Capable of measuring the HBT correlation of isospin-resolved particle pair



PPAC

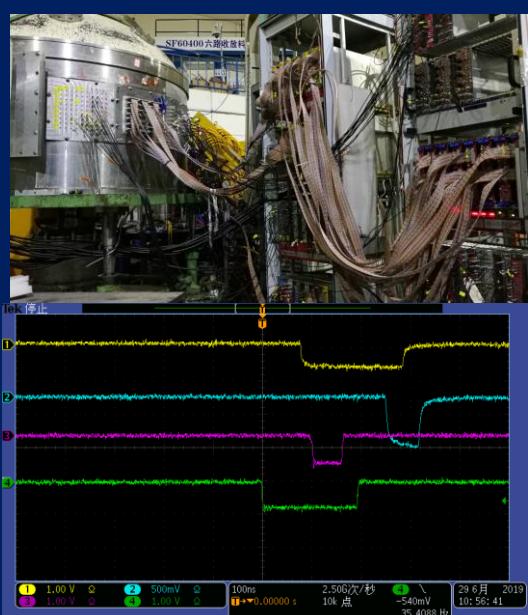
HIRA^{TU}: Phase-1 Experiments



Beam time: 6-13 Feb., 2018;
Reaction: Ar+Au at 30 MeV/u;
1/3 SSD telescopes



Beam time: 5-12 July., 2019;
Reaction: Kr+Au at 25 MeV/u;
2/3 SSD telescopes with cooling

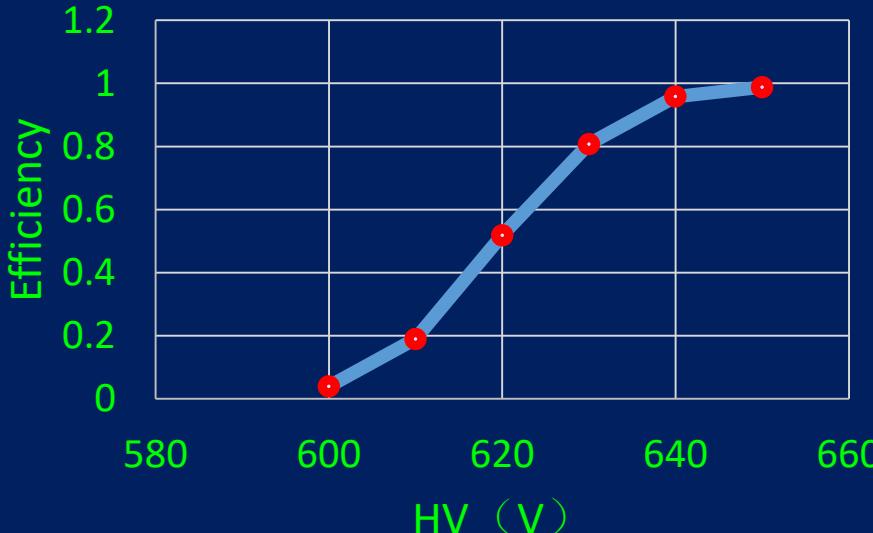


PPAC Performance for fission fragments (30 MeV/u Ar+Au)

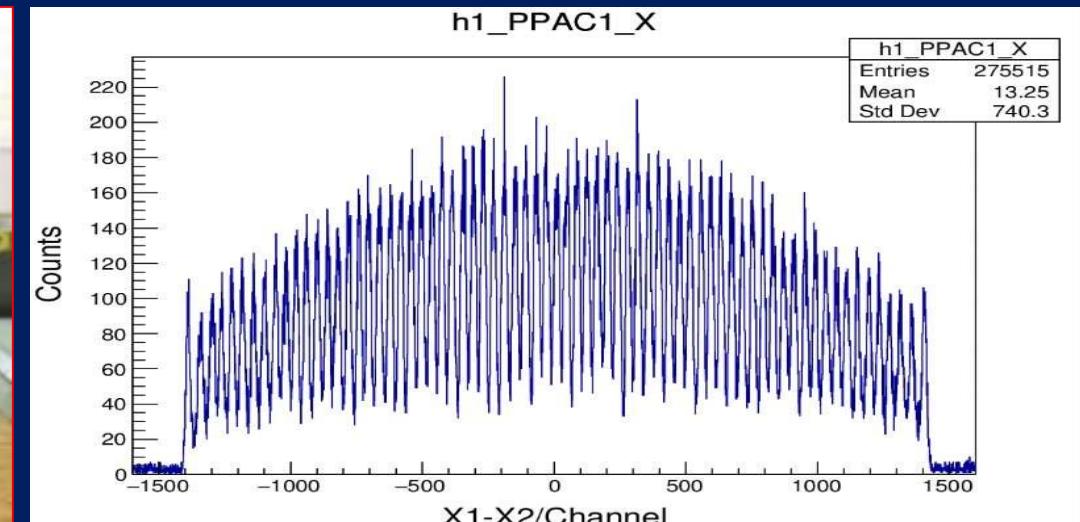
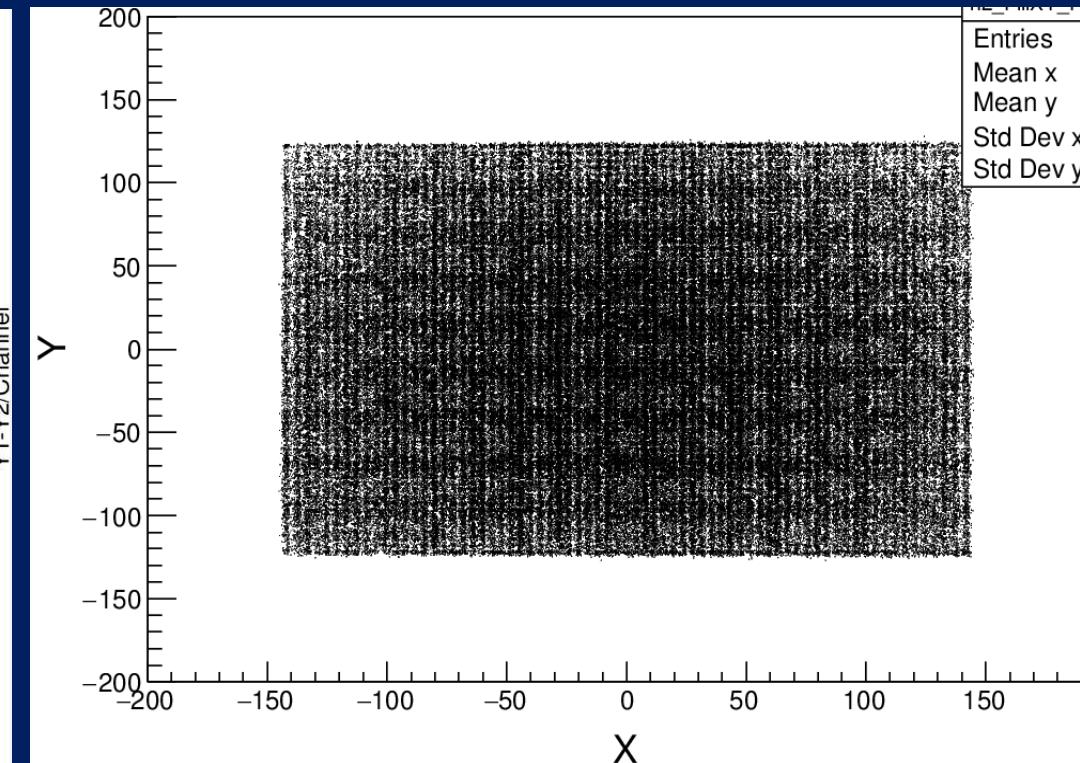
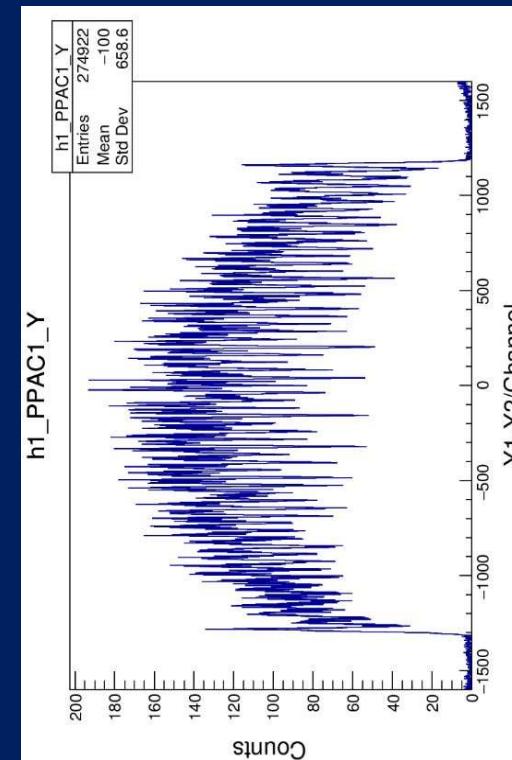
Efficiency for F. fragments/ Cf-252



Efficiency for alpha/ Pu-239

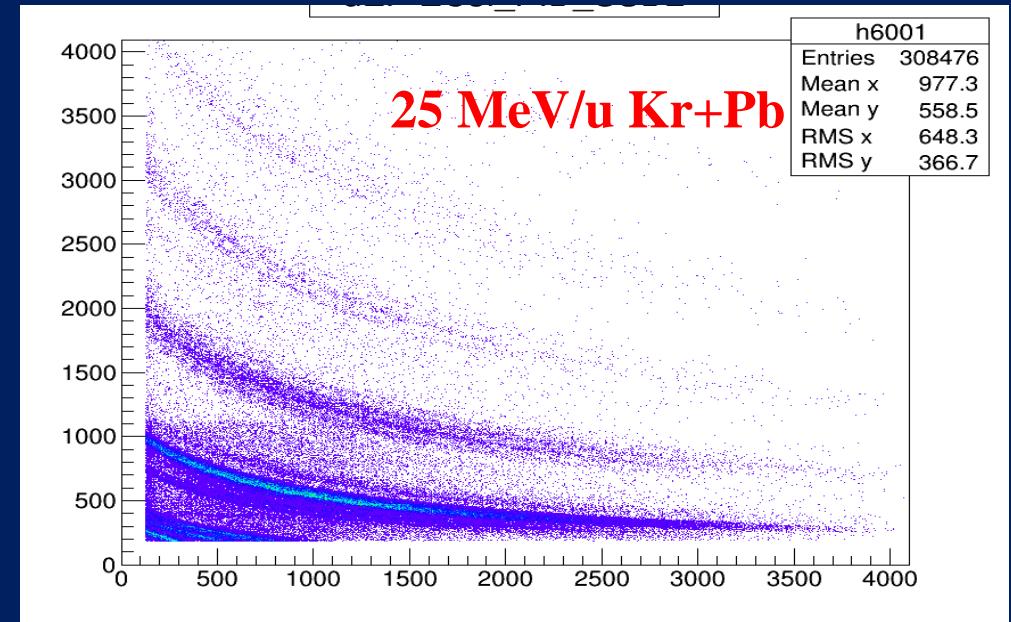
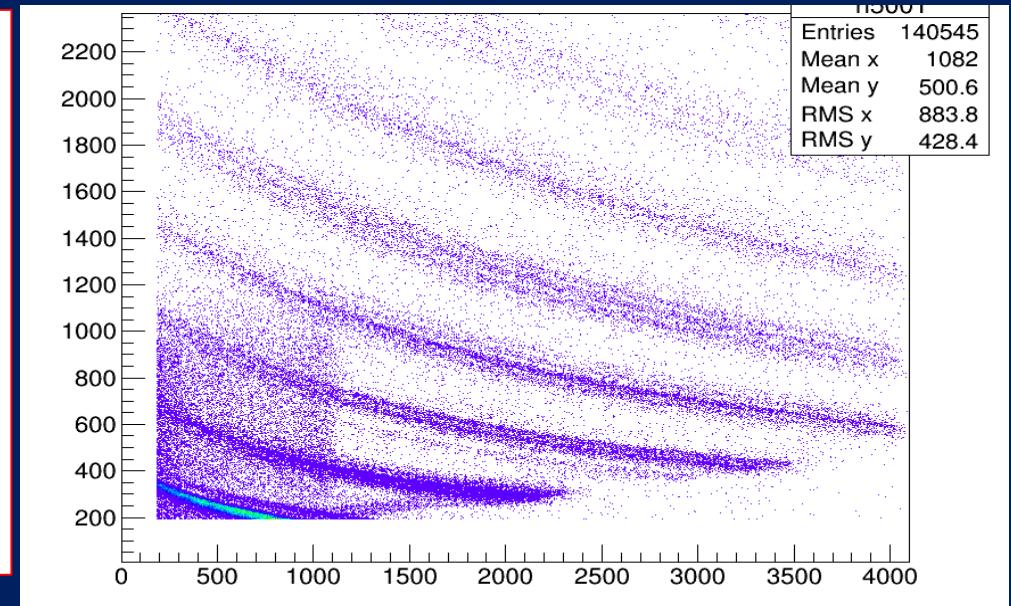
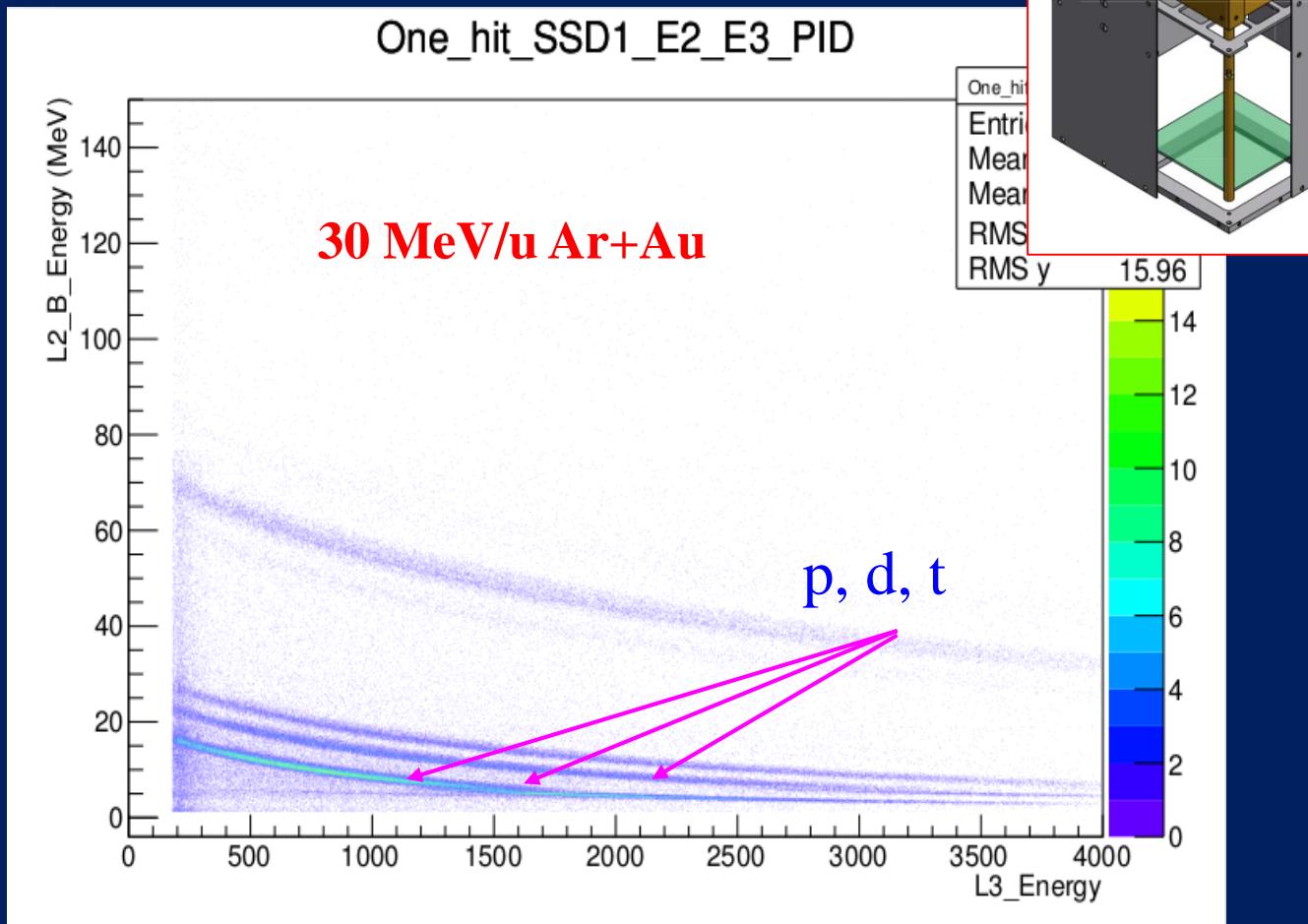
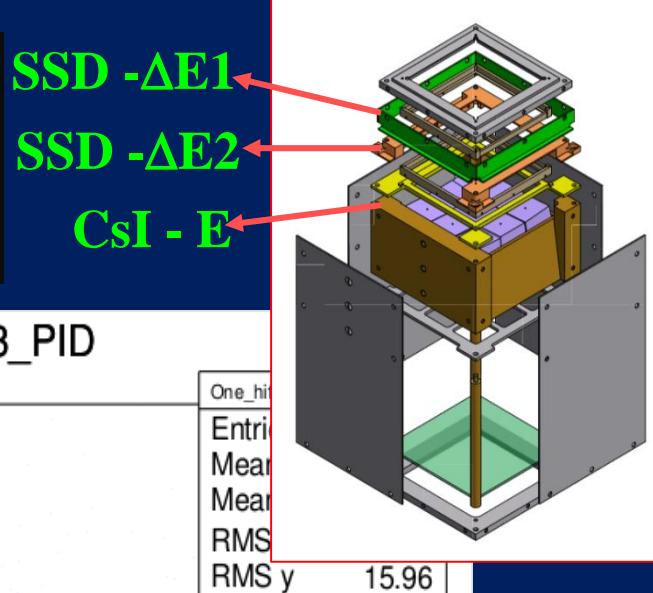


X. L Wei. Et al., Nucl. Engin. Tech. 2019

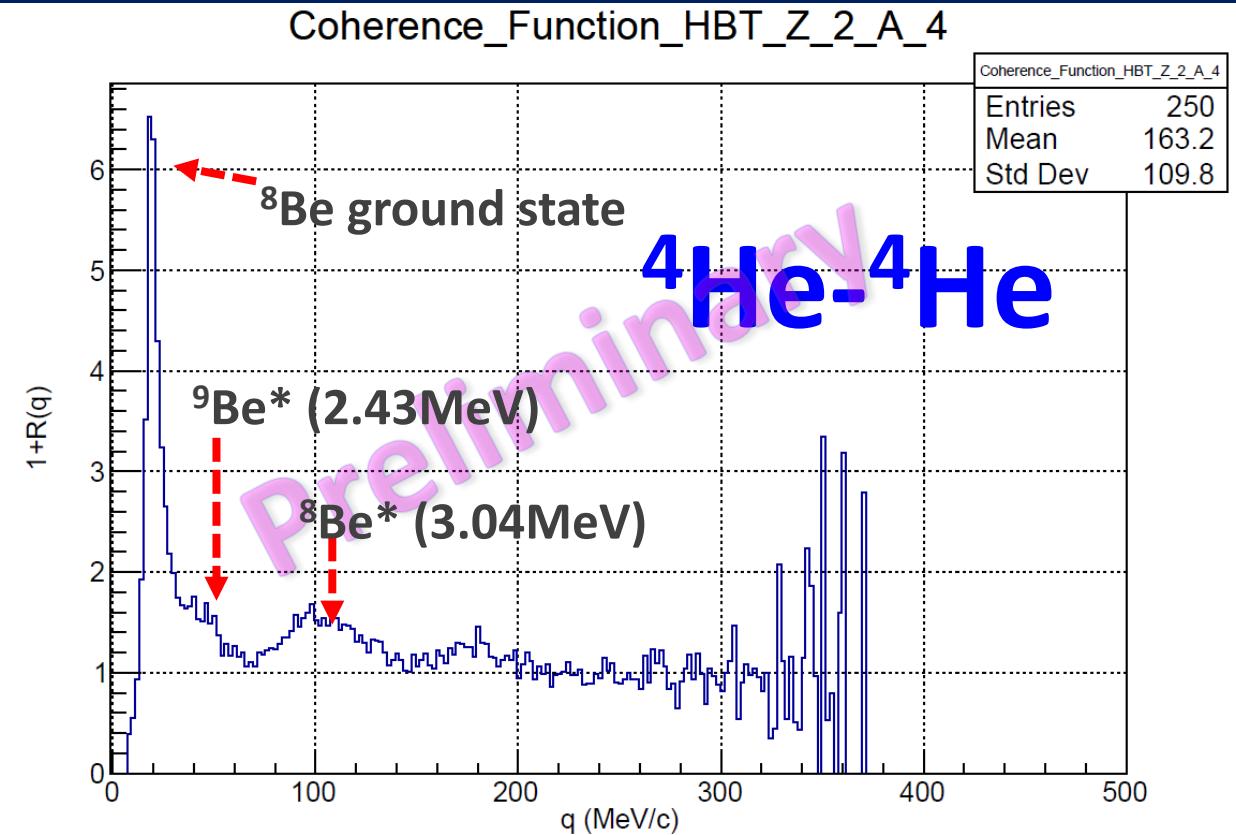
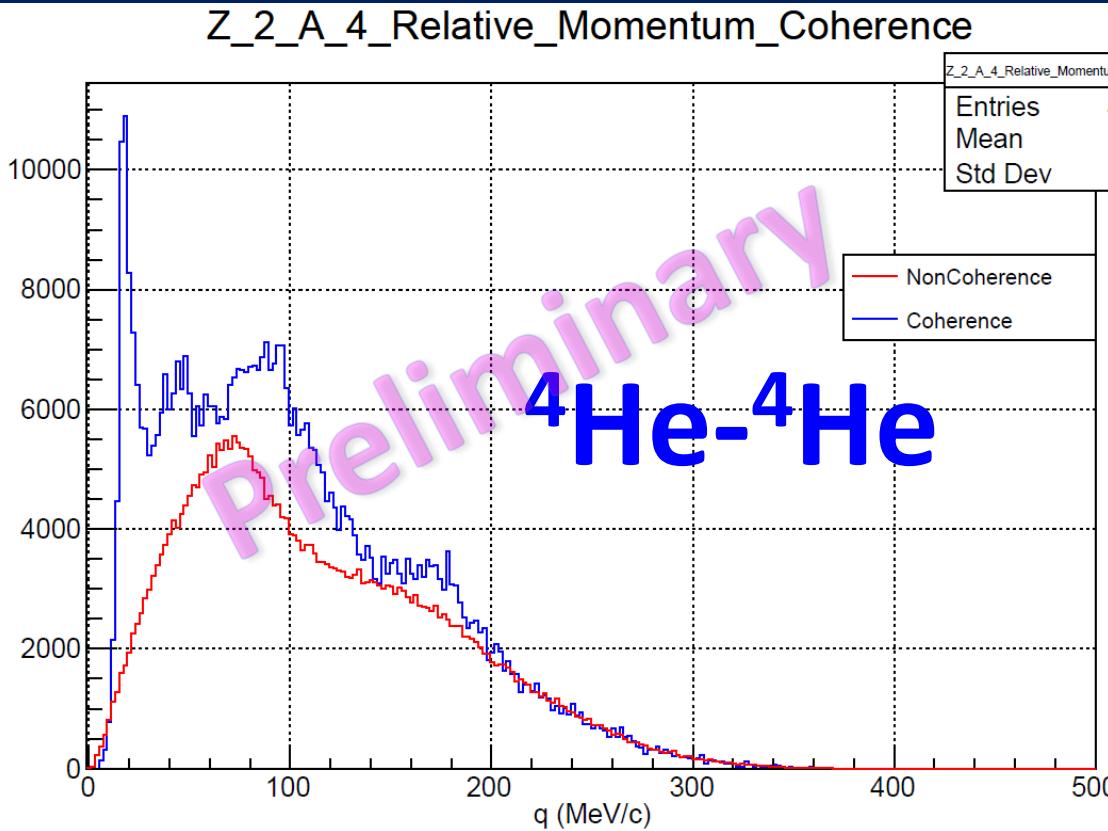


Performance of the Silicon Strip Telescopes

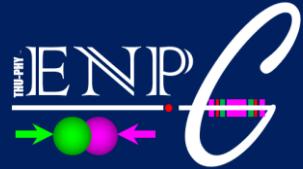
Telescope: SSD+SSD+CsI
 Sensitive area: $64 \times 64 \text{ mm}^3$
 Stripe width: 2mm
 CsI granularity: $23 \times 23 \times 50 \text{ mm}^3$



Preliminary Correlation function for α - α pair



Physical output of phase 1 experiment is expected in near future!



Outline

1 Introduction: Nuclear Symmetry Energy from HIC

2 Transport of Isospin DOF in HIC

2.1 Isospin Dependent Hierarchy of Particle Emission

2.2 Extraction of $E_{\text{sym}}(\rho)$

2.3 HIRA^{TU}: Isospin chronology study

3 Future: Isovector orientation effect of deuteron-induced reaction

4 Summary



4. Summary

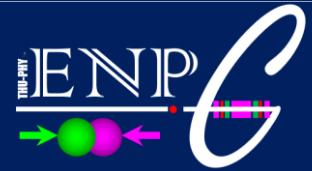
Wealthy information of the transport of **isospin** degree of freedom and $E_{\text{sym}}(\rho)$ is contained in **heavy ion collisions**.

- 1) The isospin-dependent **emission hierarchy** of light charged particles has been observed, showing neutron-rich LCPs are emitted earlier.
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Isospin **chronology** using HBT method is expected with **HIRA^{TU}**.
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Acknowledgements

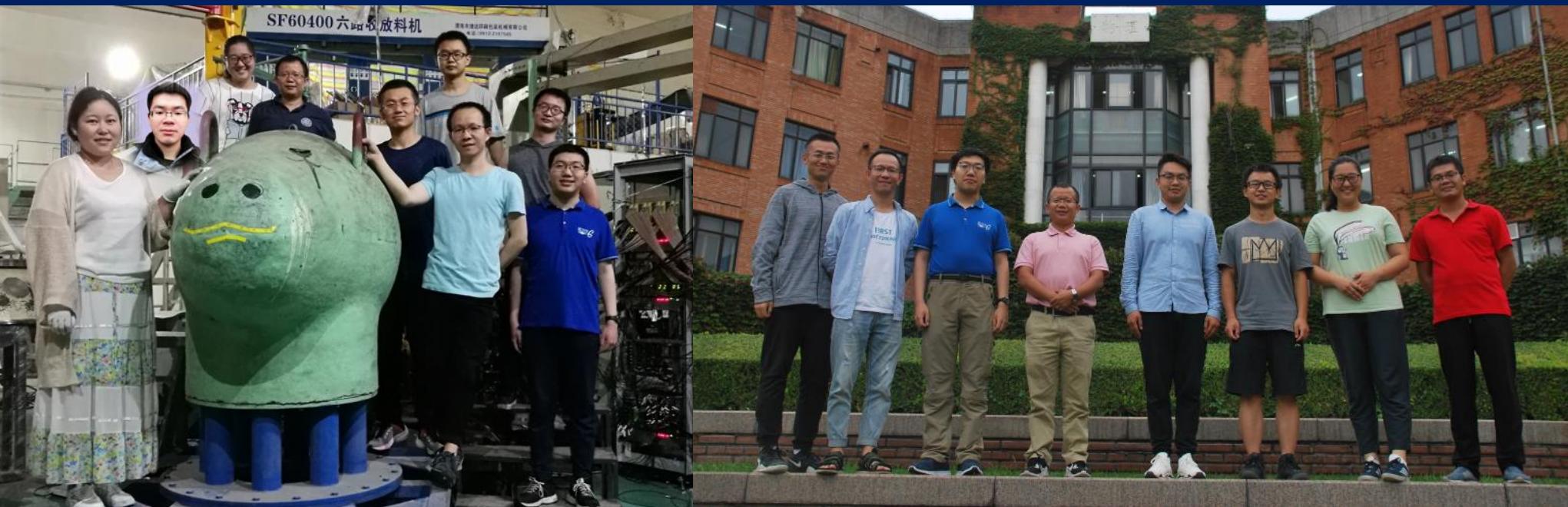


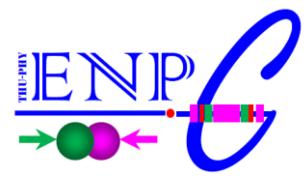
Experimental Nuclear Physics Group (ENPG)

L. M. Lv, Y. J. Wang, F. H. Guan, Q. H. Wu, X. Y. Diao, Z. Qin, Y. H. Qin, D. Guo
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IMP: L. M. Duan's, J. D. Wang's, **HNU:** C. W. Ma's, **SINAP:** H. W. Wang's and **CEE**
Collaboration.....

AYNU: J. L. Tian, **GXNU:** L. Ou, **CIAE:** Y. X. Zhang, **IMP:** G. C. Yong...





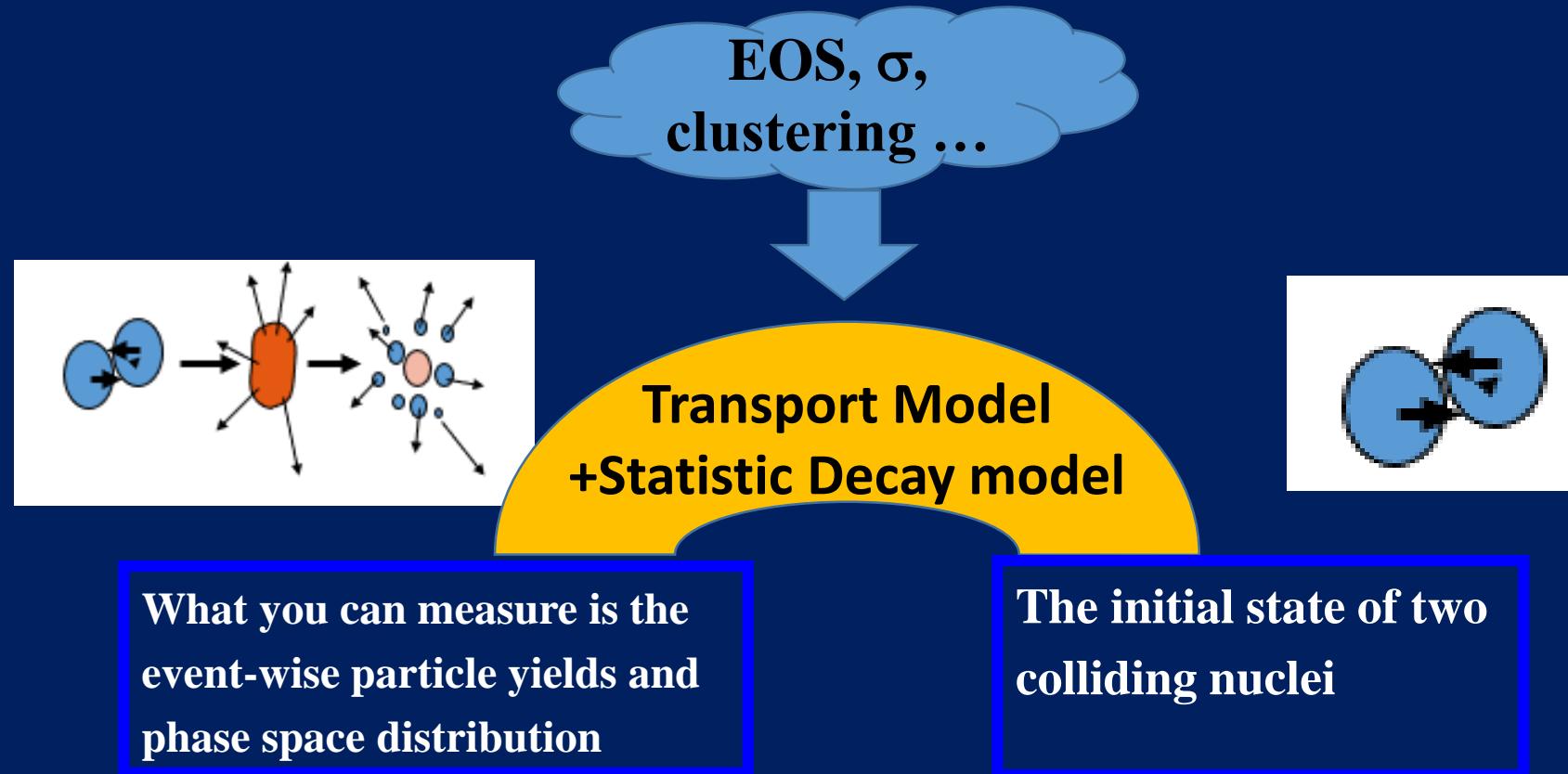
Backup Slides



3 Future: Isovector orientation of d-induced reaction as a probe of $E_{\text{sym}}(\rho)$?

Caution: $E_{\text{sym}}(\rho)$ is not the only unknown factor!

- Isospin diffusion
(MSU ...)
- Isospin scaling and isospin fractionation
(MSU...)
- n/p ratio (MSU ...)
- N/Z of the emitted fragments (LNS, TAMU, MSU, HIRFL ...)
- GMR strength
(ND ...)
-

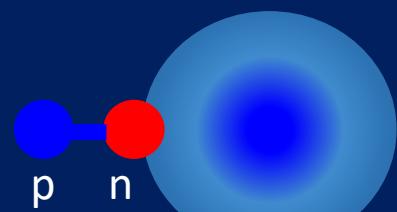


Can we find a sensitive and clean probe in direct reaction: deuteron scattering

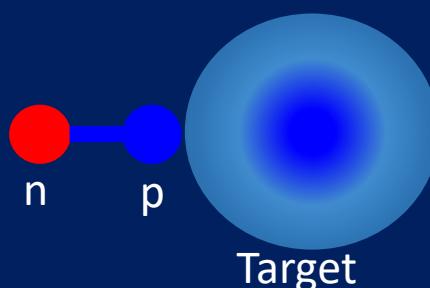
Polarization Effect in d-induced reaction

- Oppenheimer proposed first
- J. R. Oppenheimer et al., Phys. Rev. 48, 500 (1935)
- E. O. Lawrence et al., Phys. Rev. 48, 493(1935)

Favored



Un-favored



Coulomb polarization
(Reorientation)

The Transmutation Functions for Some Cases of Deuteron-Induced Radioactivity¹

ERNEST O. LAWRENCE, EDWIN McMILLAN AND R. L. THORNTON, *Radiation Laboratory, Department of Physics, University of California, Berkeley*

(Received July 1, 1935)

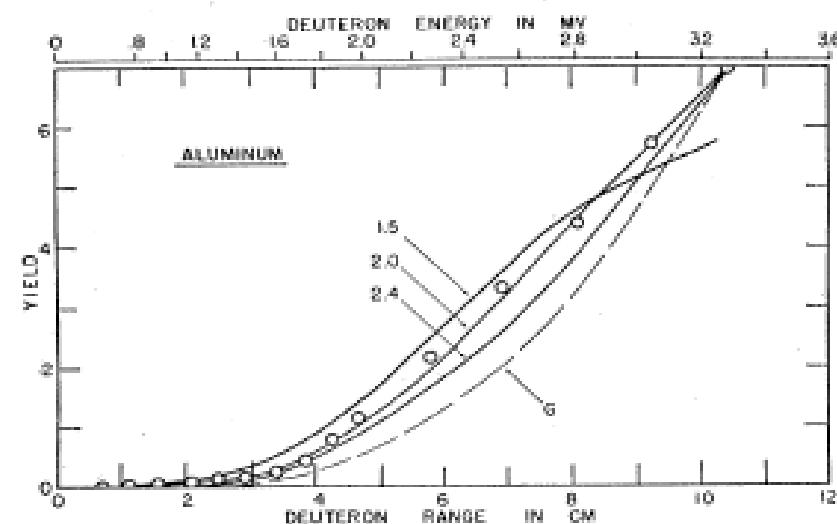


FIG. 2. Differential excitation curve of the radioactivity induced in aluminum ($Z = 13$) by deuteron bombardment. Circles, experimental points. Solid lines, Oppenheimer-Phillips functions with the values of I given by the numbers, in MV. Dashed line, Gamow function.

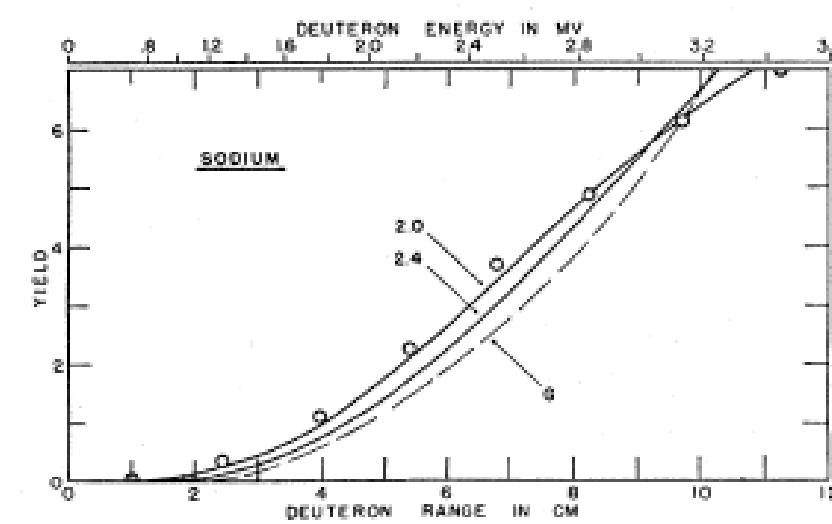
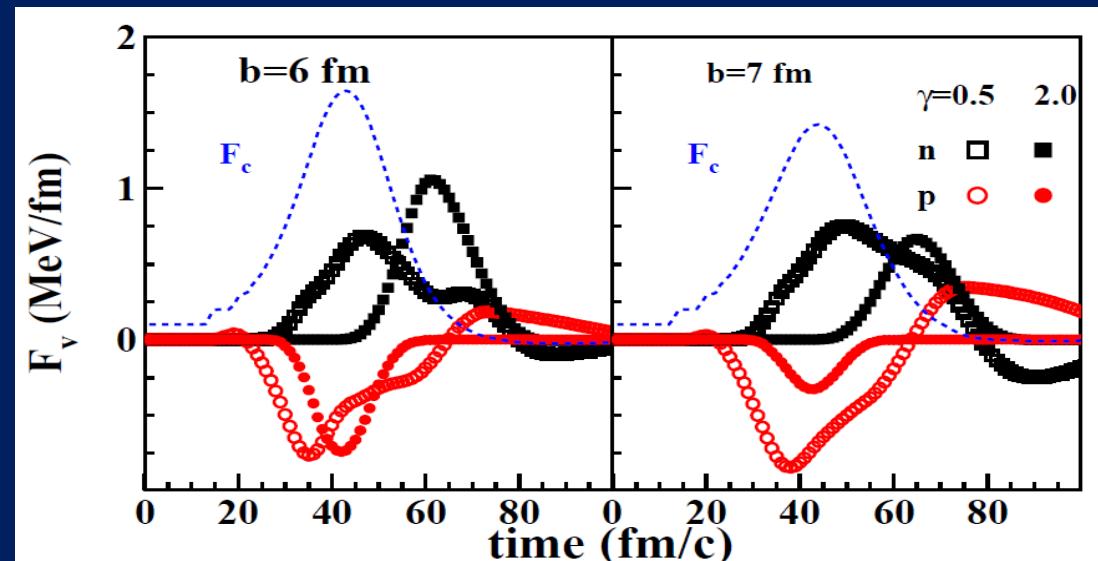
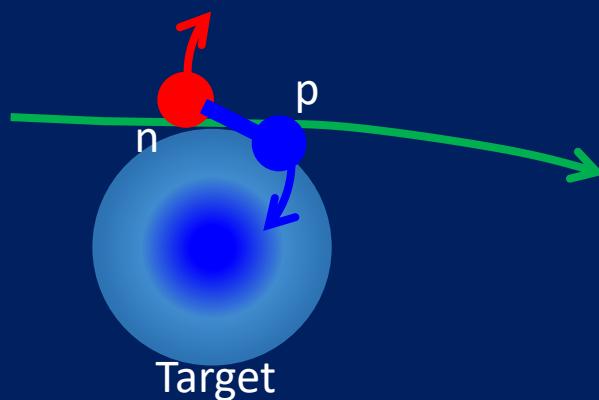


FIG. 3. Differential excitation curve of the sodium radioactivity ($Z = 11$). Notation same as in Fig. 2. The ordinate of the highest energy experimental point is probably too low.

A nature question arises now.....

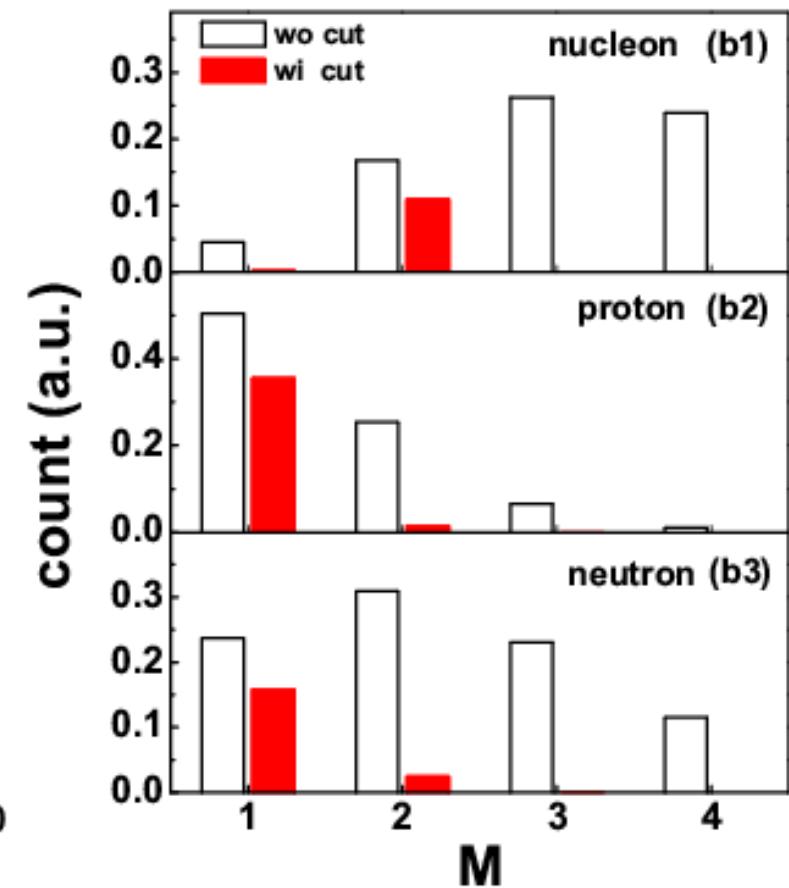
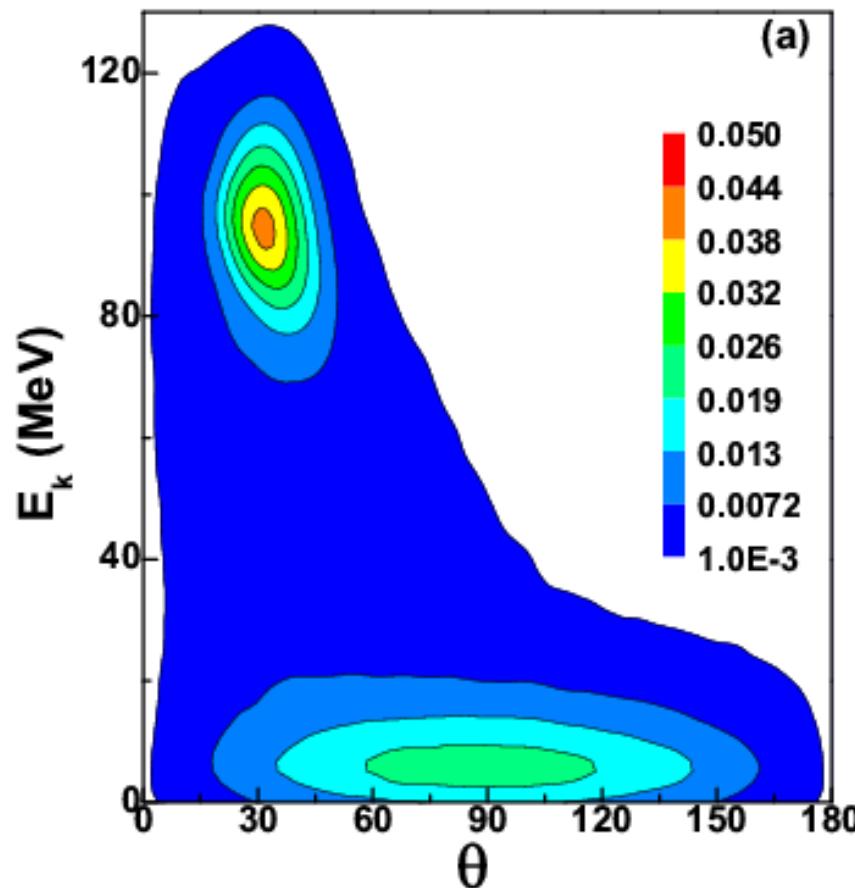
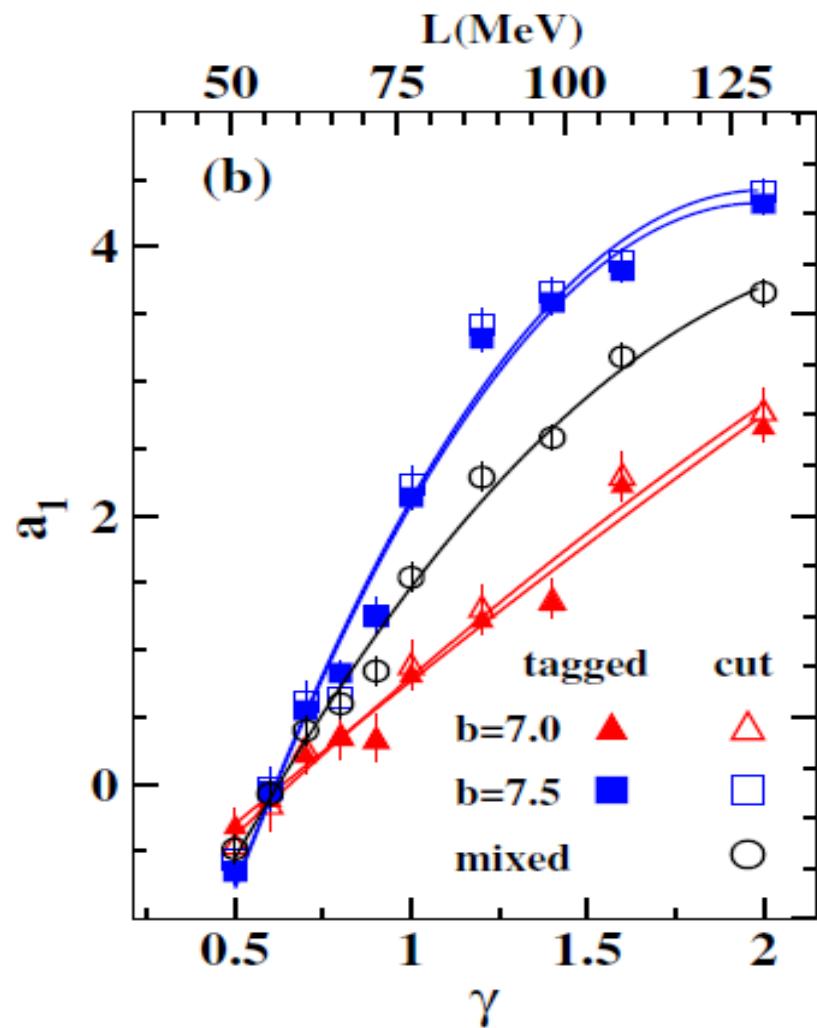
- Coulomb force, 1 for proton and 0 for neutron, leads to *Coulomb polarization* (reorientation), characterized by **the moving away of proton**.
- Isovector force, attractive for proton and repulsive for neutron, shall leads to *isovector reorientation*, characterized by **the modification of the direction of the relative motion**.



Isovector force act on p and n like a torque
→ Reorientation effect

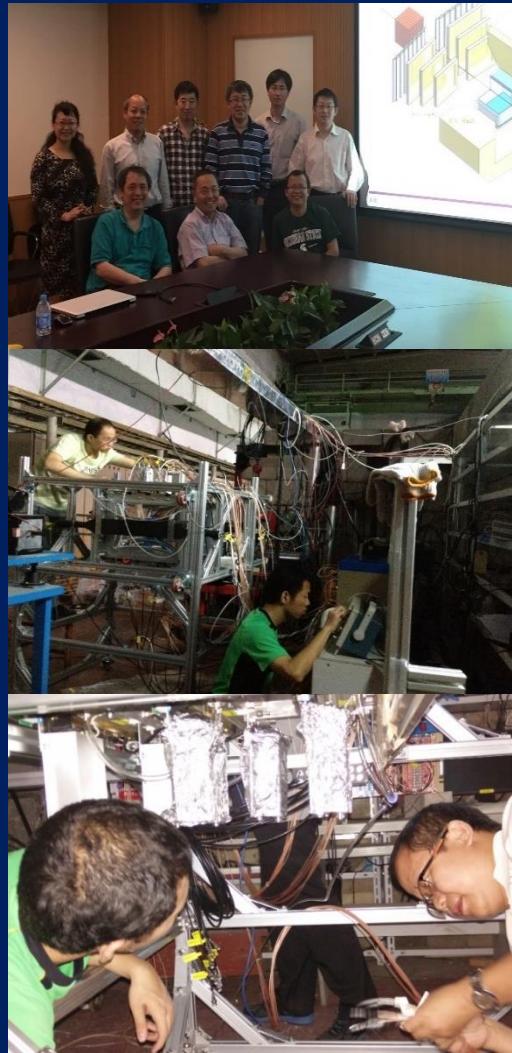
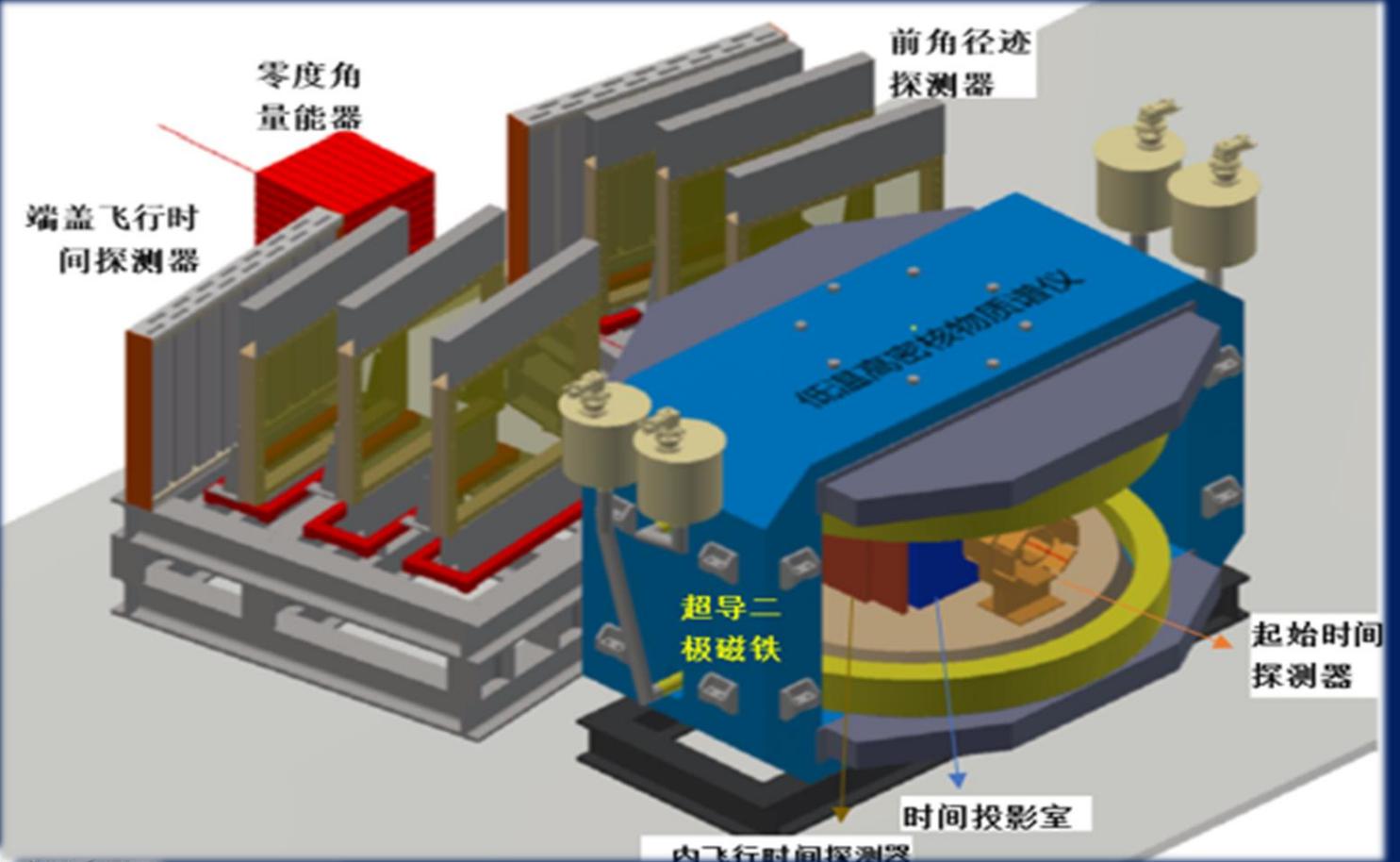
- If this effect is detectable, it should be sensitive to the isovector potential (\rightarrow symmetry energy!) at low densities ($< 0.5 \rho_0$)

Sensitivity of the dependence of the angular distribution on $E_{\text{sym}}(\rho)$



- A new way to study the $E_{\text{sym}}(\rho)$: Direct reaction may be used as a new method. It is equivalent to measuring the n/p global optic potential difference.

CEE: A spectrometer for studies on cold and dense nuclear matter



Conceptual Design:

Liming Lü, Han Yi, ZGX, Ming Shao, Song Zhang, Guoqing Xiao and Nu Xu.,
Science China, Phys. Mech. & Astro. 60, 012021 (2017)



4. Summary

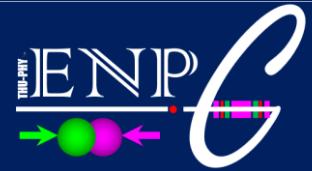
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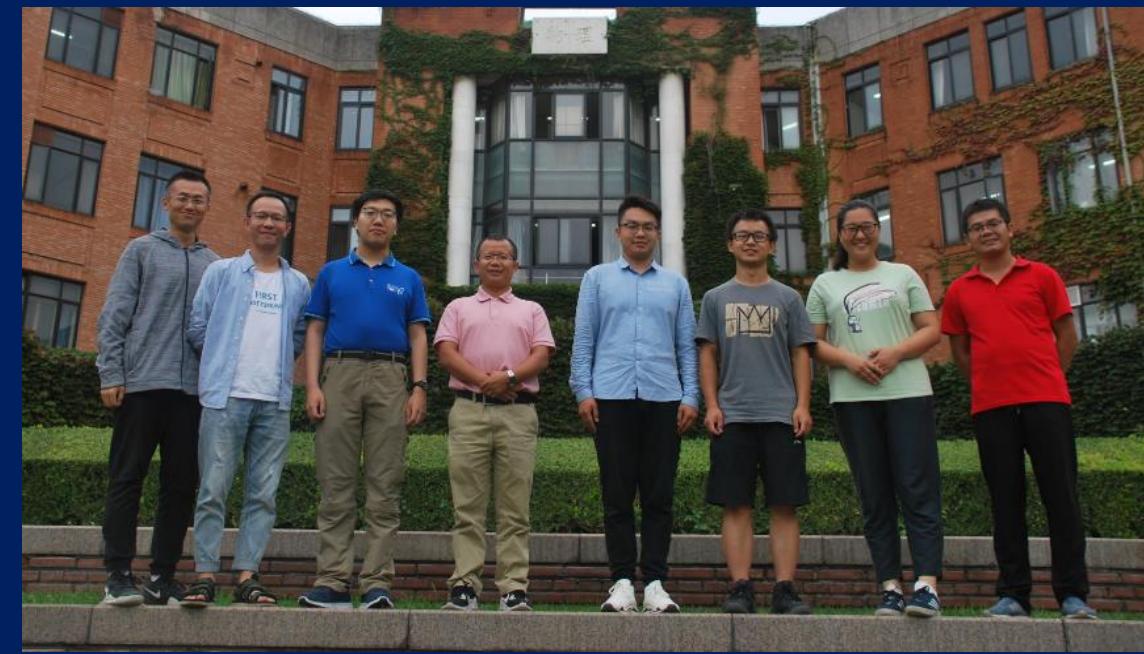


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Collaboration.....

AYNU: J. L. Tian, **GXNU:** L. Ou, **CIAE:** Y. X. Zhang, **IMP:** G. C. Yong



Very Brief Rev. of $E_{\text{sym}}(\rho)$ at $\rho < \rho_0$ in HIC

40 18 + 197 79

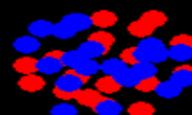
E = 1164.00000

b = 1.00000

t = 0

Blue and Green are neutrons!

nruns : 1

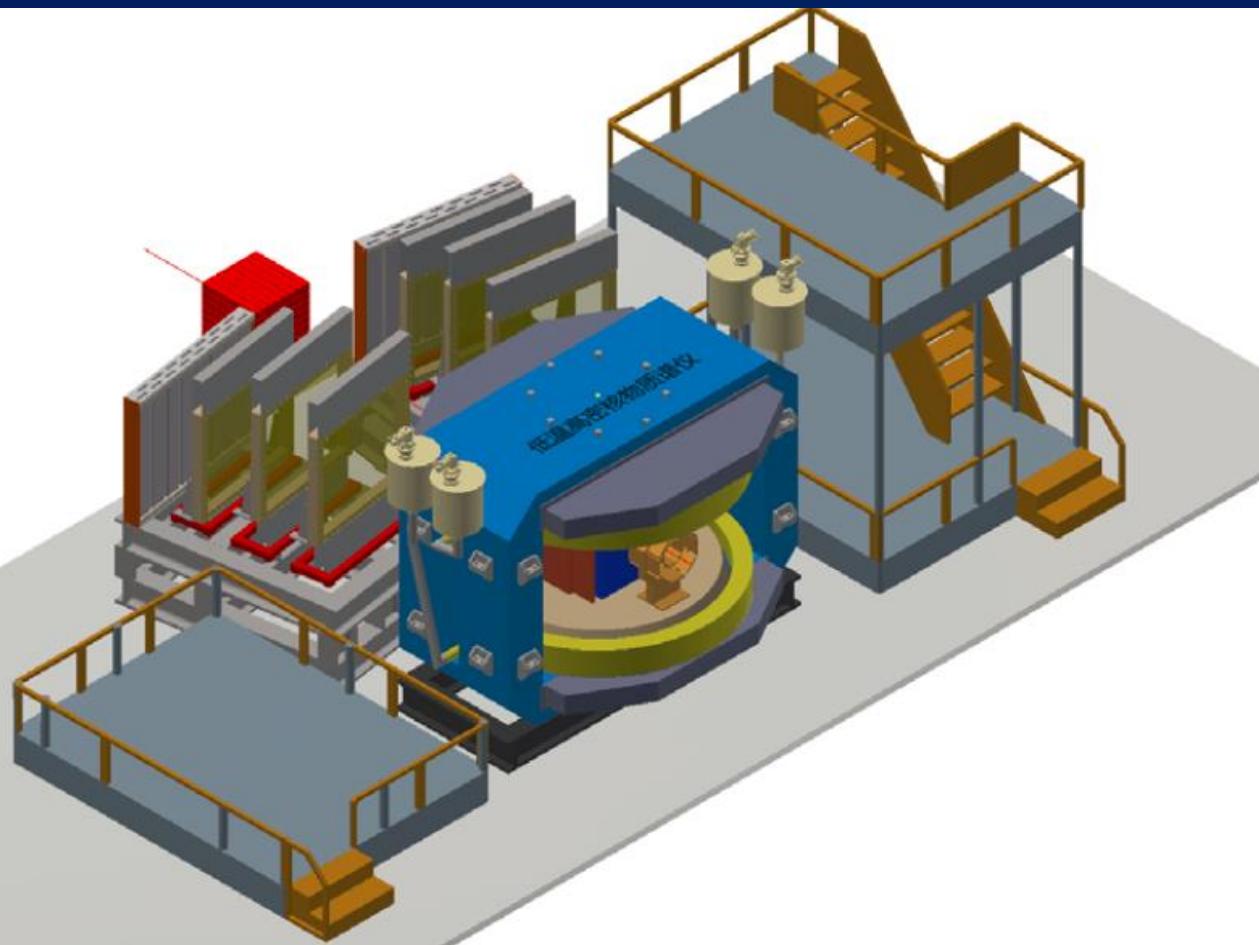


Equation of State of Asymmetric Nuclear Matter and Collisions of Neutron-Rich Nuclei

Bao-An Li,^{1,*} C. M. Ko,^{1,†} and Zhongzhou Ren^{2,‡}

未来计划 1： CEE的立项建造 --- HIAF 和 HIRFL 能区重离子反应

主要研究目标：2~3 倍饱和密度处核物质性质研究



1) TPC+MWDC 径迹重建模拟和探测器硬件研发

2) 该能区新物理/探针寻找

→ Λ 产额与核物质状态方程

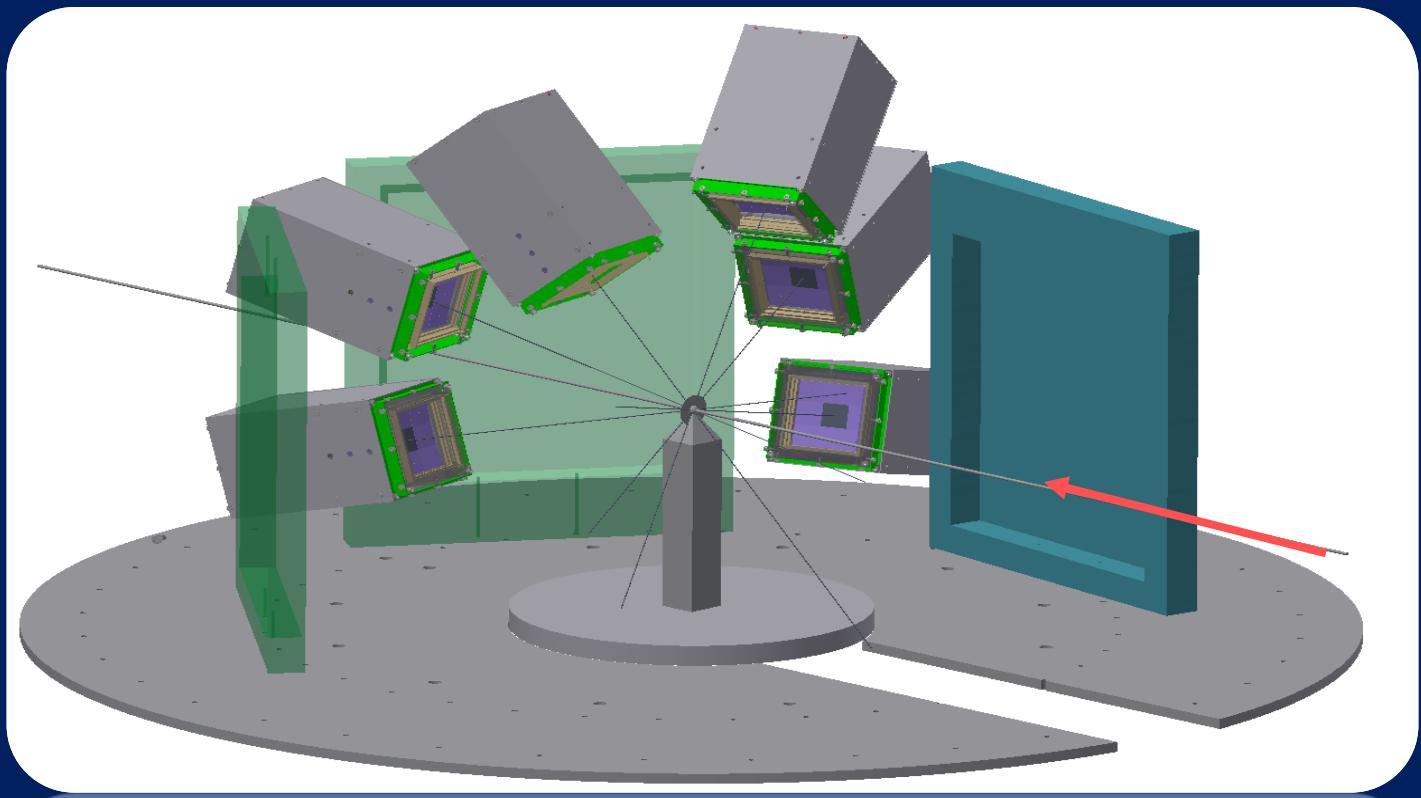
→ K^0/K^+ 比值与 $3\rho_0$ 处对称能

未来计划2： HIRATU：重离子研究阵列 ---- 清华

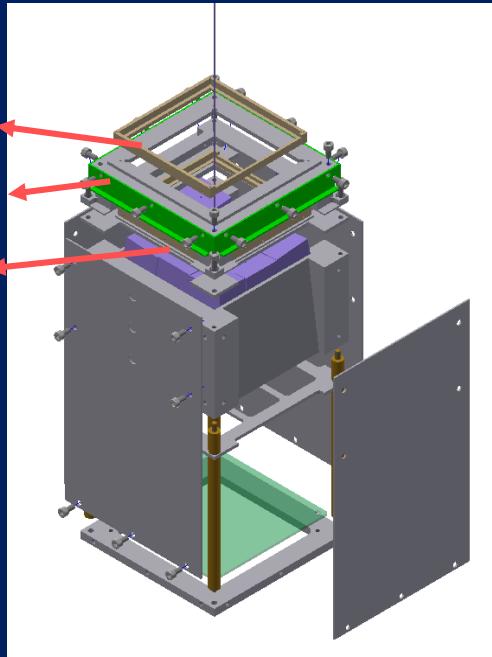
- Heavy Ion Research Array at Tsinghua University (**HIRATU**)

主要研究目标：

颈部发射的同位旋效应；快裂变动力学性质研究
→ 低密区丰中子物质性质研究



SSD - ΔE 1
SSD - ΔE 2
CsI - E

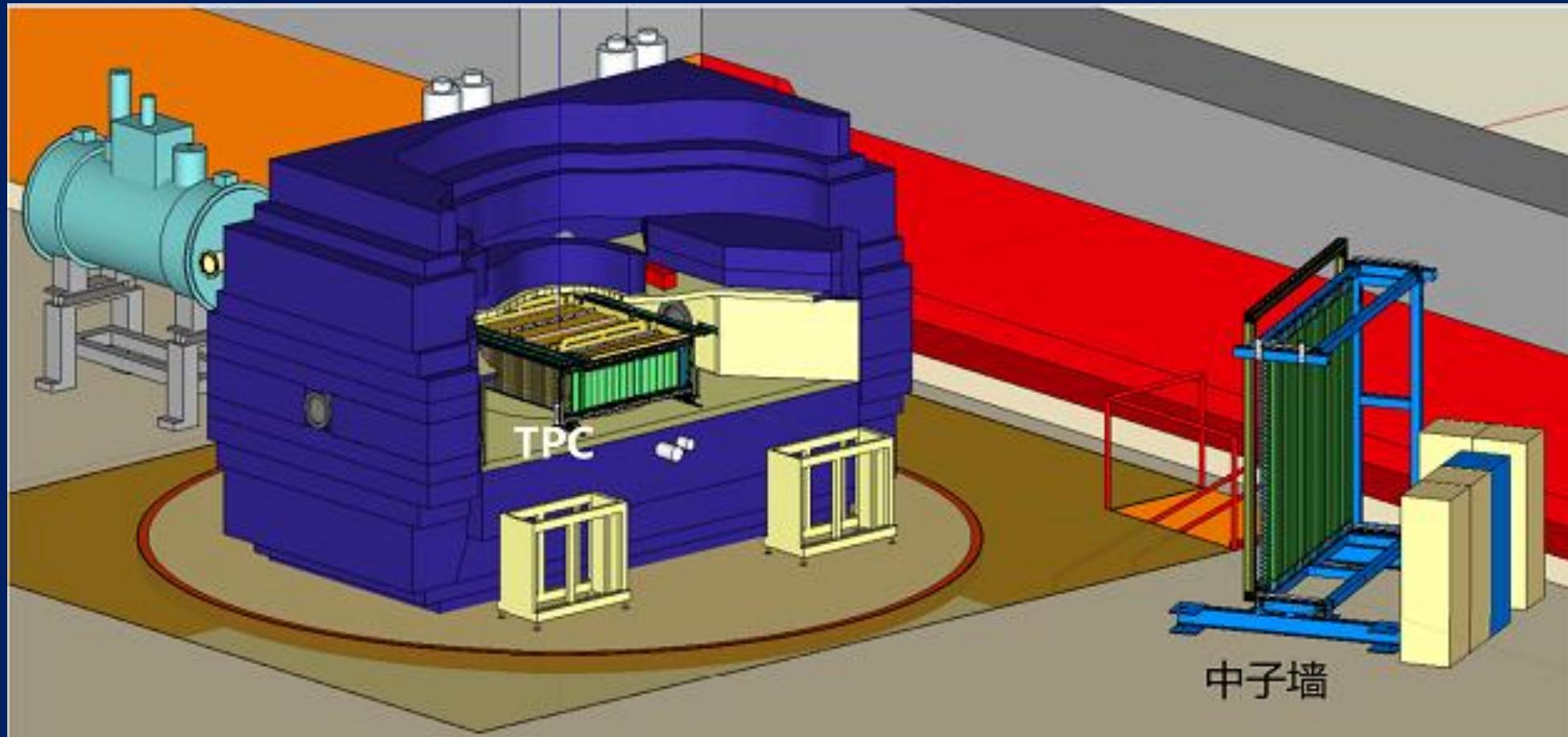


HIRA型的望远镜阵列和PPAC阵列构成

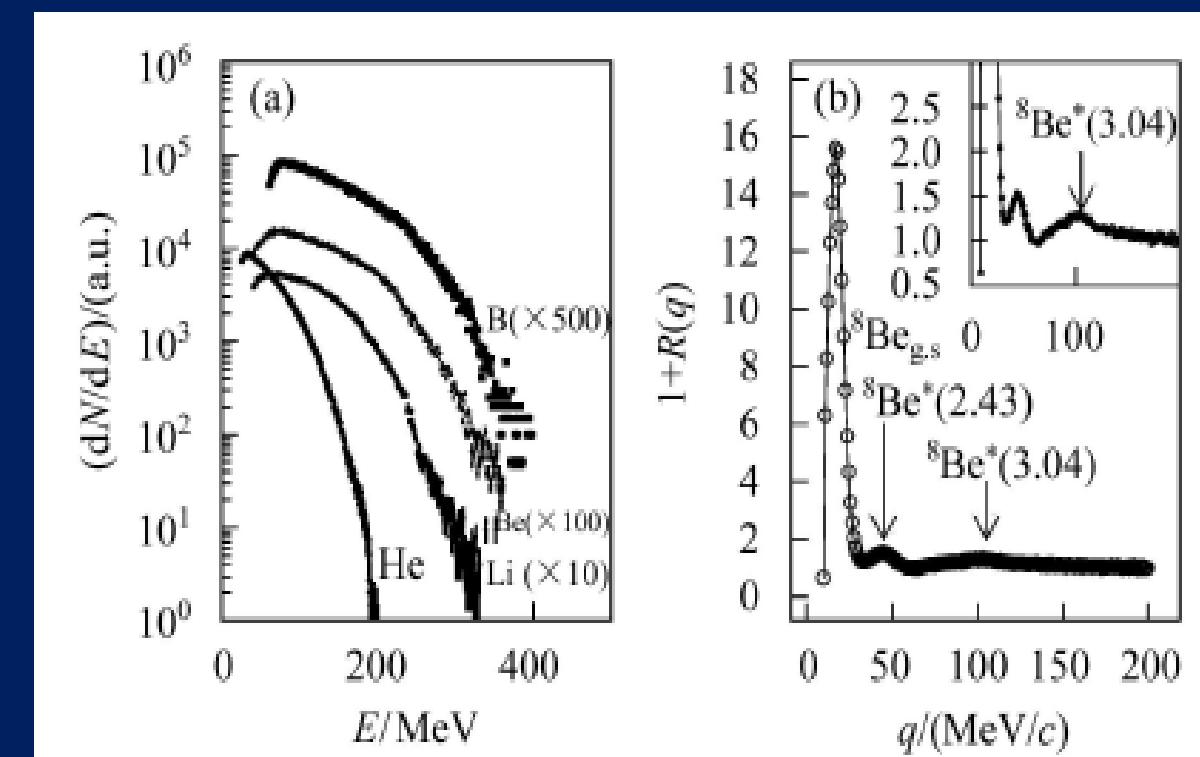
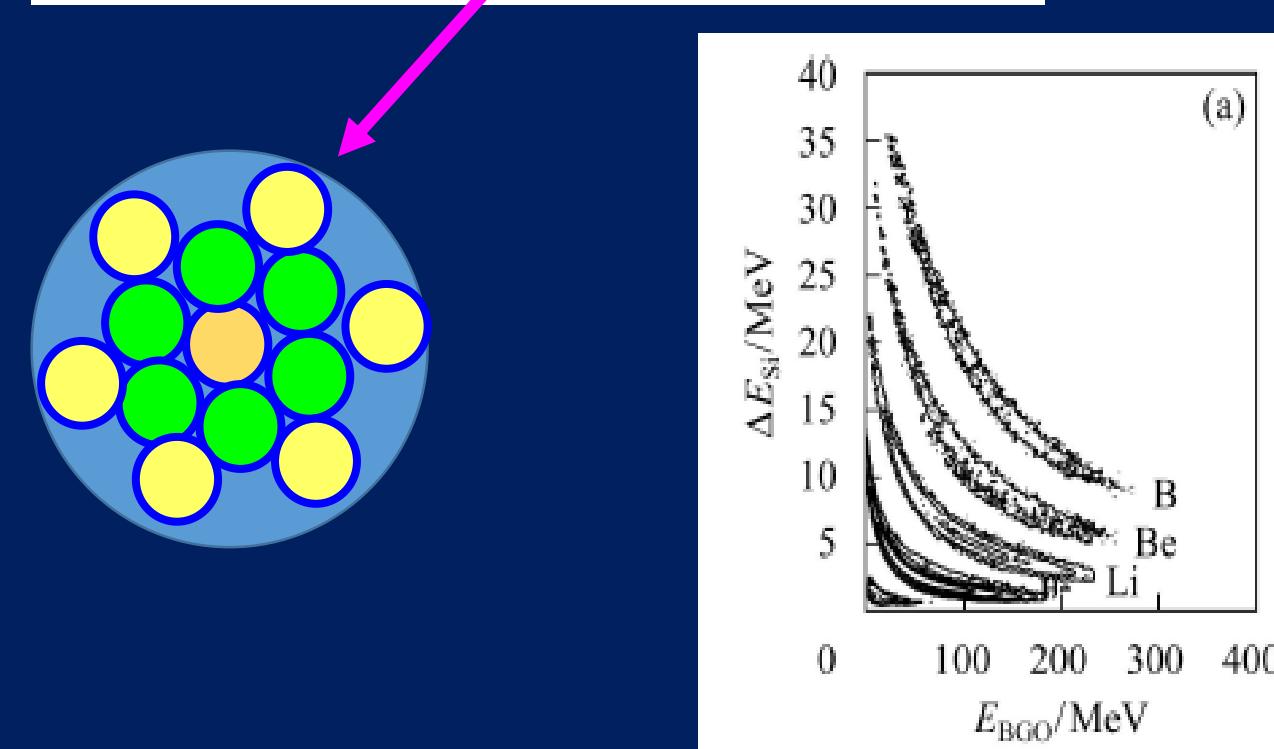
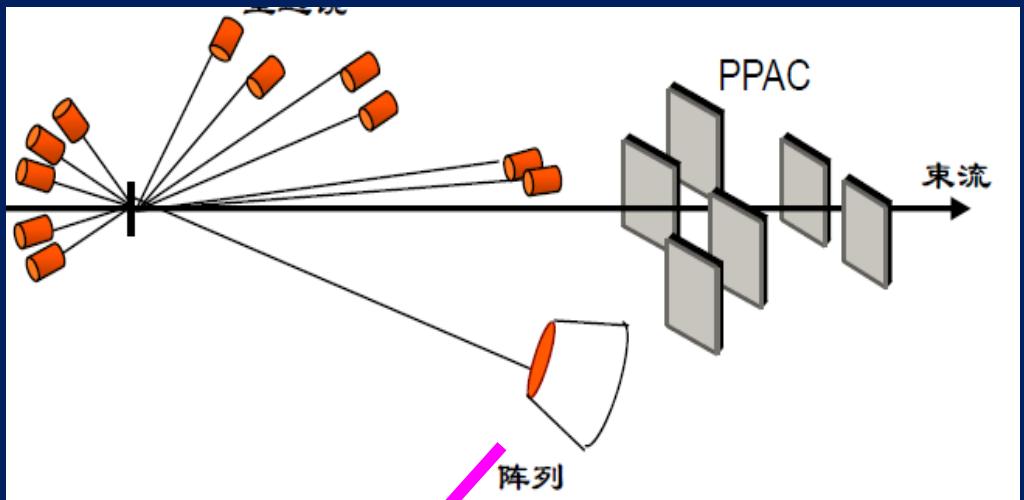
未来计划 3：极化氘核的破裂反应精确测量

主要研究目标：

测量极化氘核的破裂反应，除了约束对称能（中子、质子与靶核光学势）以外，研究氘核散射中的各类精细效应（与质子关联）。

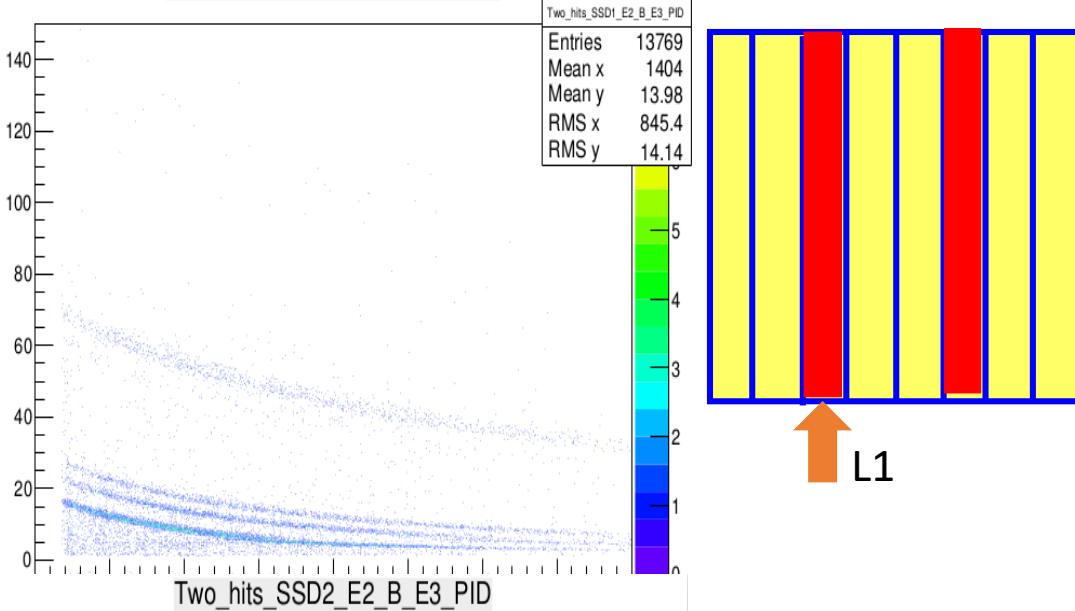


Experimental measurement of Isospin effect on IMF HBT correlation



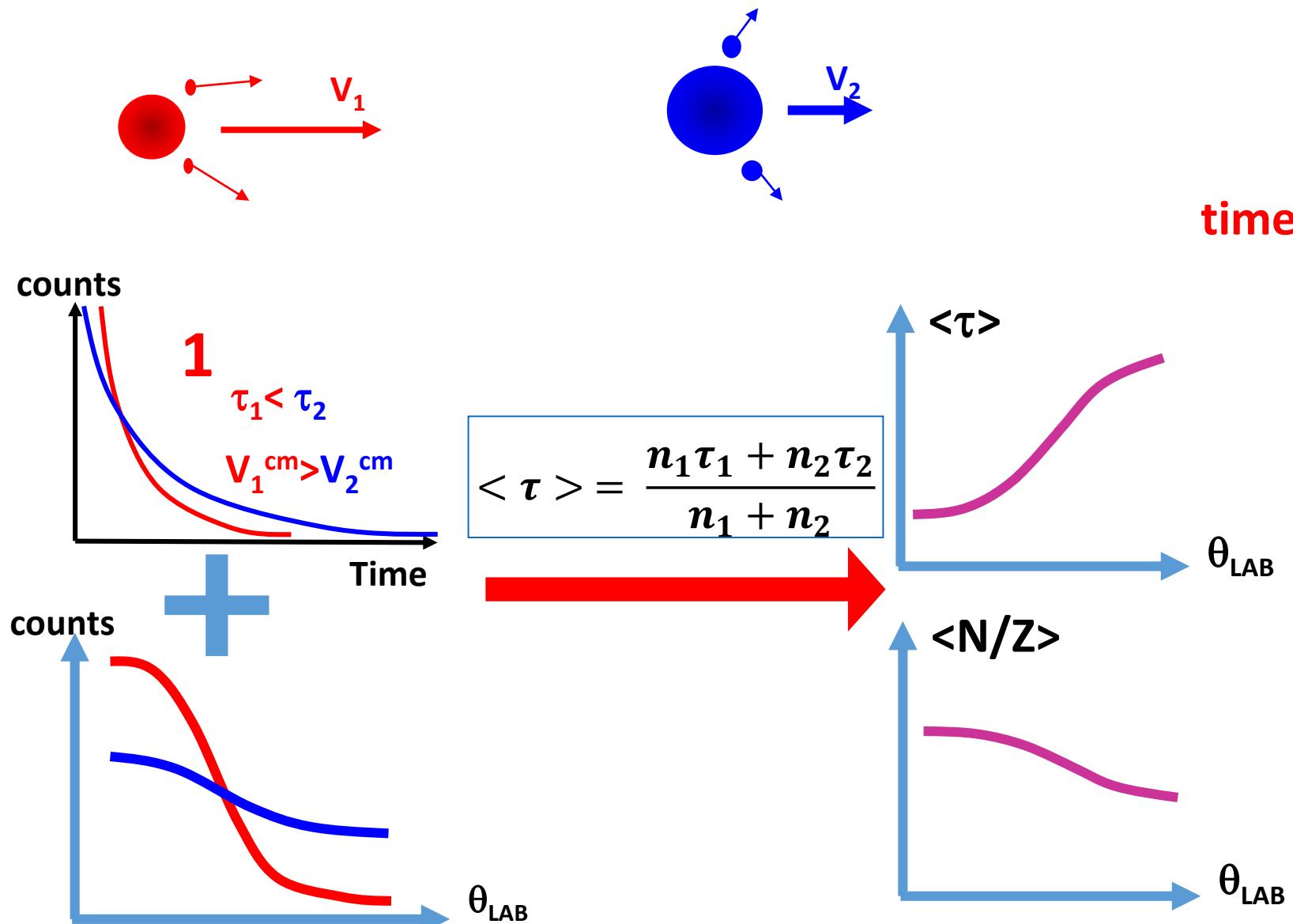
LCP-LCP correlation identified

Two_hits_SSD1_E2_B_E3_PID



Two_hits_SSD1_E2_B_E3_PID

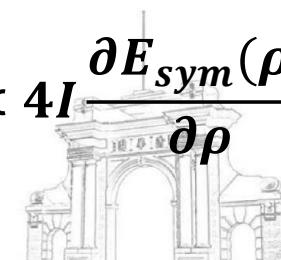
Build a qualitative relation between the angle in lab and the emission time

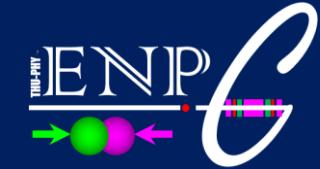


1 Angular distribution in large angular range reflects the time evolution of isospin transport;

2 A stiffer symmetry energy leads to faster isospin drift, thus to more rapidly changing in angular distribution.

$$\begin{aligned} j_{np} &= j_n - j_p \\ &= (D_n^\rho - D_p^\rho) \nabla \rho - (D_n^I - D_p^I) \nabla I \end{aligned}$$

 $D_n^\rho - D_p^\rho \propto 4I \frac{\partial E_{\text{sym}}(\rho)}{\partial \rho}$




What is our Motivations with HIC?

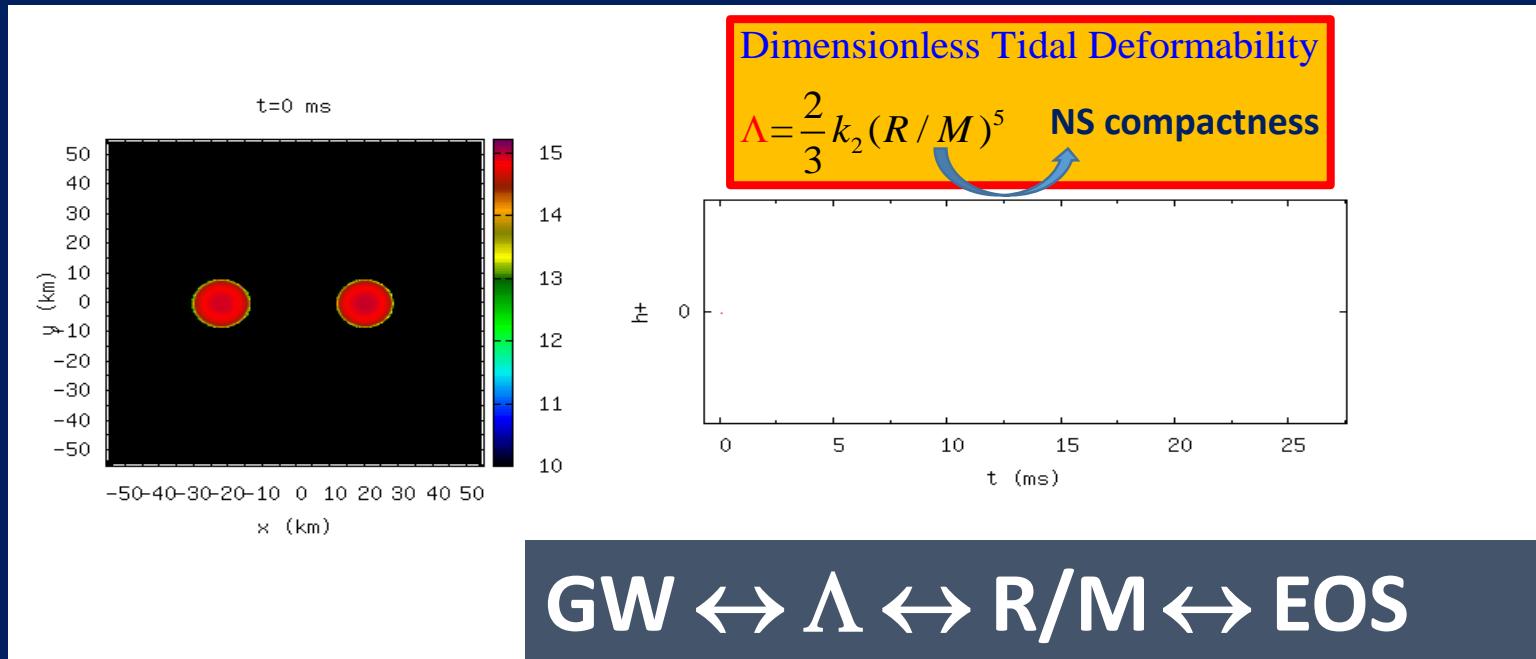
1) Look for new $E_{\text{sym}}(\rho)$ ($\rho < \rho_0$) probes in slow process for the enhanced sensitivity.

- Neck Emission in Fission reactions is characterized by low density and neutron-richness.
- Transport of isospin degree of freedom (IDOF) involving the neck emission helps to identify a probe.

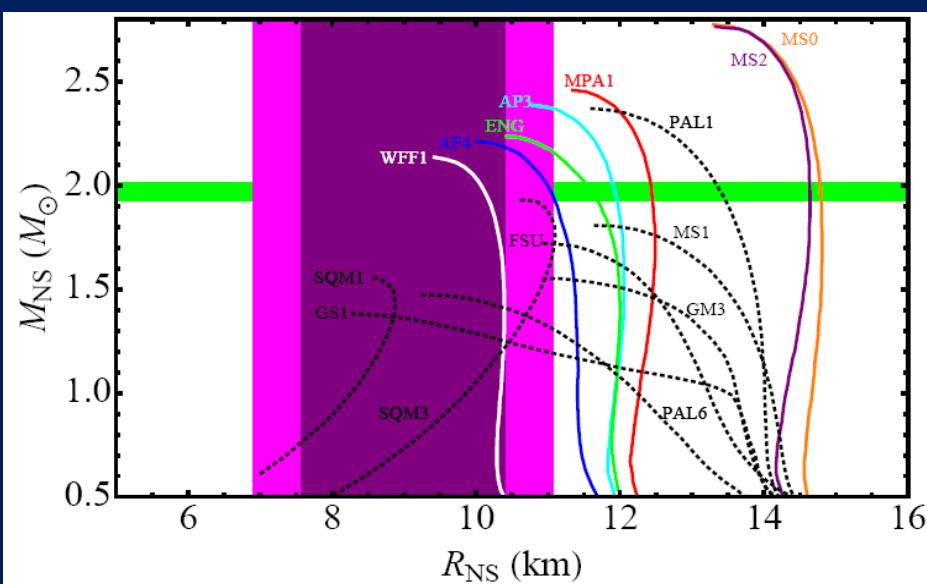
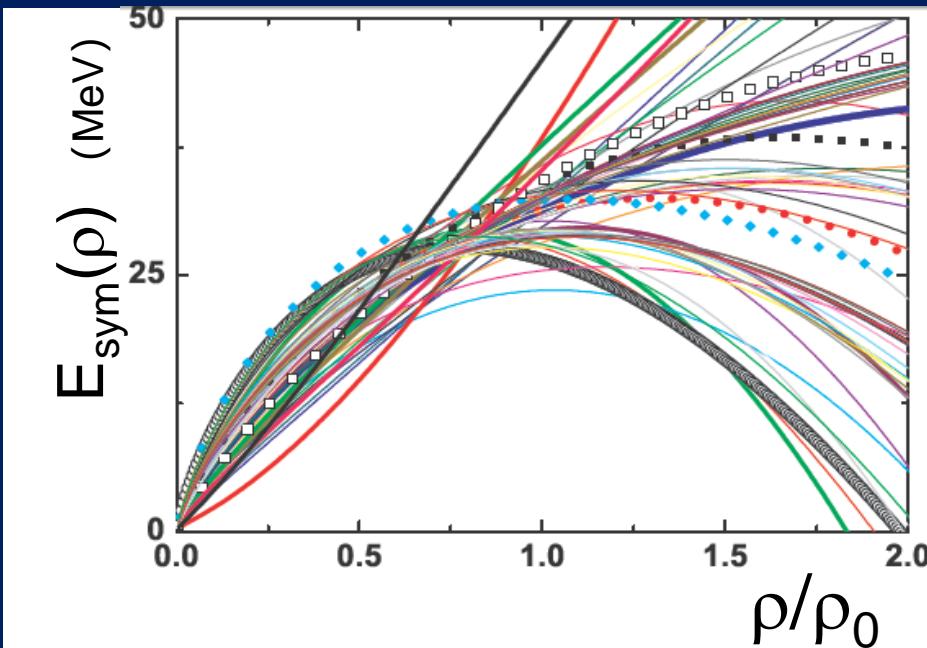
2) To measure quantitatively the time scale of the transport of IDOF.

3) To develop new method to pin down the $E_{\text{sym}}(\rho)$ ($\rho < \rho_0$) .

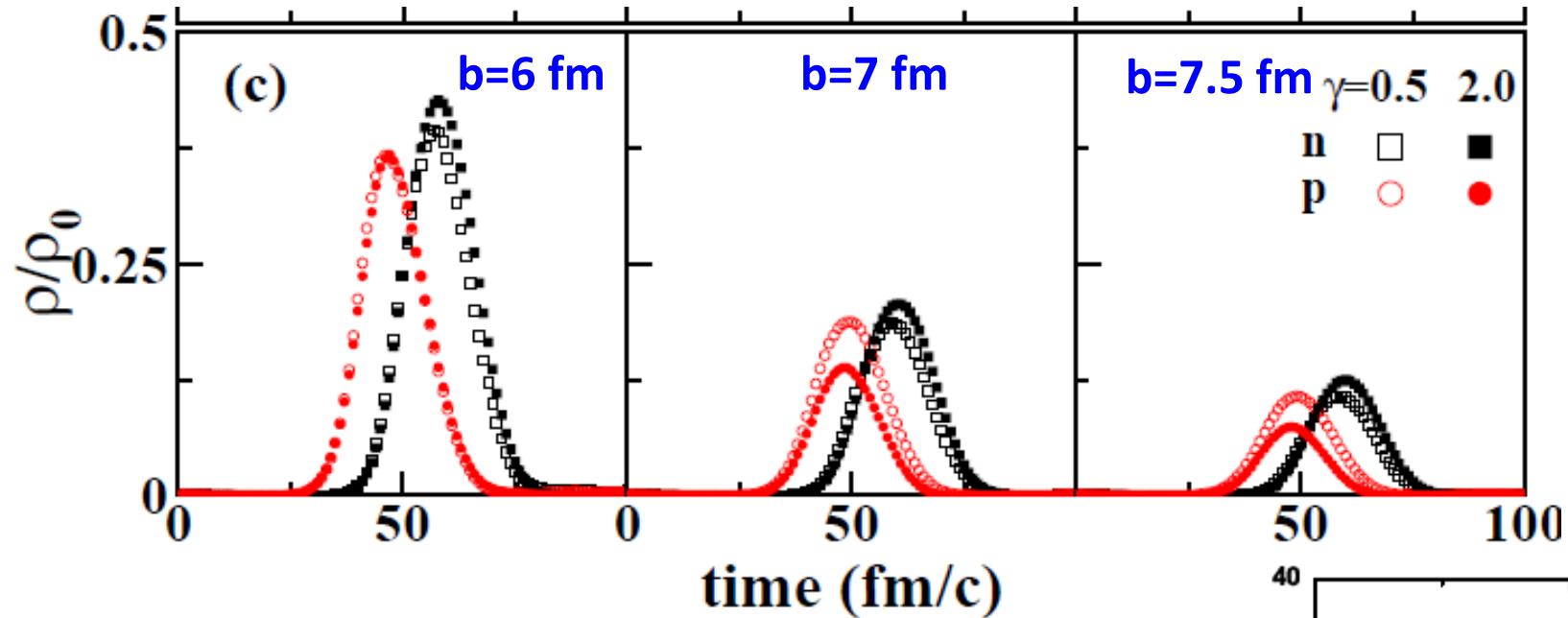
GW170817 与核物质压缩性质（核物态方程）的联系



- 原子的电偶极矩和原子半径的三次方成比例: $\kappa \propto R^3$
- 中子星的四极质量极化度和中子星的半径 5 次方成比例 $\Lambda \propto R^5$
- Ligo对双中子星的轨道频率变化敏感，轨道半径取决于并和过程中引力波导致能量损失的和中子星内部激发过程。
- GW170817 的引力波探测，给出中子星的潮汐极化度限制，故能给出中子星的半径限制。



Density range of sensitivity



- What density region is this observable sensitive on?

Density range $< 0.5 \rho_0$

