

# Quarks and Compact Stars 2019

## Effects of nuclear symmetry energy and equation of state on neutron star properties

Presenter : Fan Ji

Supervisor : Prof. Hong Shen

Collaborators :

Jinniu Hu      Nankai University (China)

Shishao Bao      Shanxi Normal University (China)



2019 BUSAN KOREA



2019.09.26~2019.09.28, Pusan National University, Korea



**Background**



**Model and Method**



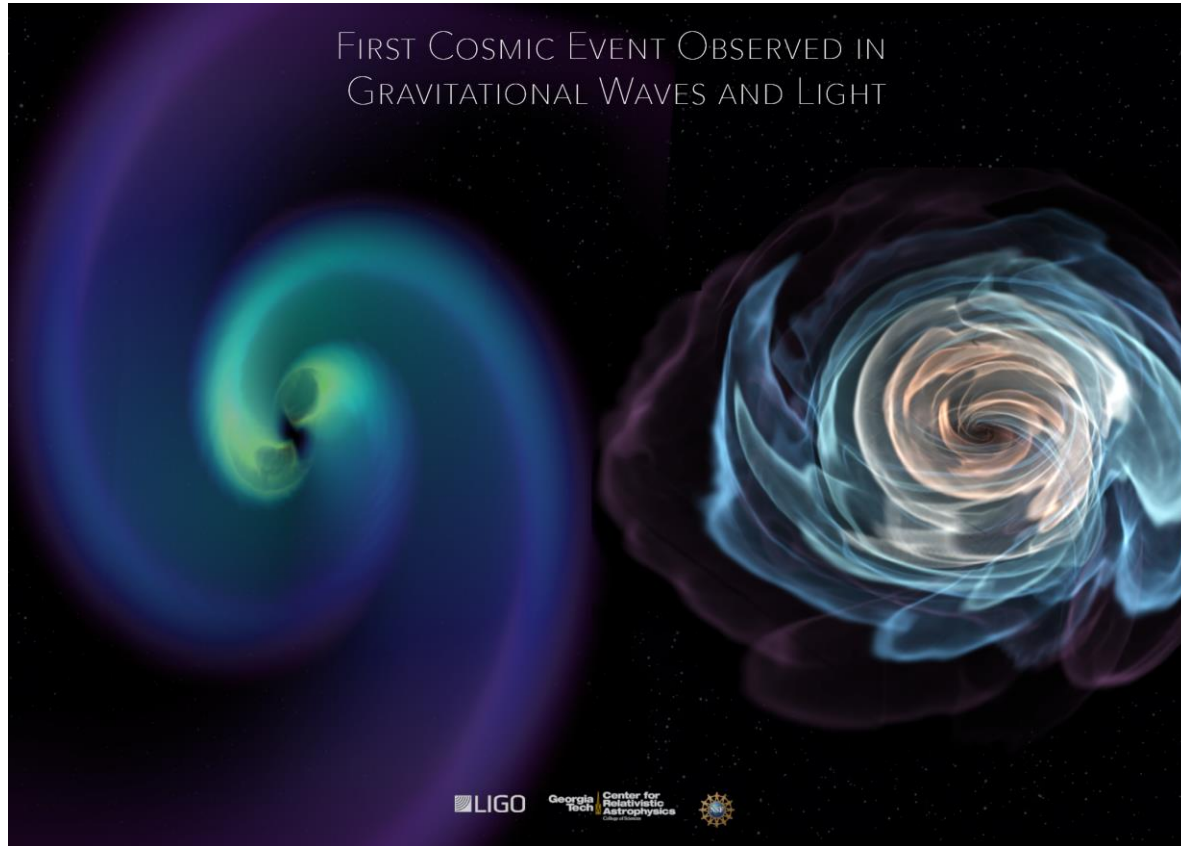
**Results**



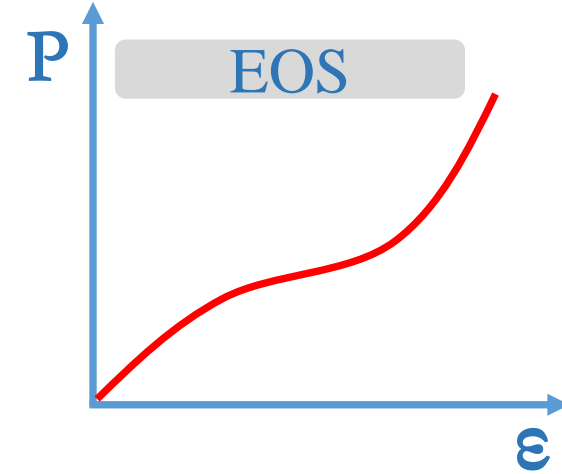
**Conclusions**

# 1 Background

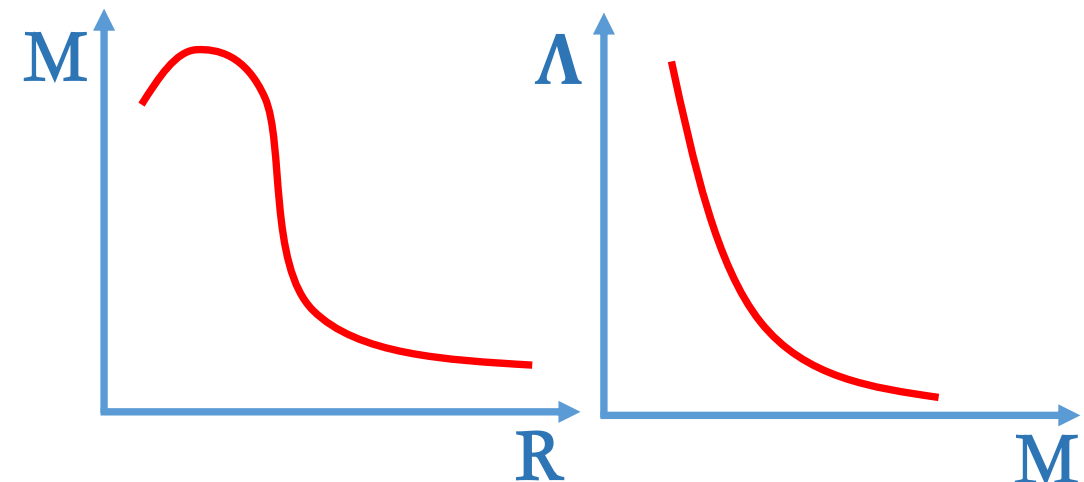
## Binary neutron-star merger



constrain

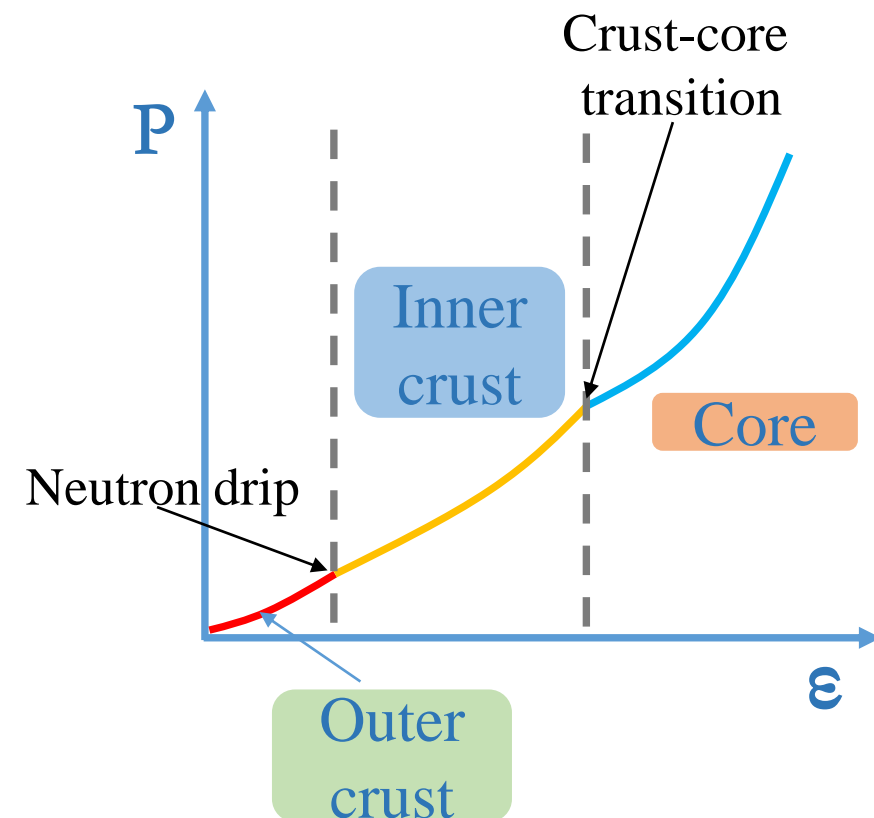
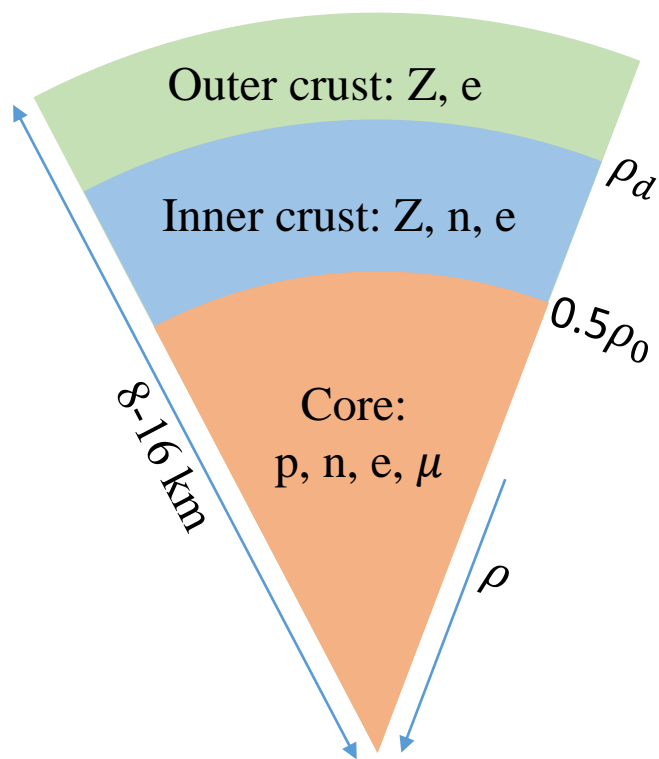
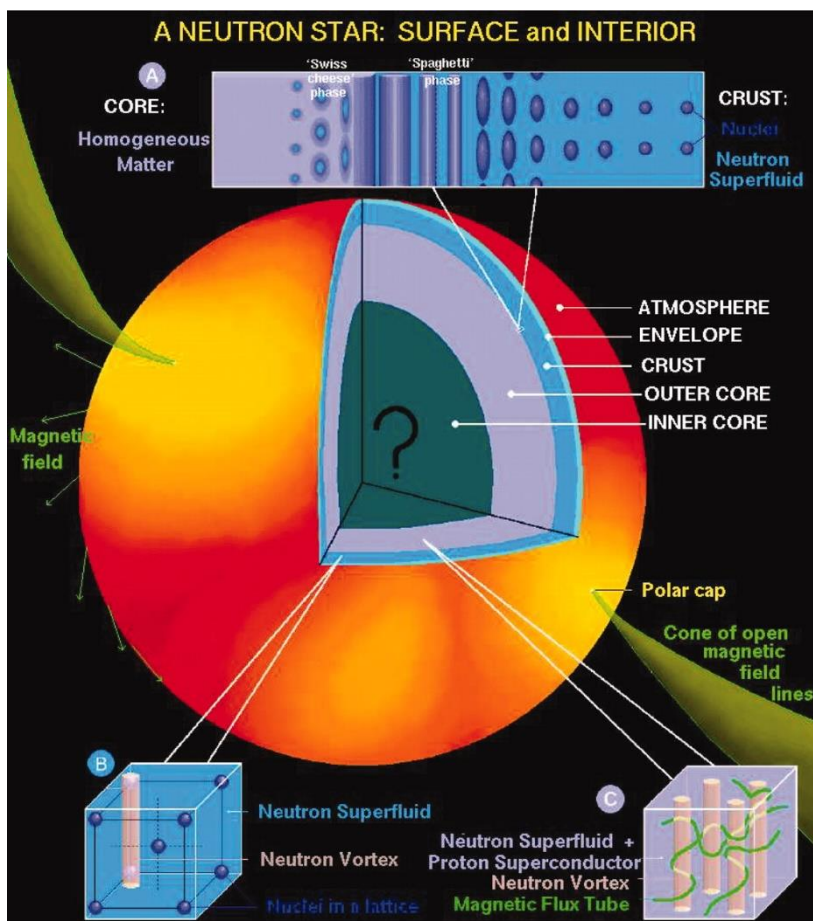


TOV



# Structure of neutron star

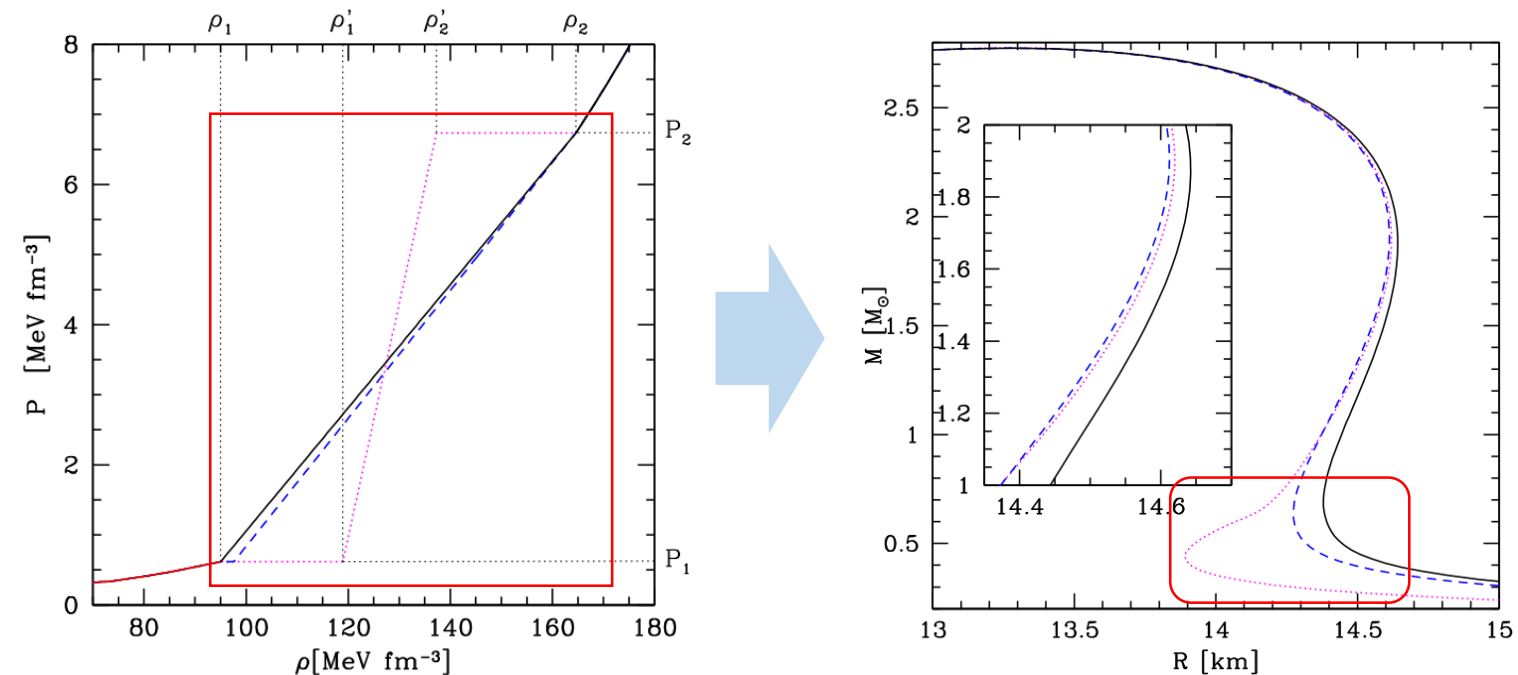
EOS



# 1 Background

## Non-unified EOS

### Matching EOS with different models



M. Fortin, C. Providencia, Ad. R. Raduta, F. Gulminelli, J. L. Zdunik, P. Haensel, and M. Bejger, Phys. Rev. C94, 035804 (2016).

## Unified EOS

### Outer crust EOS: BPS EOS

G. Baym, C. Pethick, and P. Sutherland, Astrophys. J.170, 299 (1971).



### Inner crust EOS: TM1 models

S. S. Bao and H. Shen, Phys. Rev. C 91, 015807 (2015).



### Core EOS: TM1 models

## Lagrangian density

$$\begin{aligned}
 \mathcal{L}_{\text{RMF}} = & \sum_{b=p,n} \bar{\psi}_b \{ i\gamma_\mu \partial^\mu - (M + g_\sigma \sigma) \\
 & - \gamma_\mu \left[ g_\omega \omega^\mu + \frac{g_\rho}{2} \tau_a \rho^{a\mu} + \frac{e}{2} (1 + \tau_3) A^\mu \right] \} \psi_b \\
 & + \frac{1}{2} \partial_\mu \sigma \partial^\mu \sigma - \frac{1}{2} m_\sigma^2 \sigma^2 - \frac{1}{3} g_2 \sigma^3 - \frac{1}{4} g_3 \sigma^4 \\
 & - \frac{1}{4} W_{\mu\nu} W^{\mu\nu} + \frac{1}{2} m_\omega^2 \omega_\mu \omega^\mu + \frac{1}{4} c_3 (\omega_\mu \omega^\mu)^2 \\
 & - \frac{1}{4} R_{\mu\nu}^a R^{a\mu\nu} + \frac{1}{2} m_\rho^2 \rho_\mu^a \rho^{a\mu} - \frac{1}{4} F_{\mu\nu} F^{\mu\nu} \\
 & + \Lambda_v (g_\omega^2 \omega_\mu \omega^\mu) (g_\rho^2 \rho_\mu^a \rho^{a\mu}) \\
 & + \sum_{l=e,\mu} \bar{\psi}_l (i\gamma_\mu \partial^\mu - m_l + e\gamma_\mu A^\mu) \psi_l,
 \end{aligned}$$

## Symmetry energy slope

$$L = 3n_0 \left[ \frac{\partial E_{\text{sym}}(n_b)}{\partial n_b} \right]_{n_b=n_0}$$

## TM1 parametrization

Model	TM1(L=40)	TM1(L=60)	TM1(L=80)	TM1(L=111)
$g_\sigma$	10.0289	10.0289	10.0289	10.0289
$g_\omega$	12.6139	12.6139	12.6139	12.6139
$g_2$ (fm <sup>-1</sup> )	-7.2325	-7.2325	-7.2325	-7.2325
$g_3$	0.6183	0.6183	0.6183	0.6183
$c_3$	71.3075	71.3075	71.3075	71.3075
$g_\rho$	<b>13.9714</b>	<b>11.2610</b>	<b>10.1484</b>	<b>9.2644</b>
$\Lambda_v$	<b>0.0429</b>	<b>0.0248</b>	<b>0.0128</b>	<b>0.0000</b>
$n_0$ (fm <sup>-3</sup> )	0.145	0.145	0.145	0.145
$E_0$ (MeV)	-16.3	-16.3	-16.3	-16.3
$K$ (MeV)	281	281	281	281
$E_{\text{sym}}$ (MeV)	<b>31.38</b>	<b>33.29</b>	<b>34.86</b>	<b>36.89</b>
$L$ (MeV)	<b>40</b>	<b>60</b>	<b>80</b>	<b>111</b>
$\Delta r_{\text{np}}$ ( <sup>208</sup> Pb) (fm)	<b>0.16</b>	<b>0.21</b>	<b>0.24</b>	<b>0.27</b>
$r_c$ ( <sup>208</sup> Pb) (fm)	<b>5.56</b>	<b>5.55</b>	<b>5.54</b>	<b>5.54</b>
$E/A$ ( <sup>208</sup> Pb) (MeV)	7.88	7.88	7.88	7.88

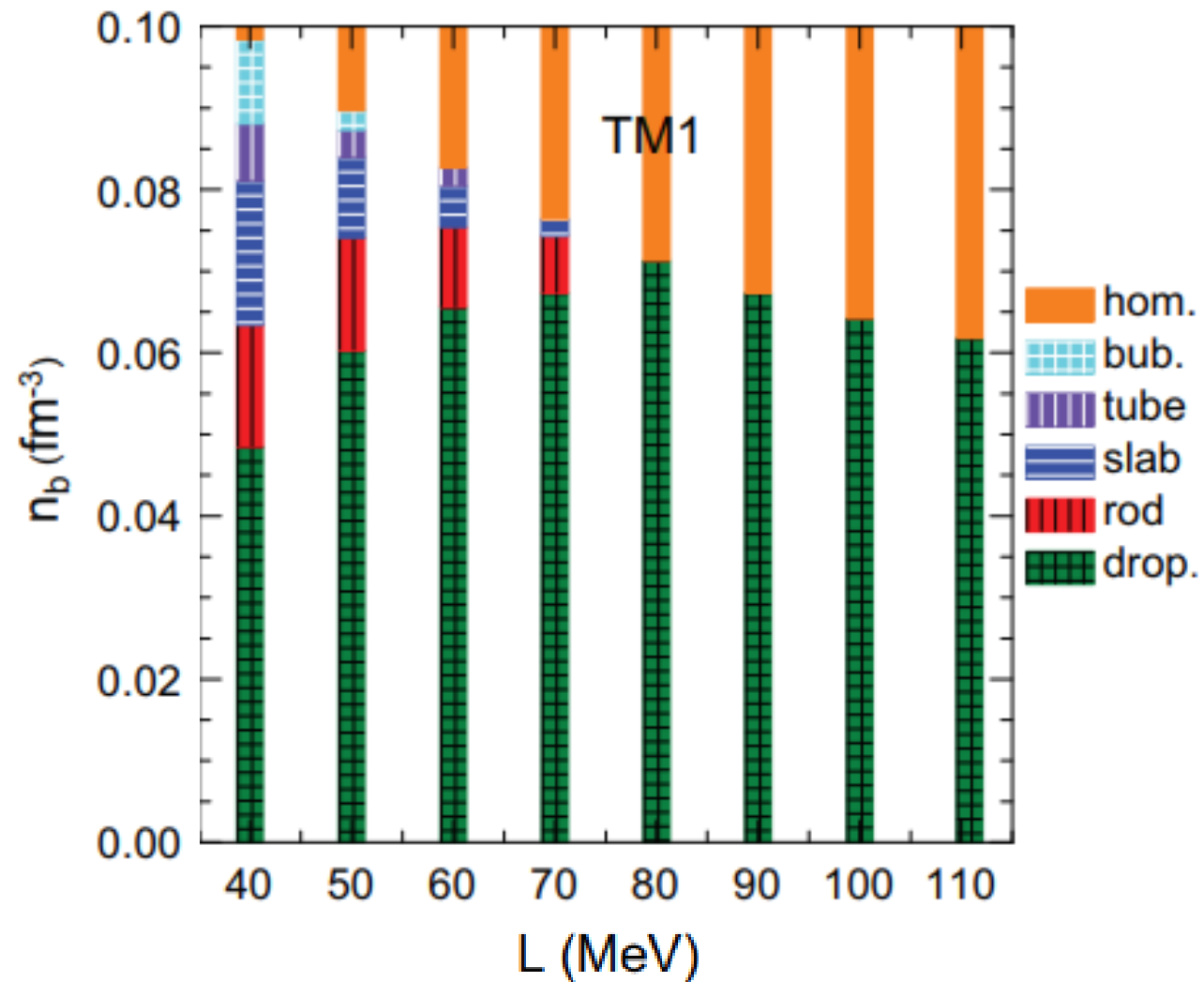


Self-consistent Thomas-Fermi

Non-uniform matter

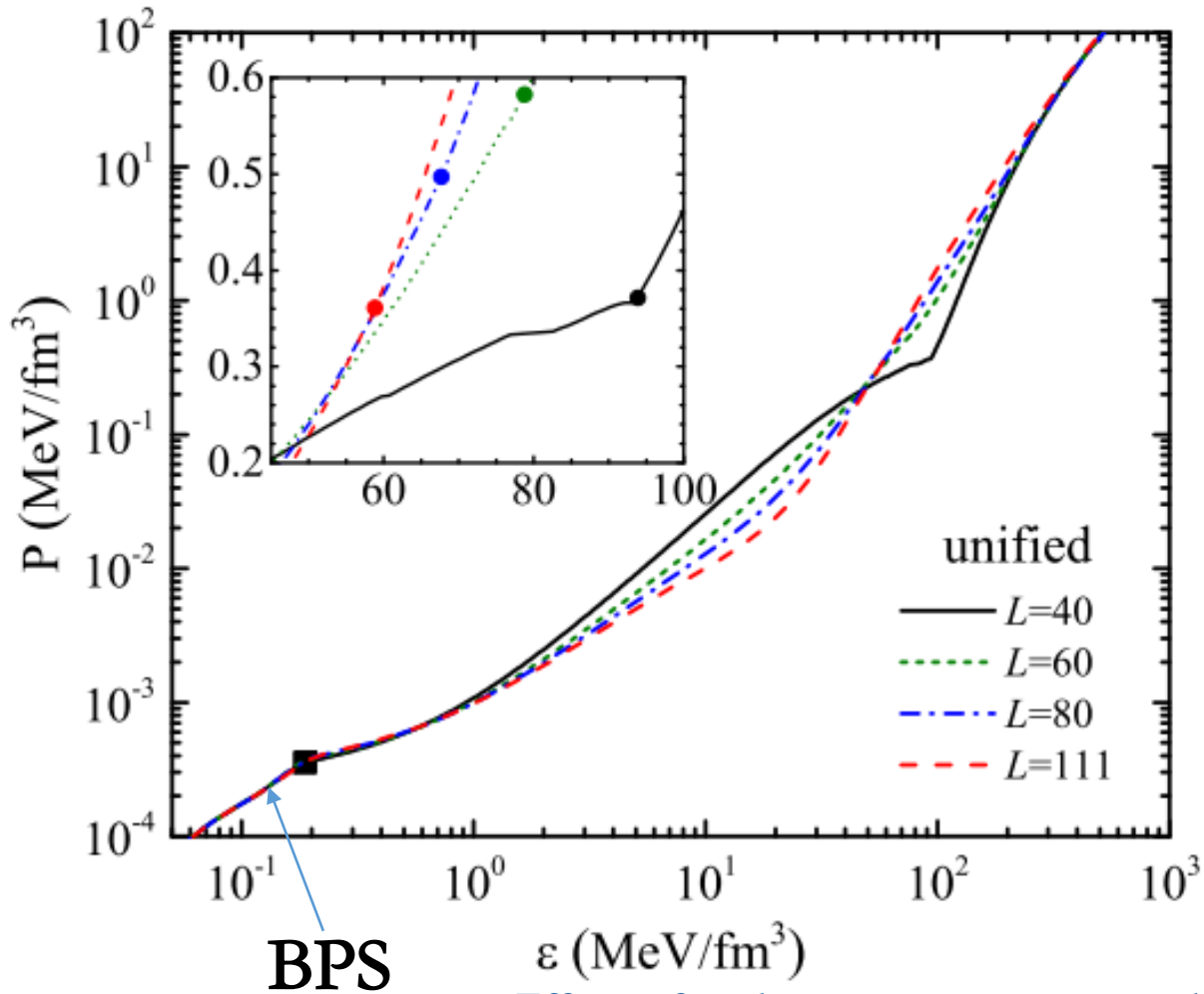
Pasta phases

Model	rod	slab	tube	bubble	HM
TM1( $L=40$ )	0.049	0.064	0.082	0.089	0.099
TM1( $L=60$ )	0.066	0.076	0.081	—	0.083
TM1( $L=80$ )	—	—	—	—	0.072
TM1( $L=111$ )	—	—	—	—	0.062

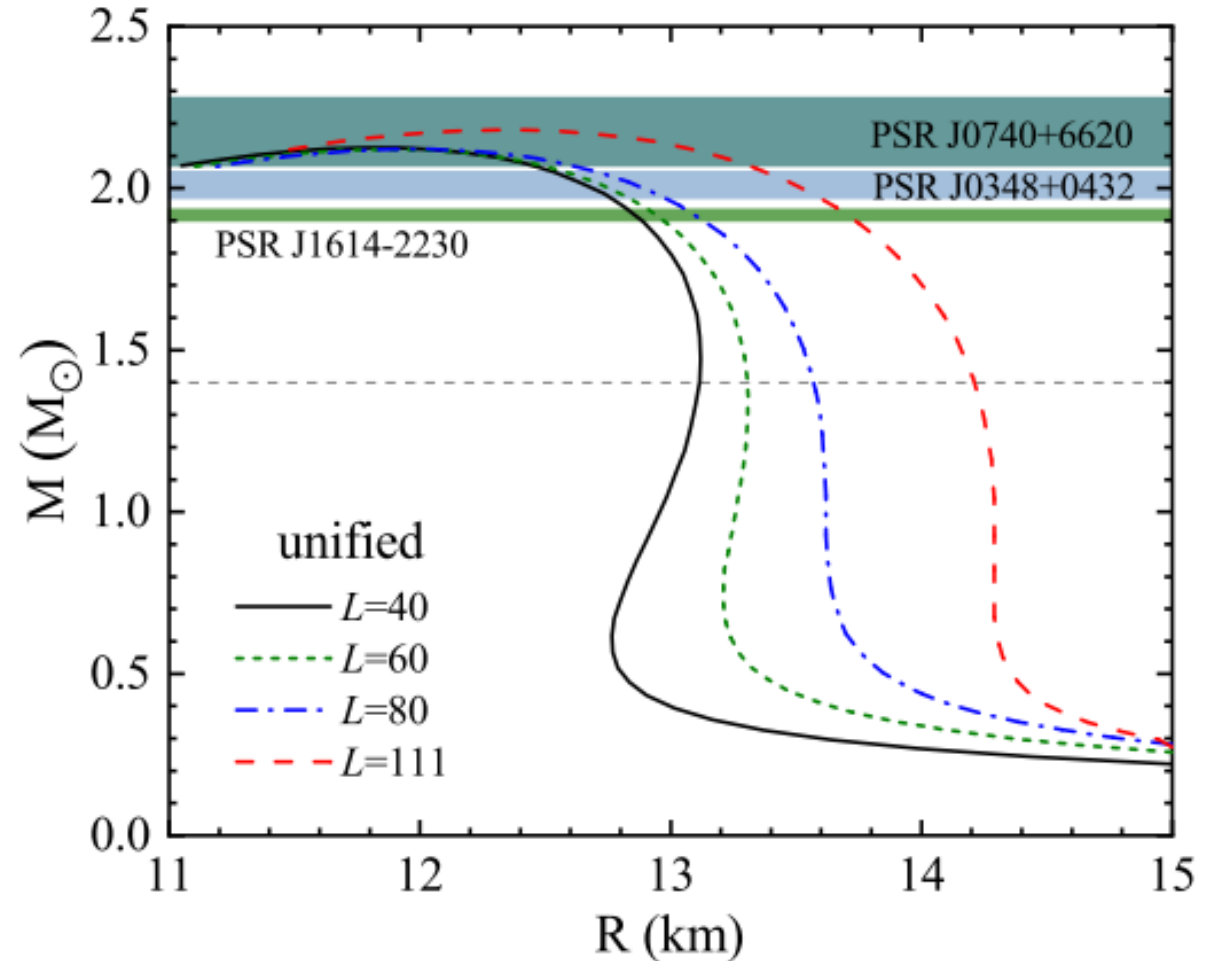


# 3 Results—Neutron-star properties with unified EOSs

EOSs



Mass-radius relations



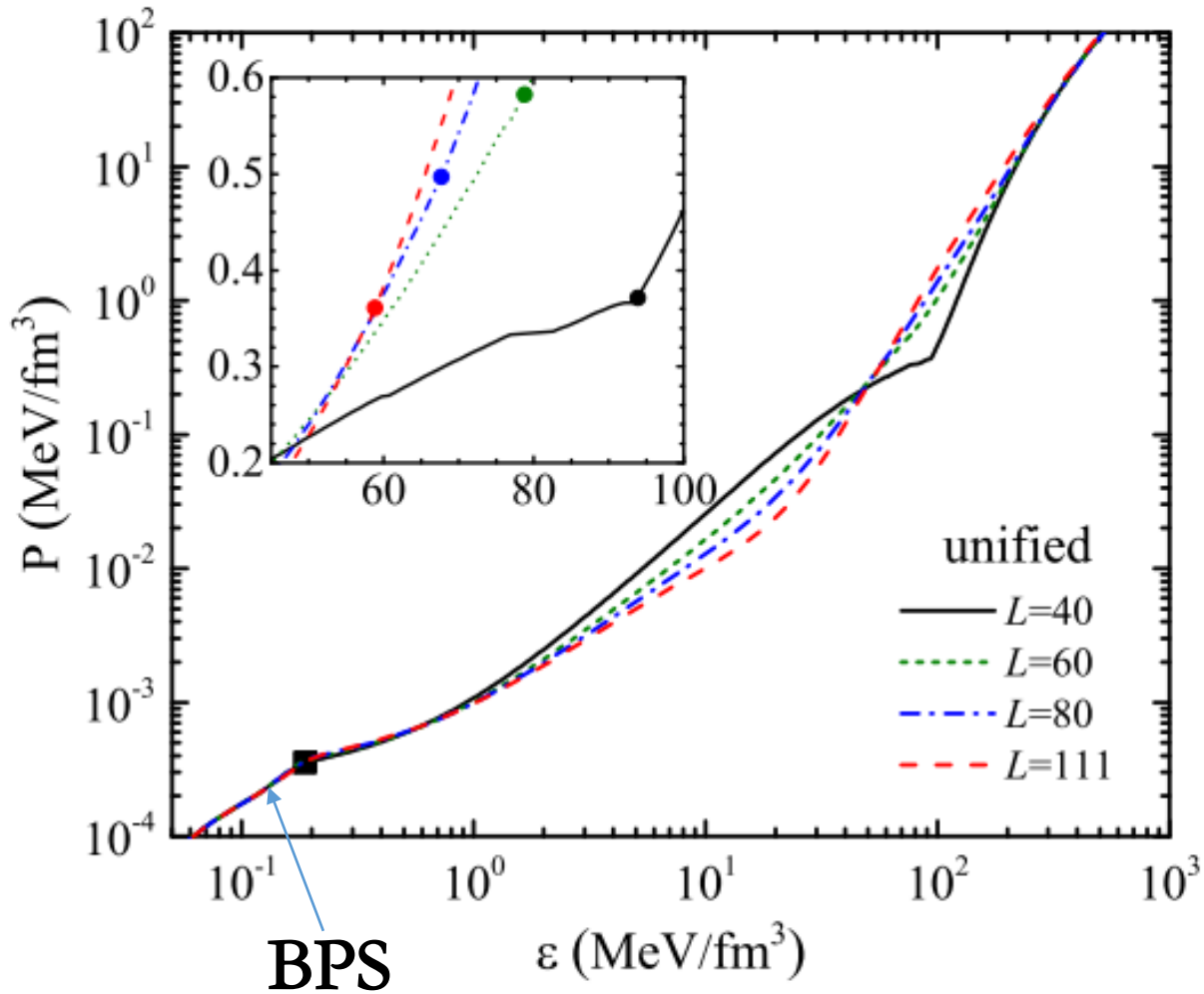
Effects of nuclear symmetry energy and equation of state on neutron star properties,

Fan Ji, Jinniu Hu, S. S. Bao and H. Shen, Phys. Rev. C (accepted) .

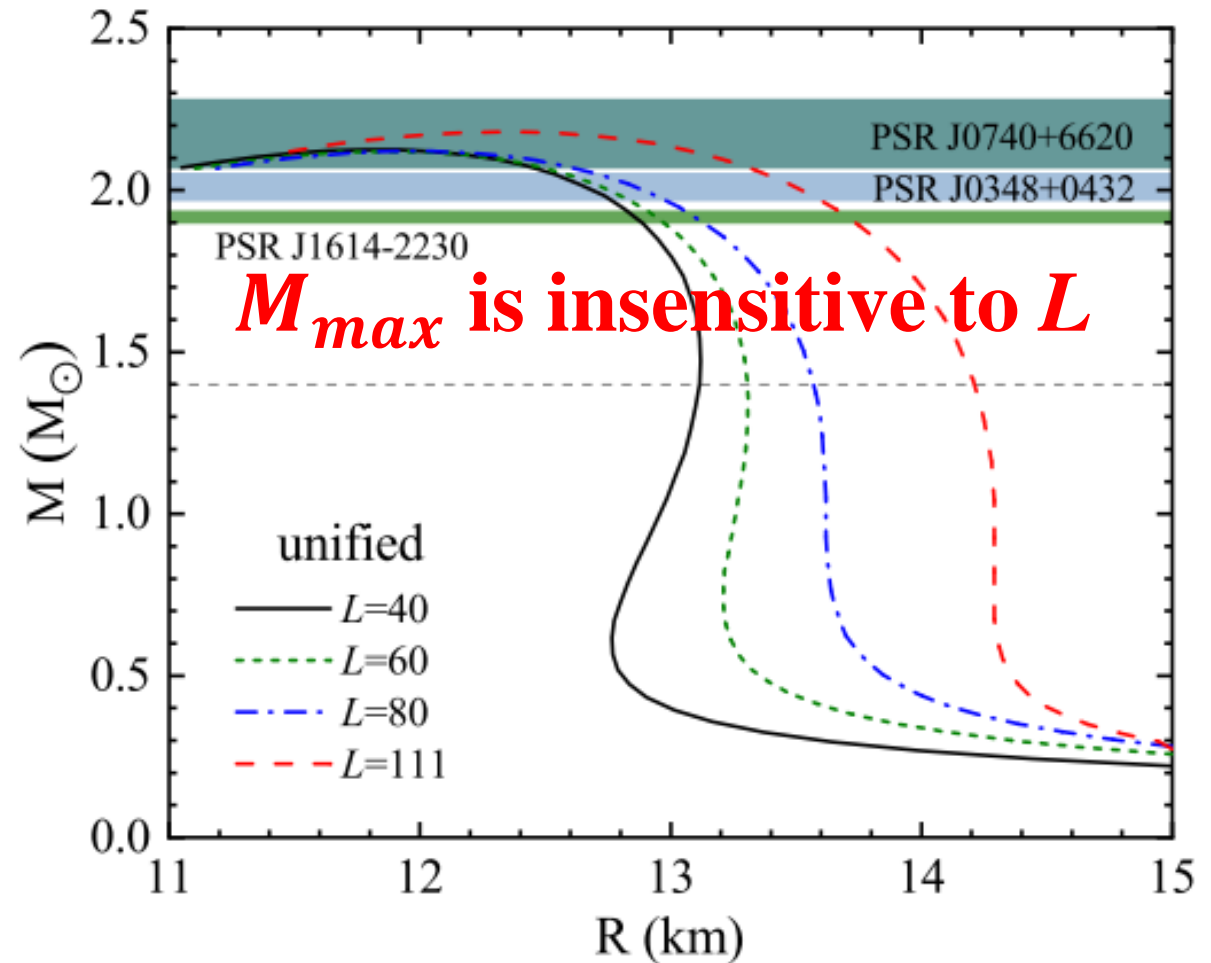


# 3 Results—Neutron-star properties with unified EOSs

EOSs

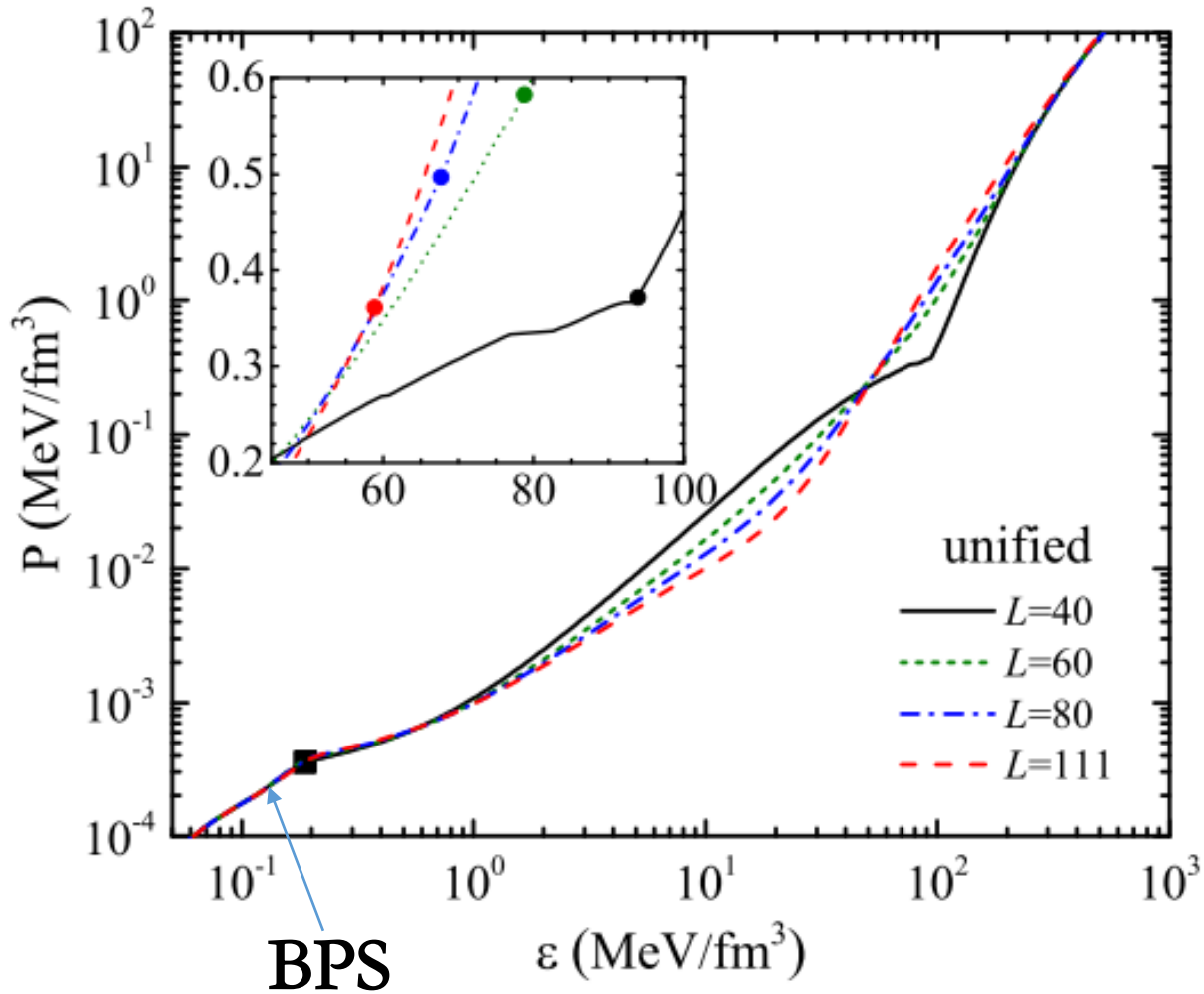


Mass-radius relations

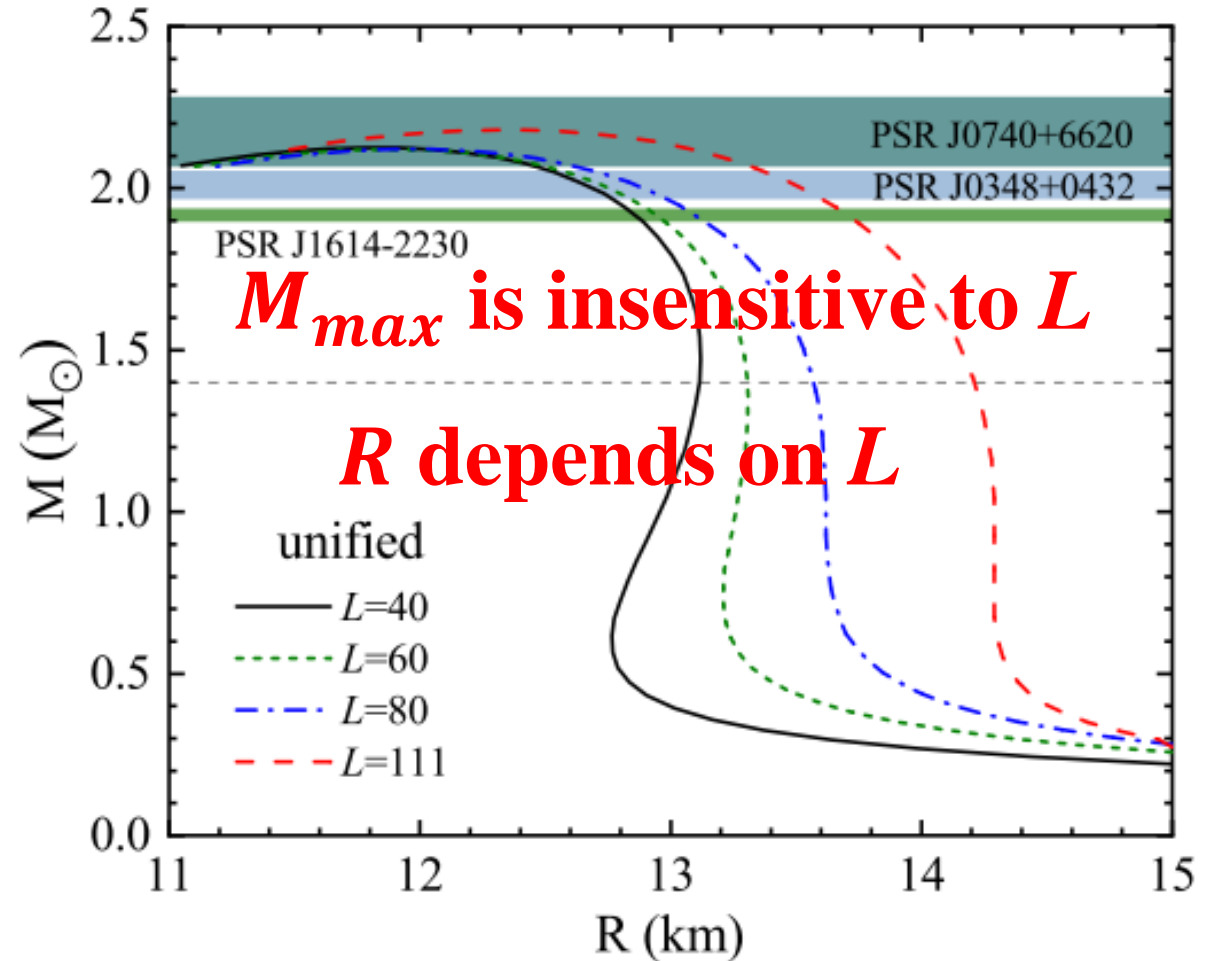


# 3 Results—Neutron-star properties with unified EOSs

EOSs

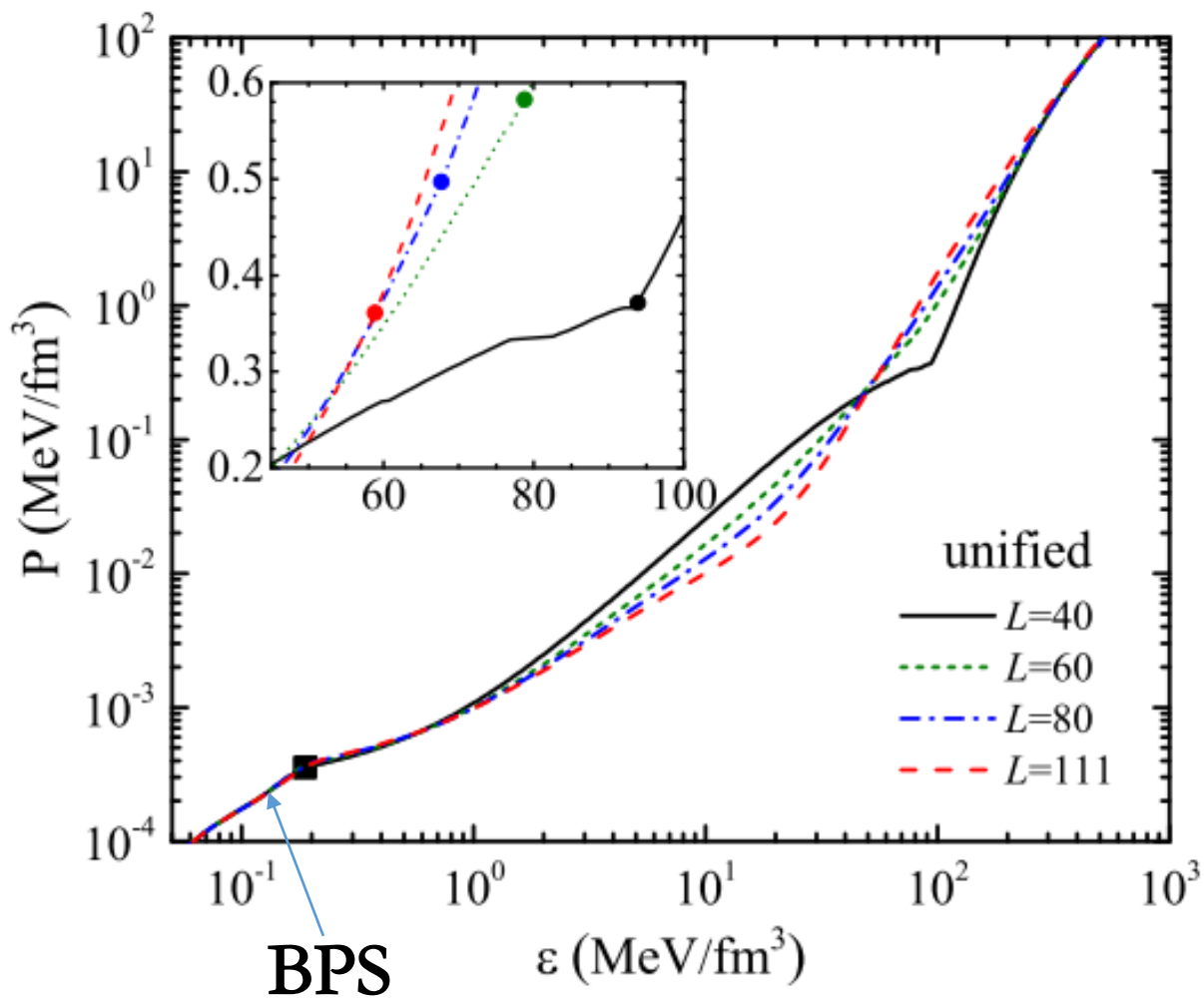


Mass-radius relations

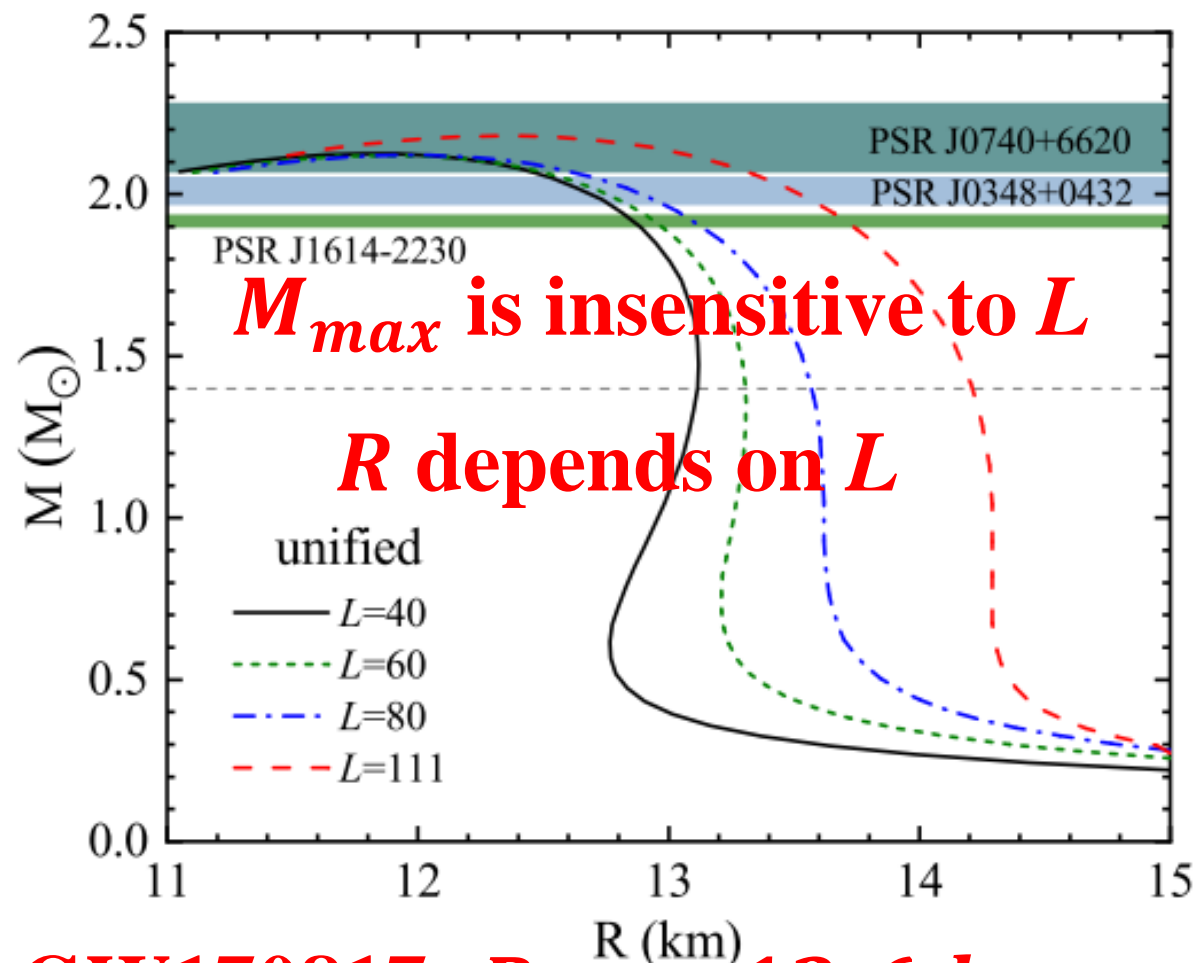


# 3 Results—Neutron-star properties with unified EOSs

EOSs

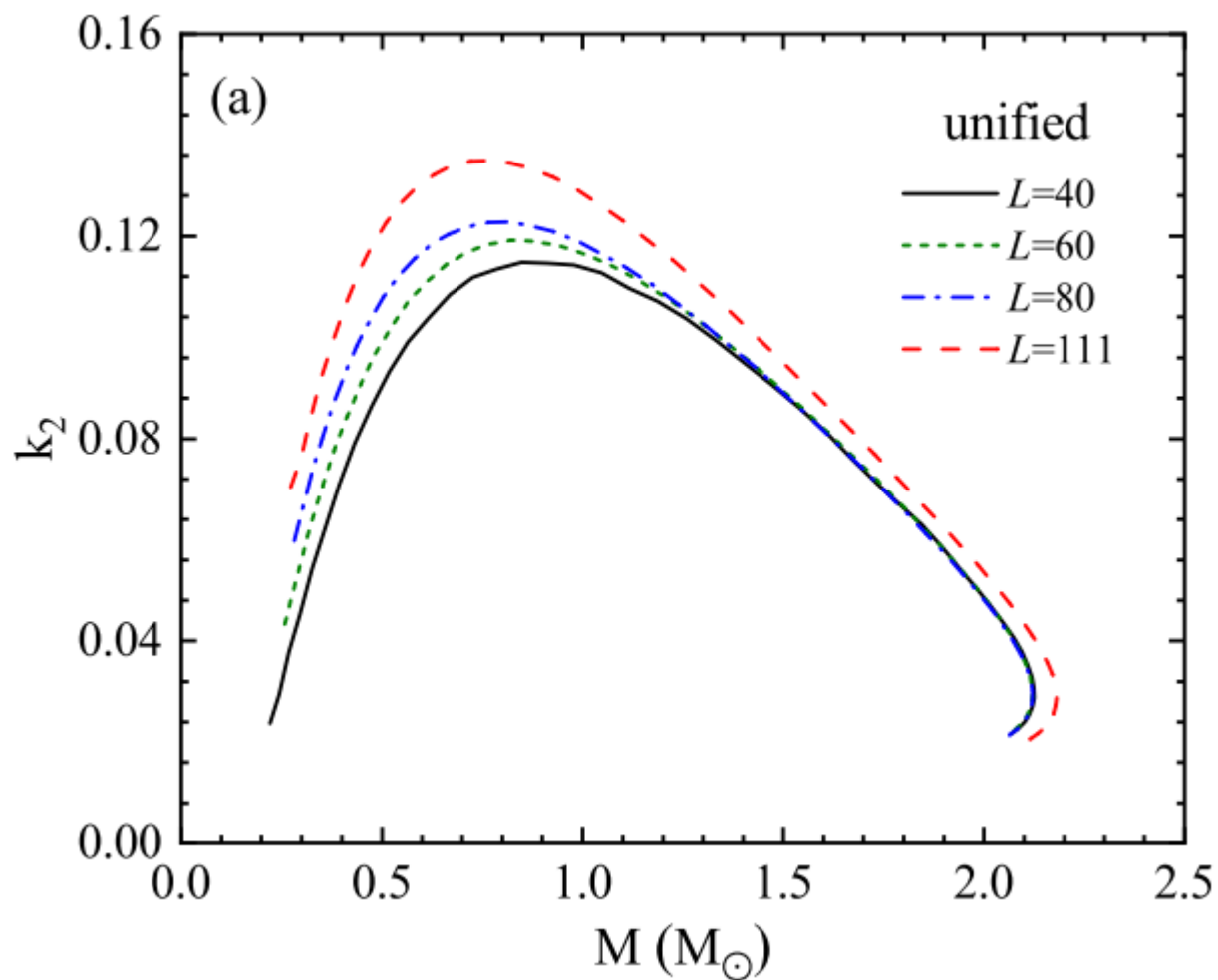


Mass-radius relations

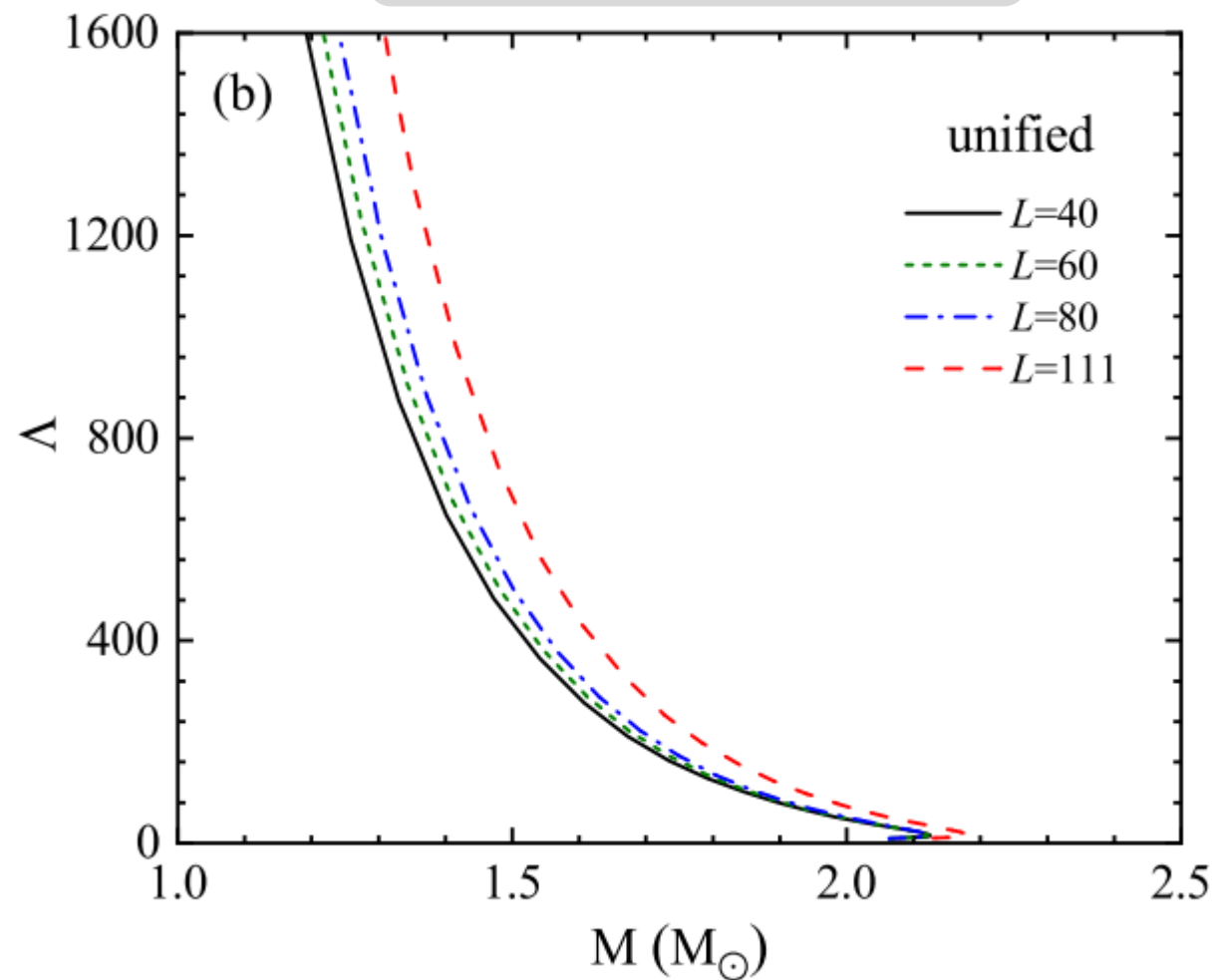


**GW170817:  $R_{1.4} < 13.6$  km**

Love number  $k_2$

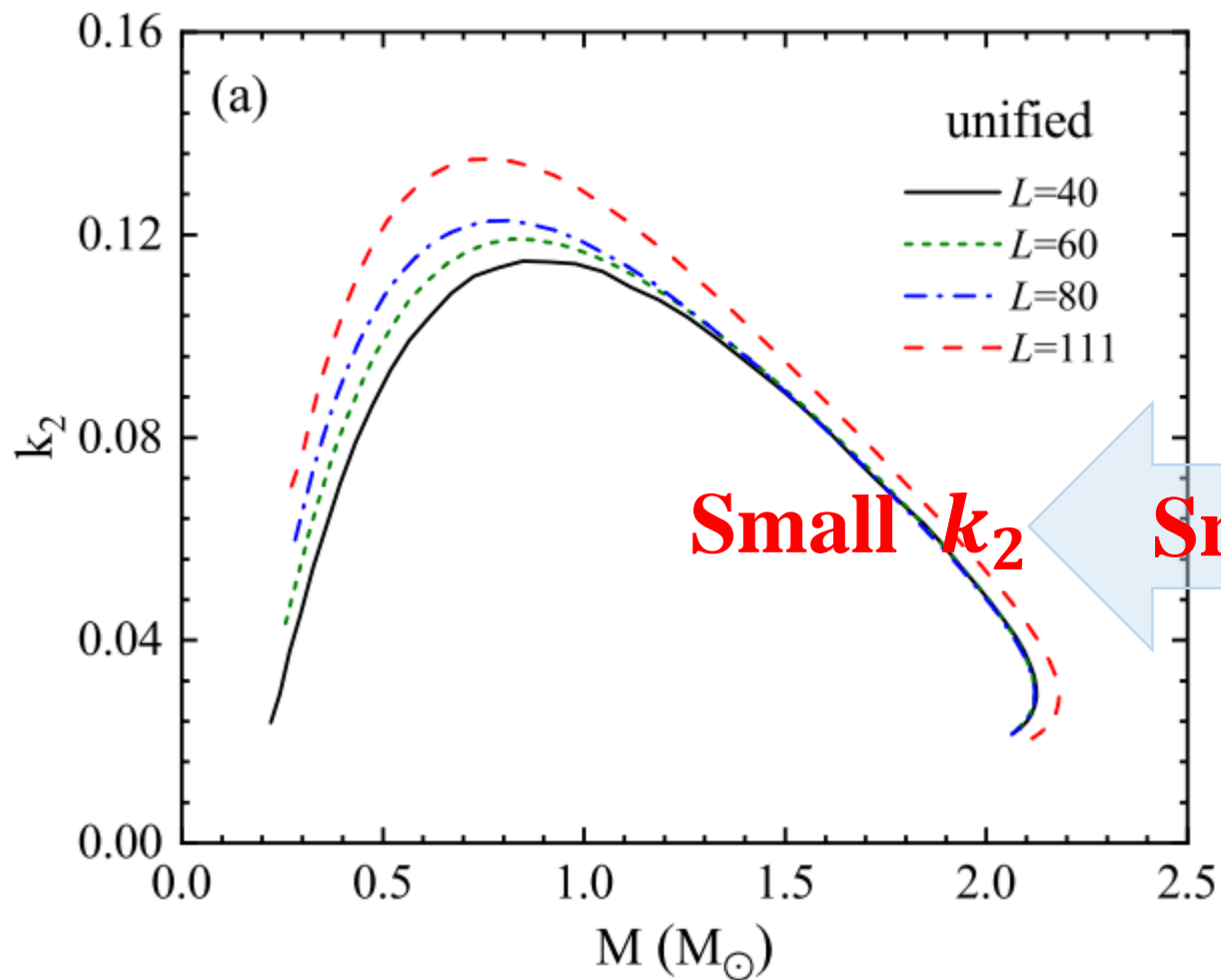


Tidal deformability  $\Lambda$

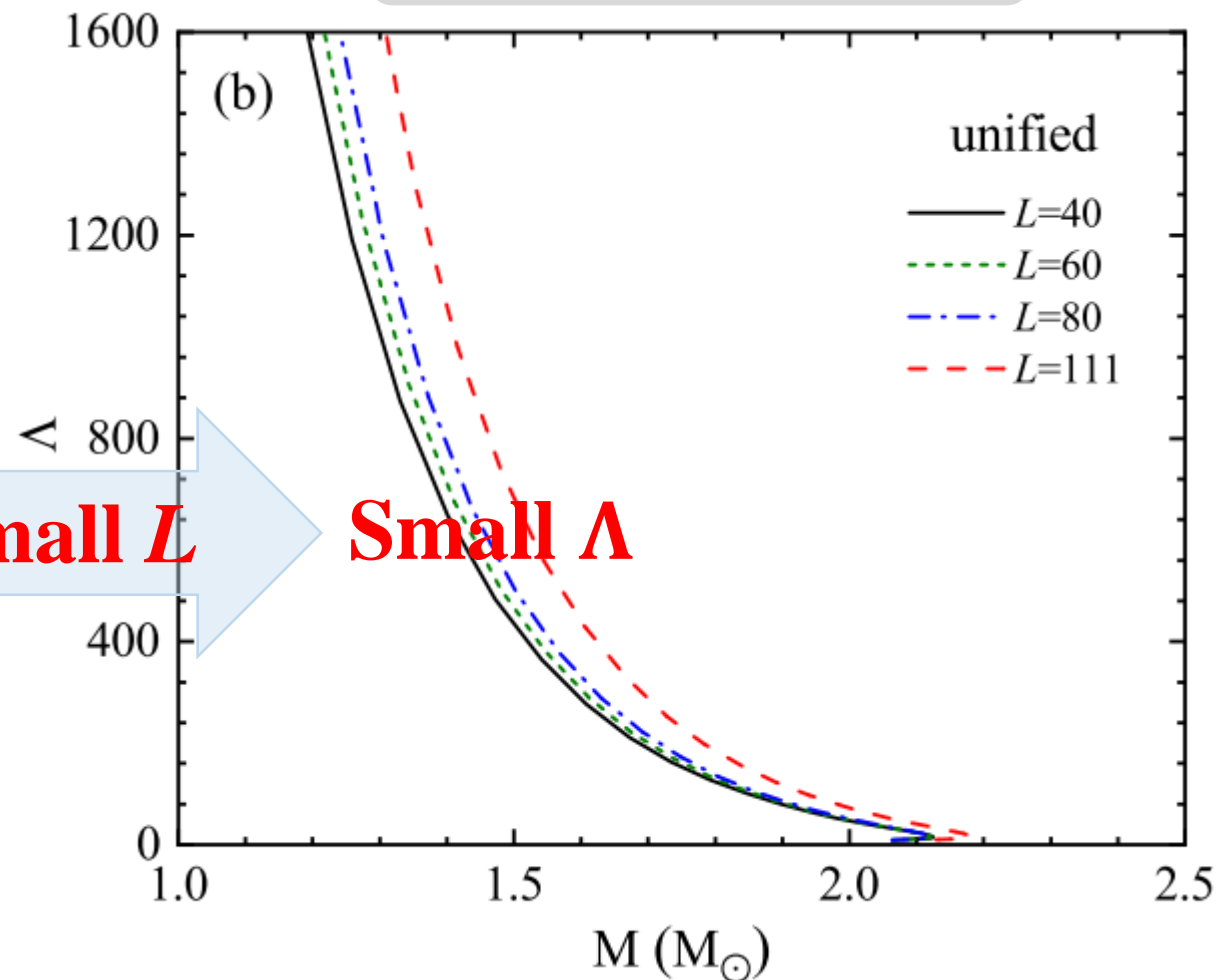


### 3 Results—Neutron-star properties with unified EOSs

Love number  $k_2$



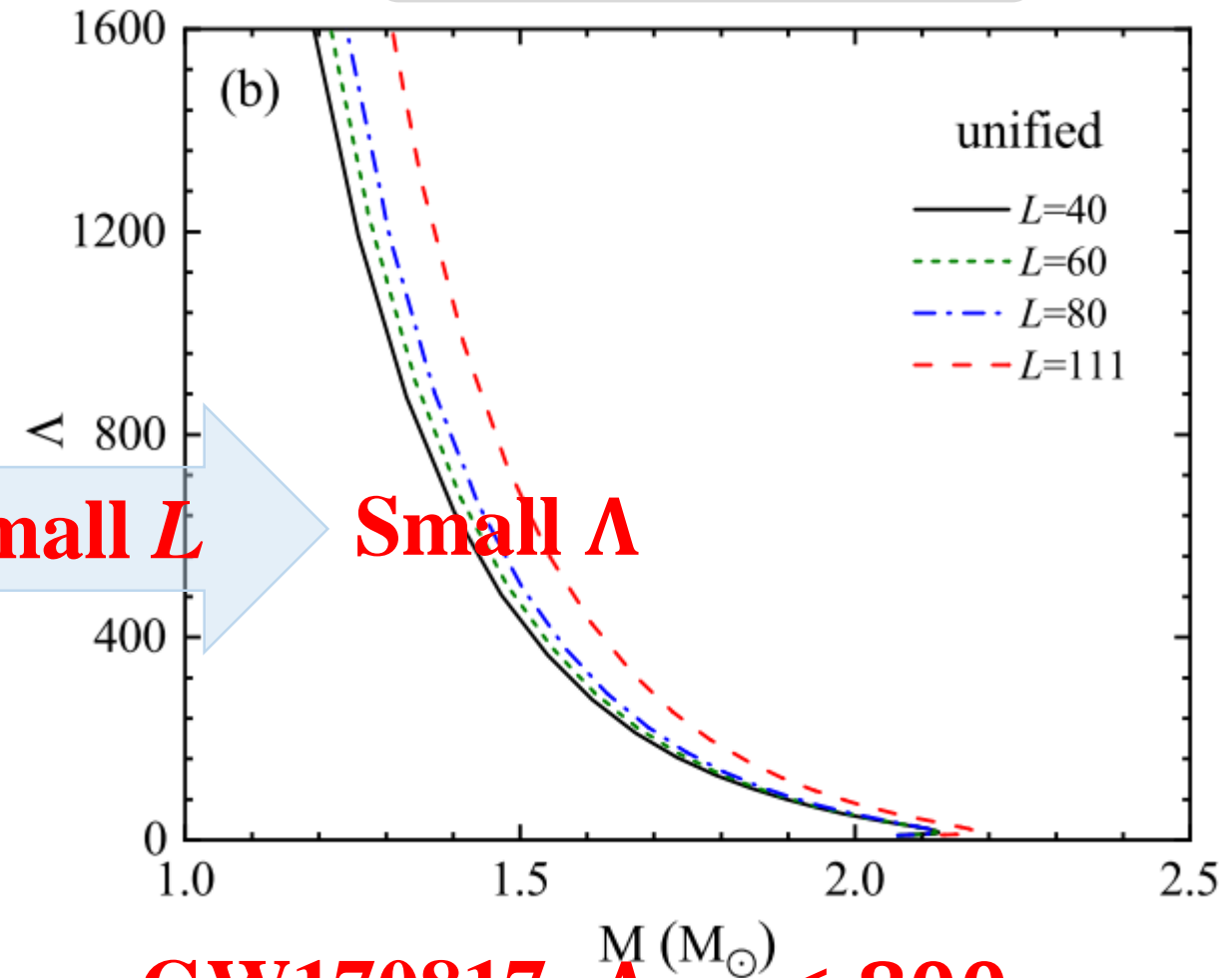
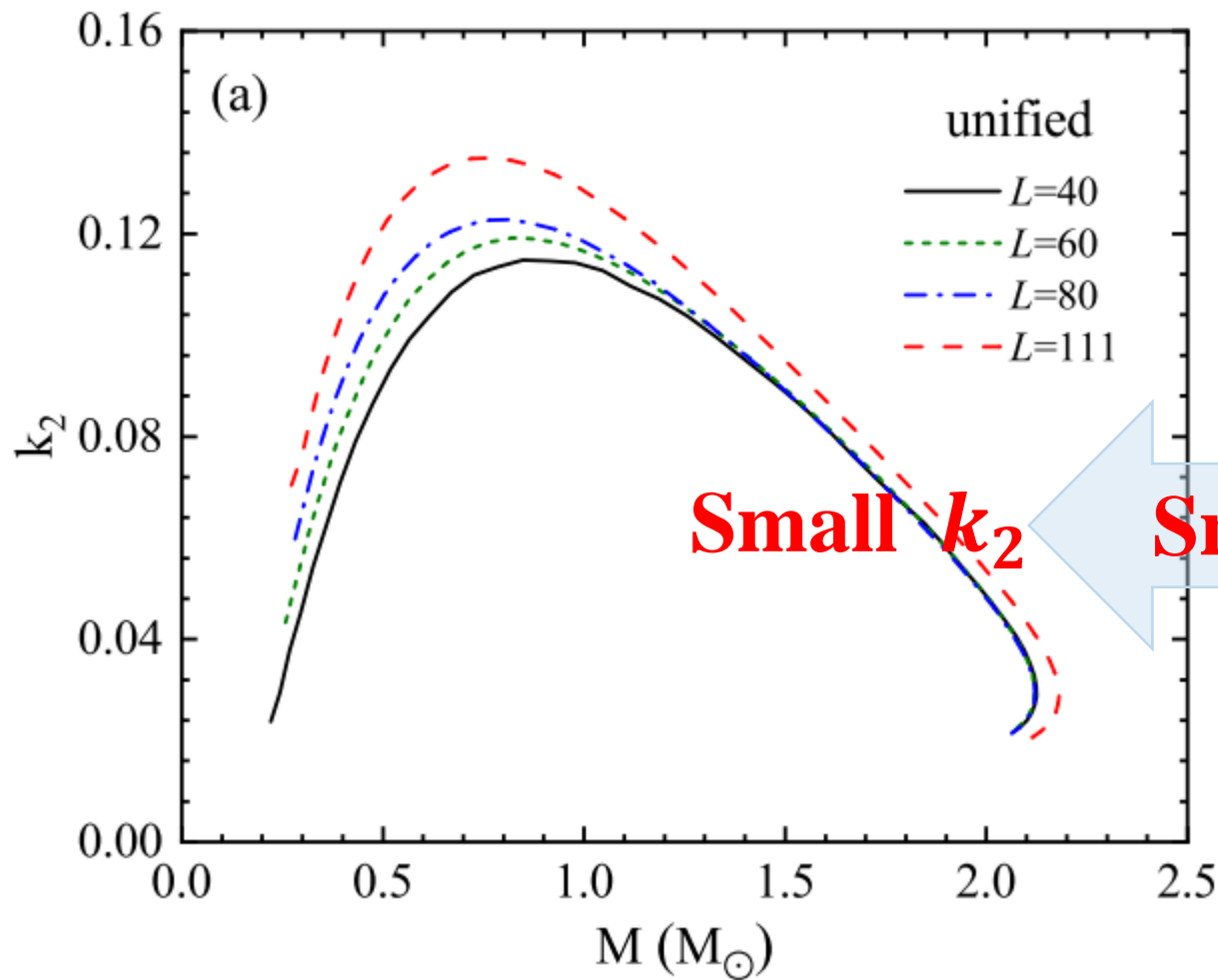
Tidal deformability  $\Lambda$



# 3 Results—Neutron-star properties with unified EOSs

Love number  $k_2$

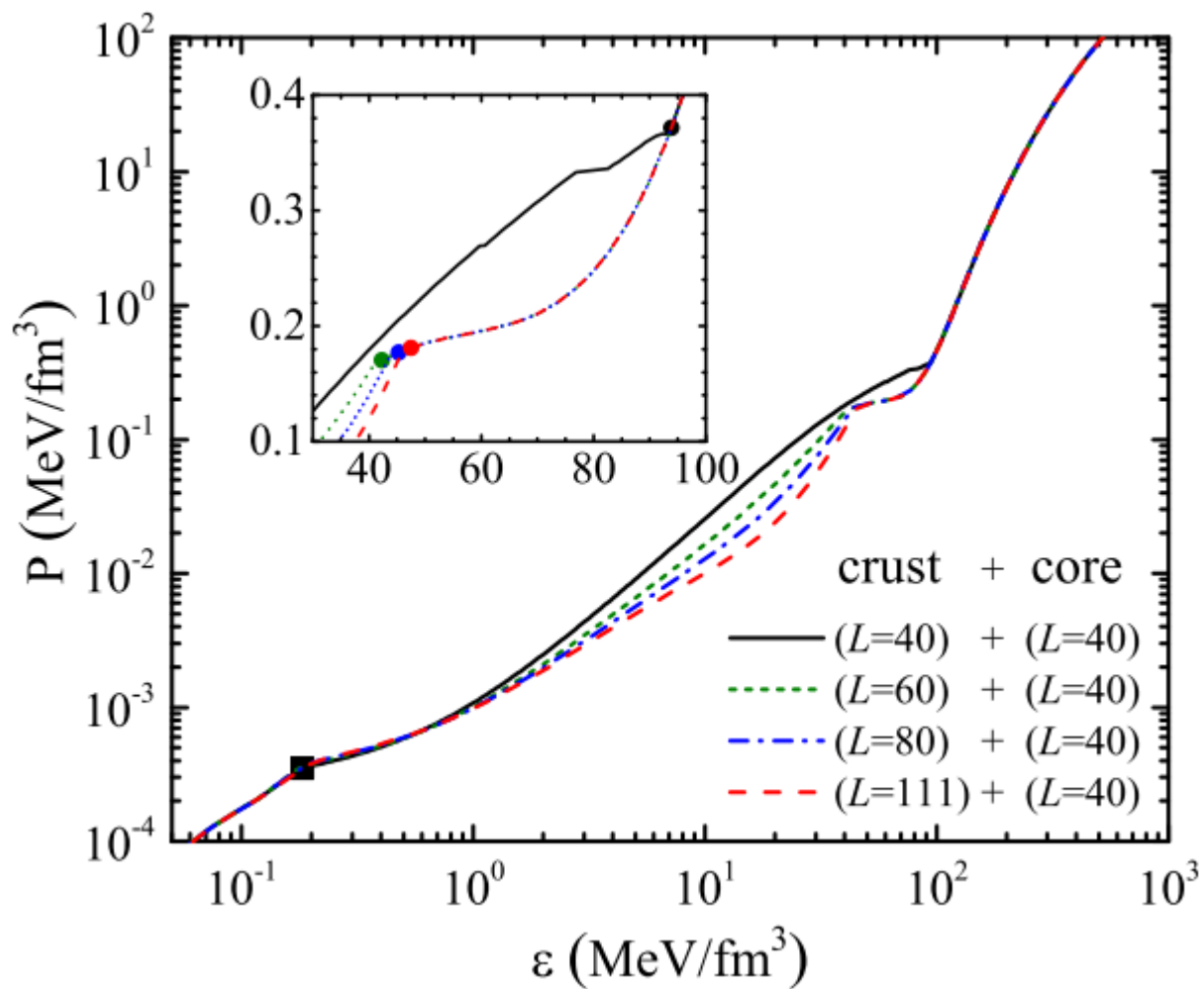
Tidal deformability  $\Lambda$



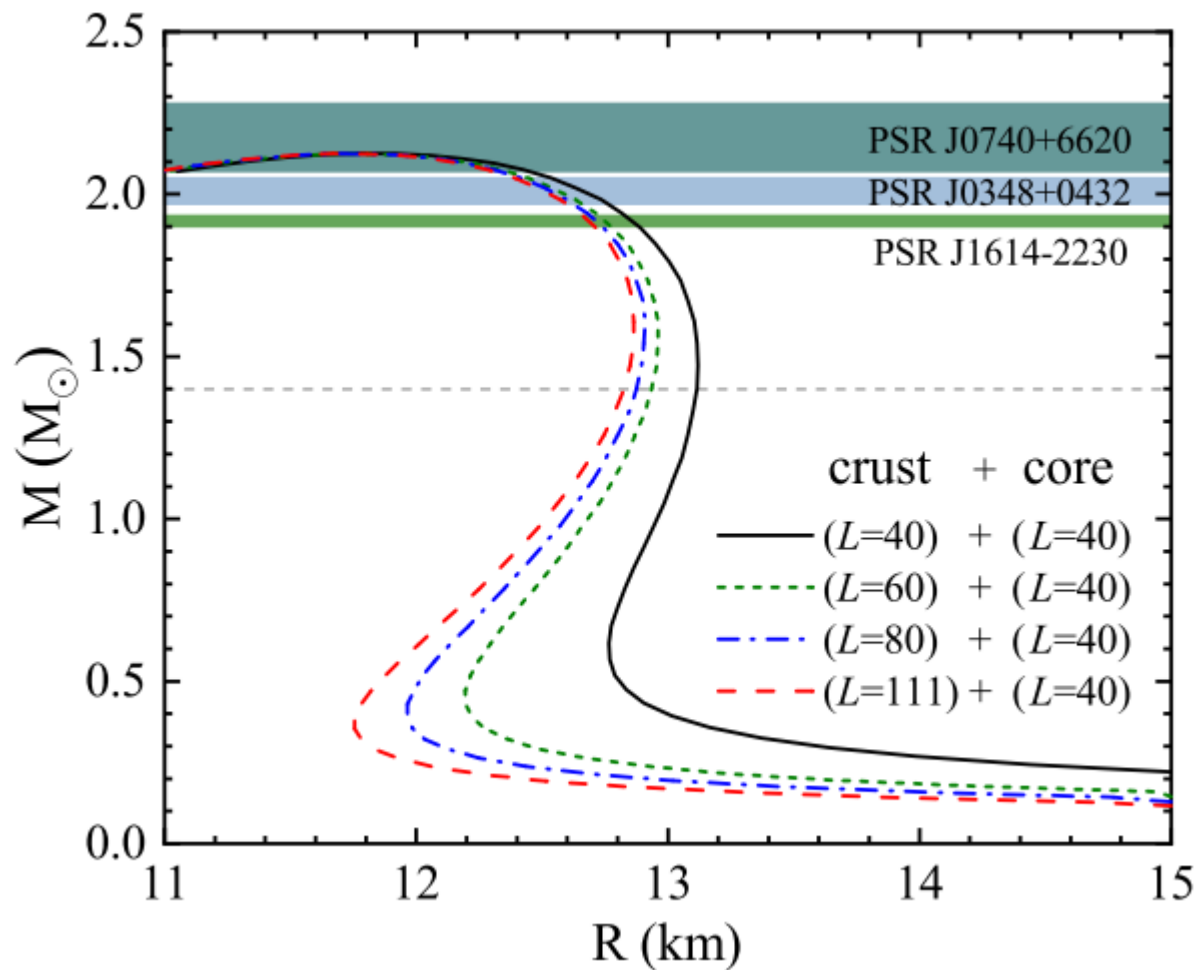
**GW170817:  $\Lambda_{1.4} < 800$**

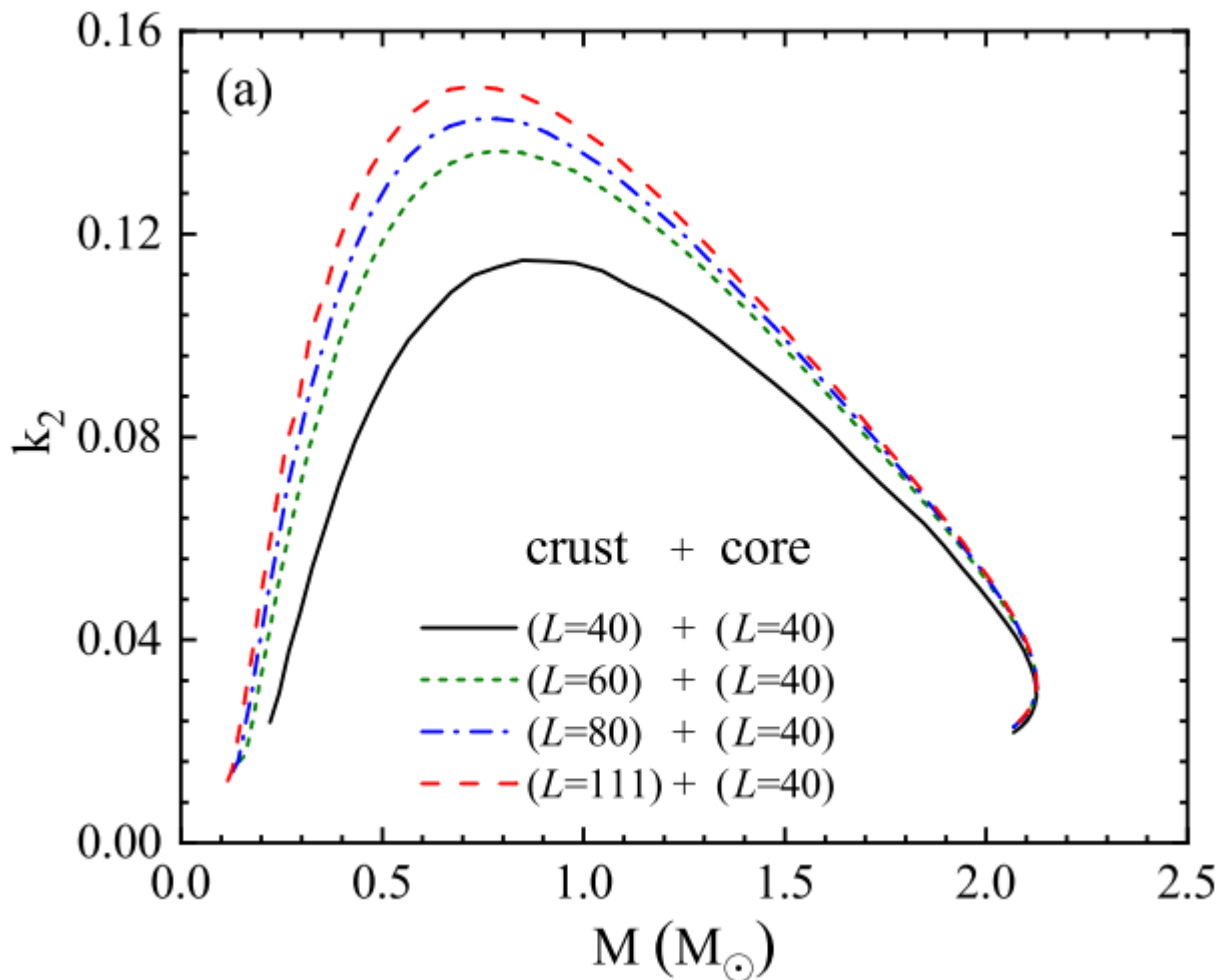
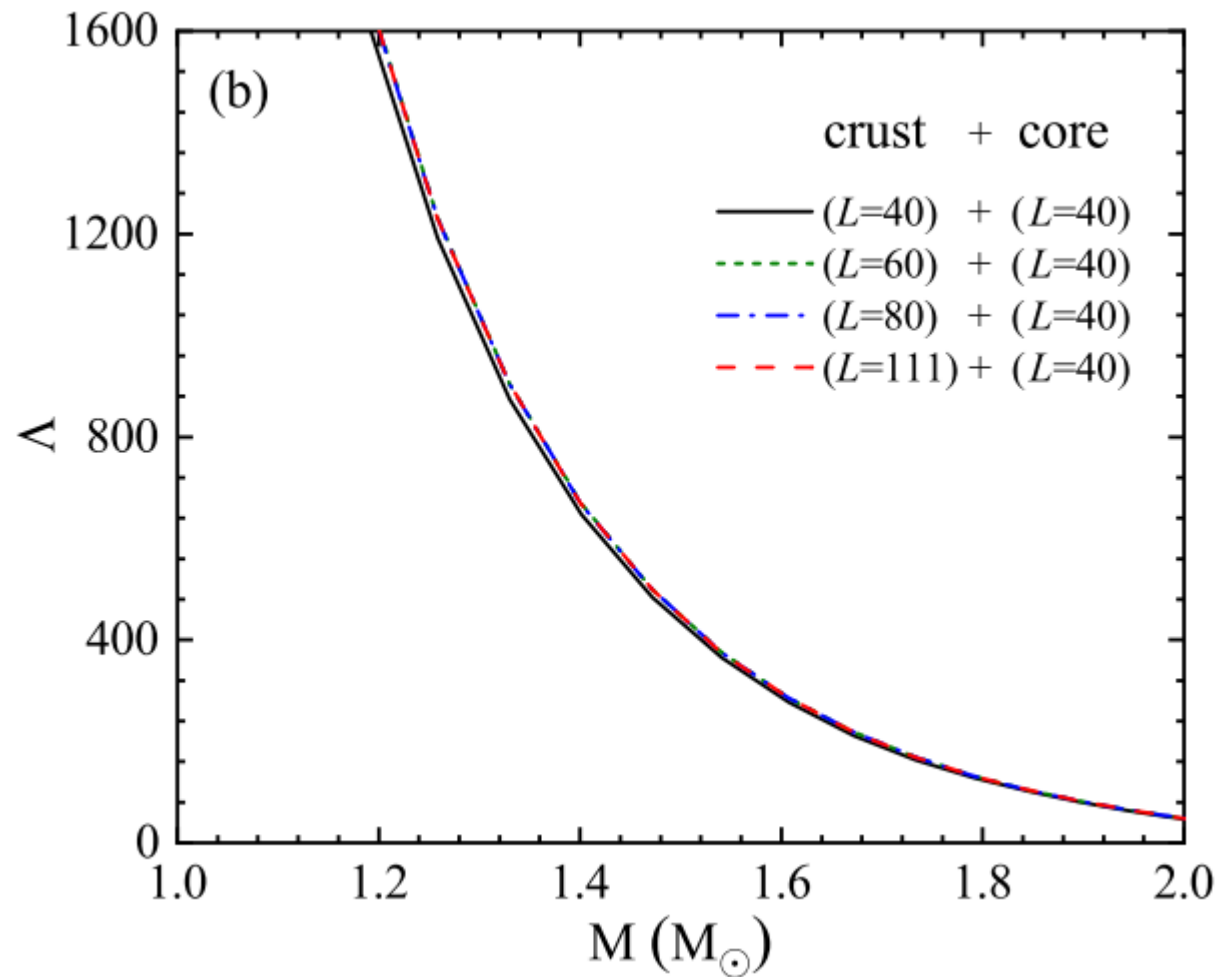


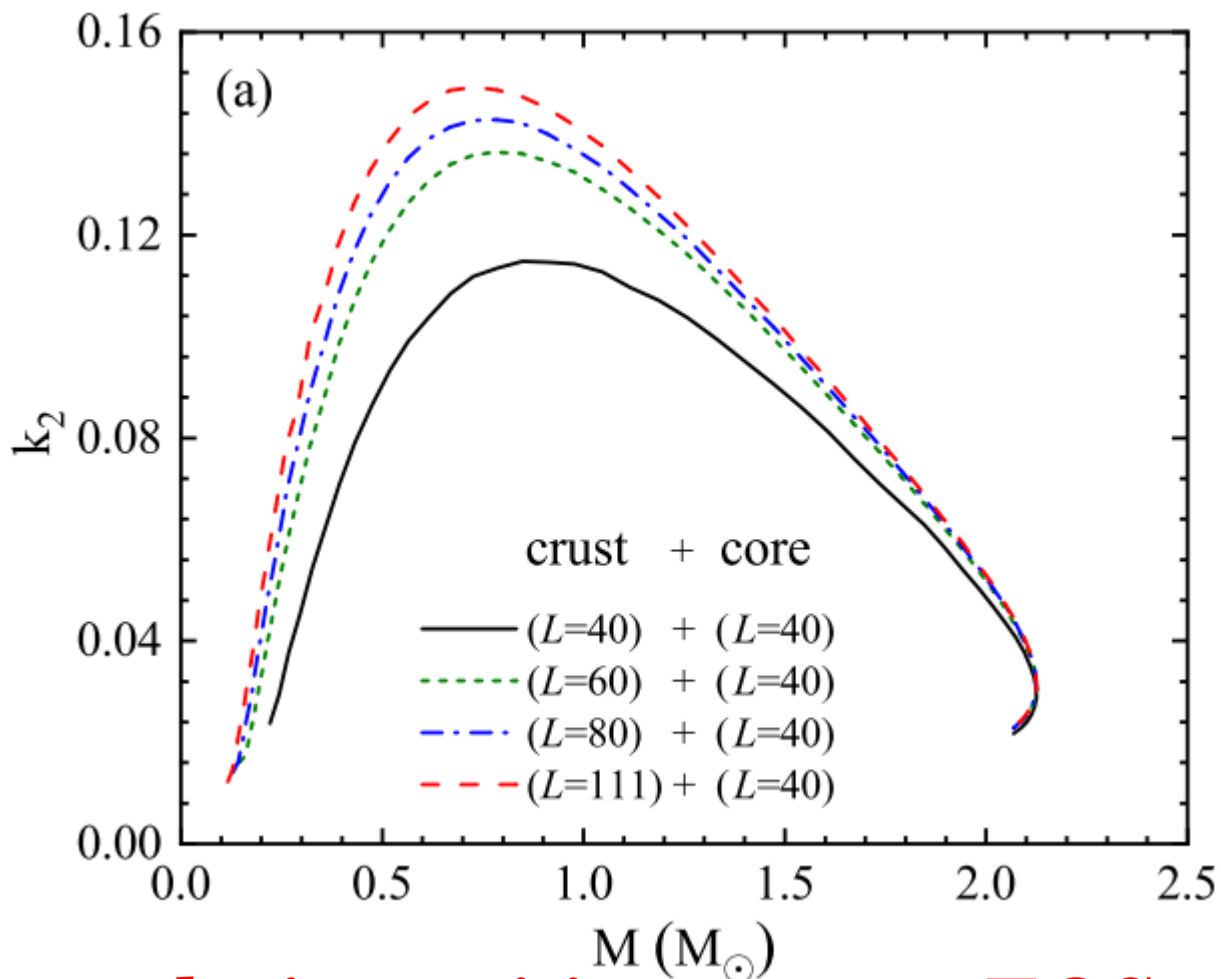
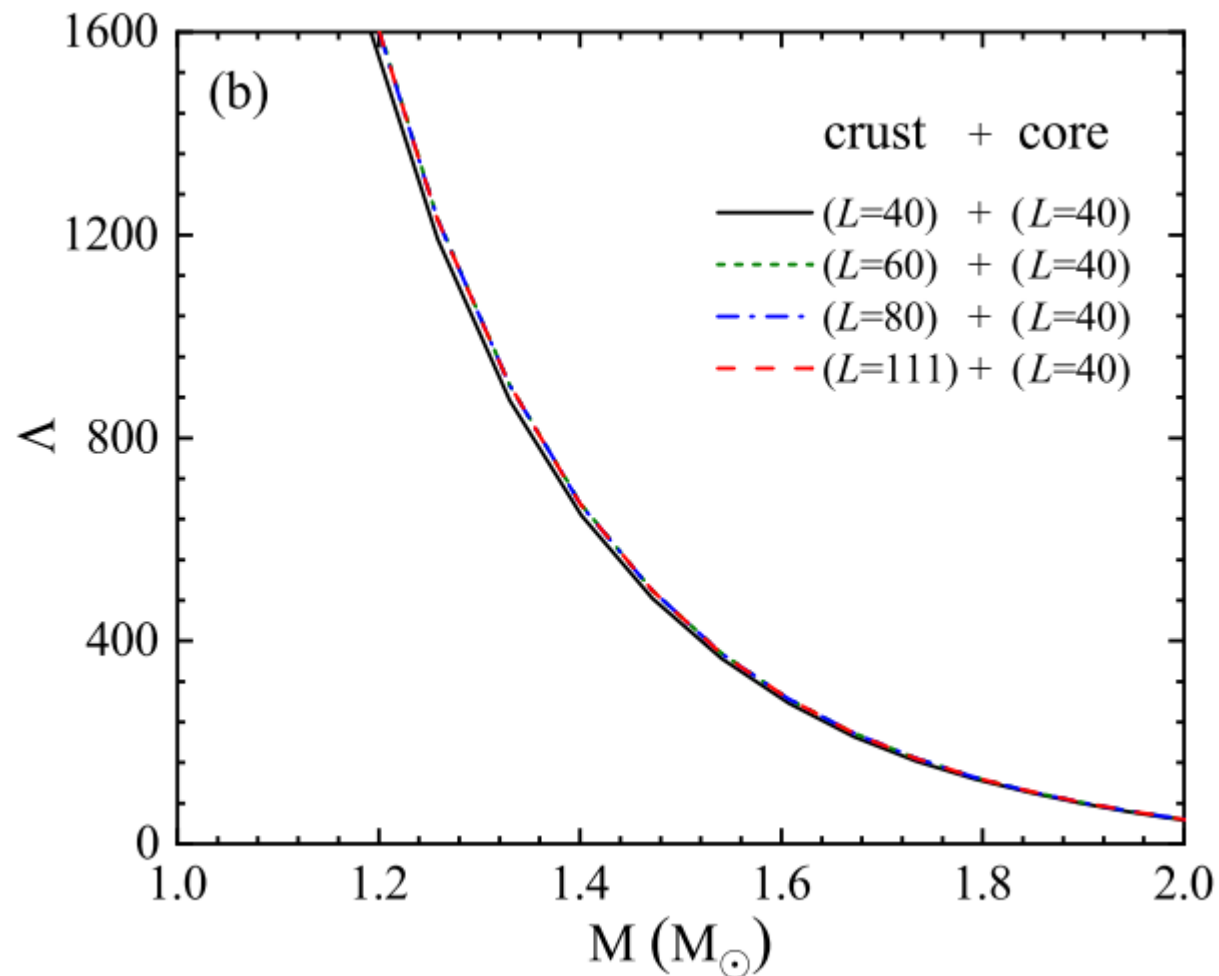
EOSs

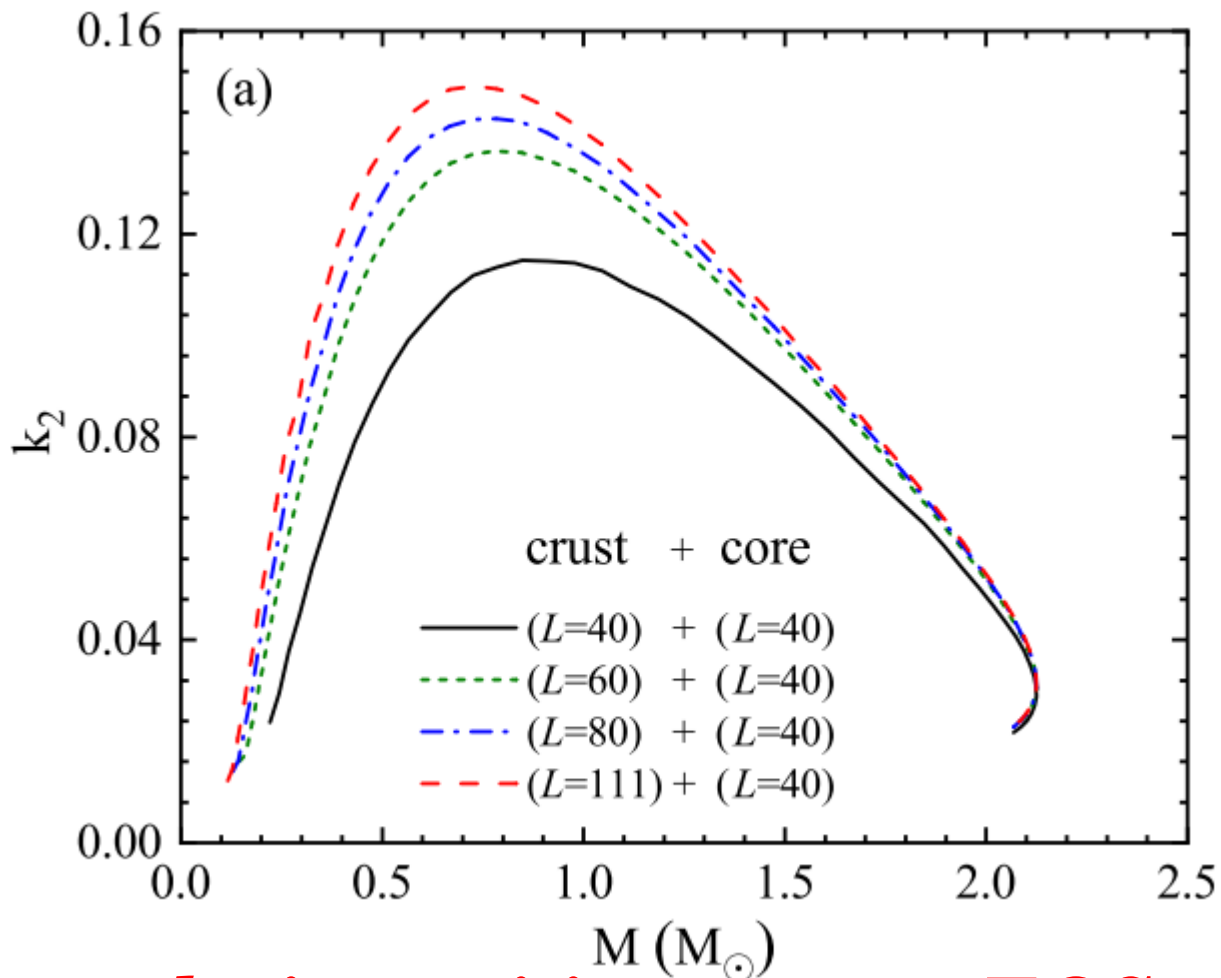
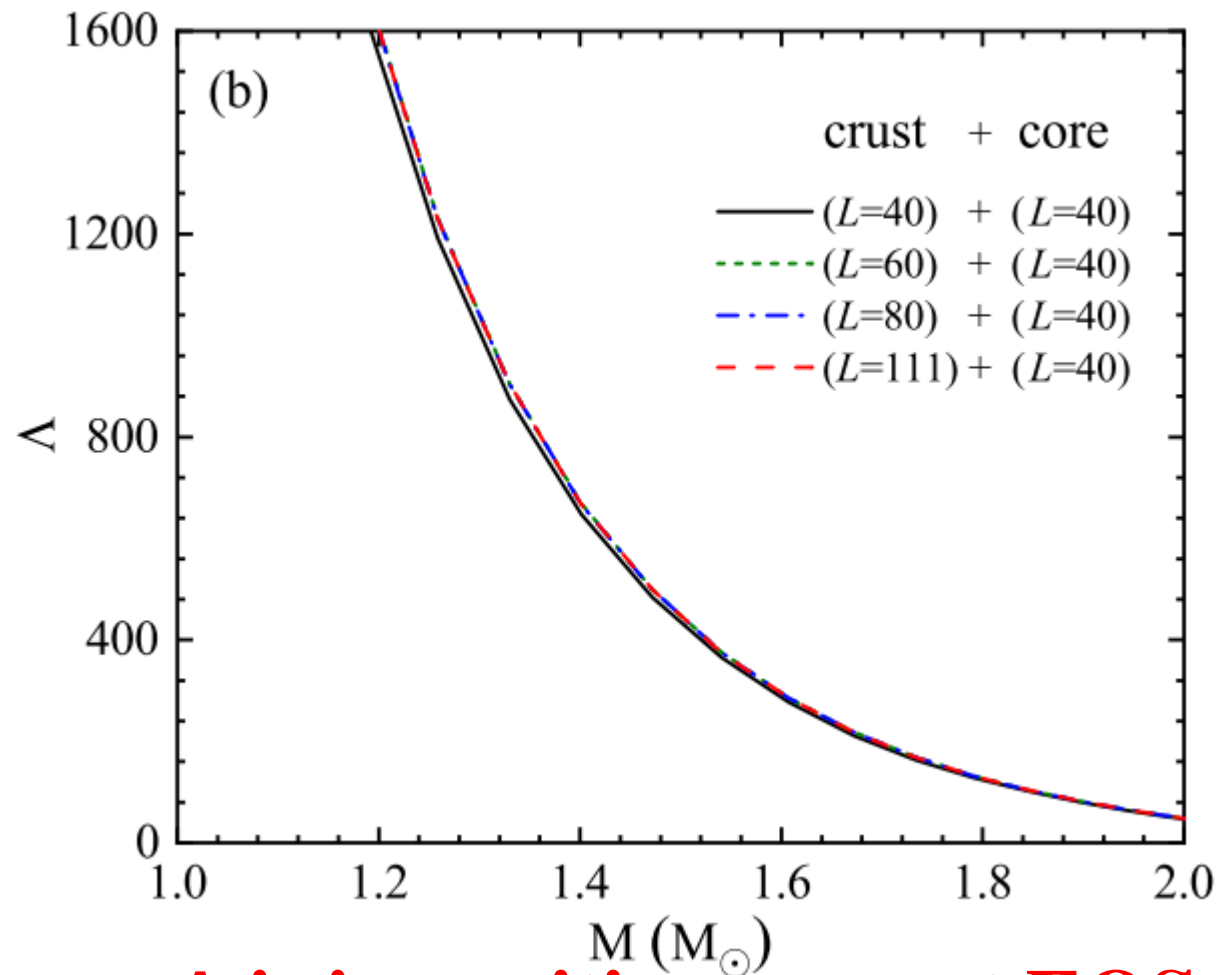


Mass-radius relations

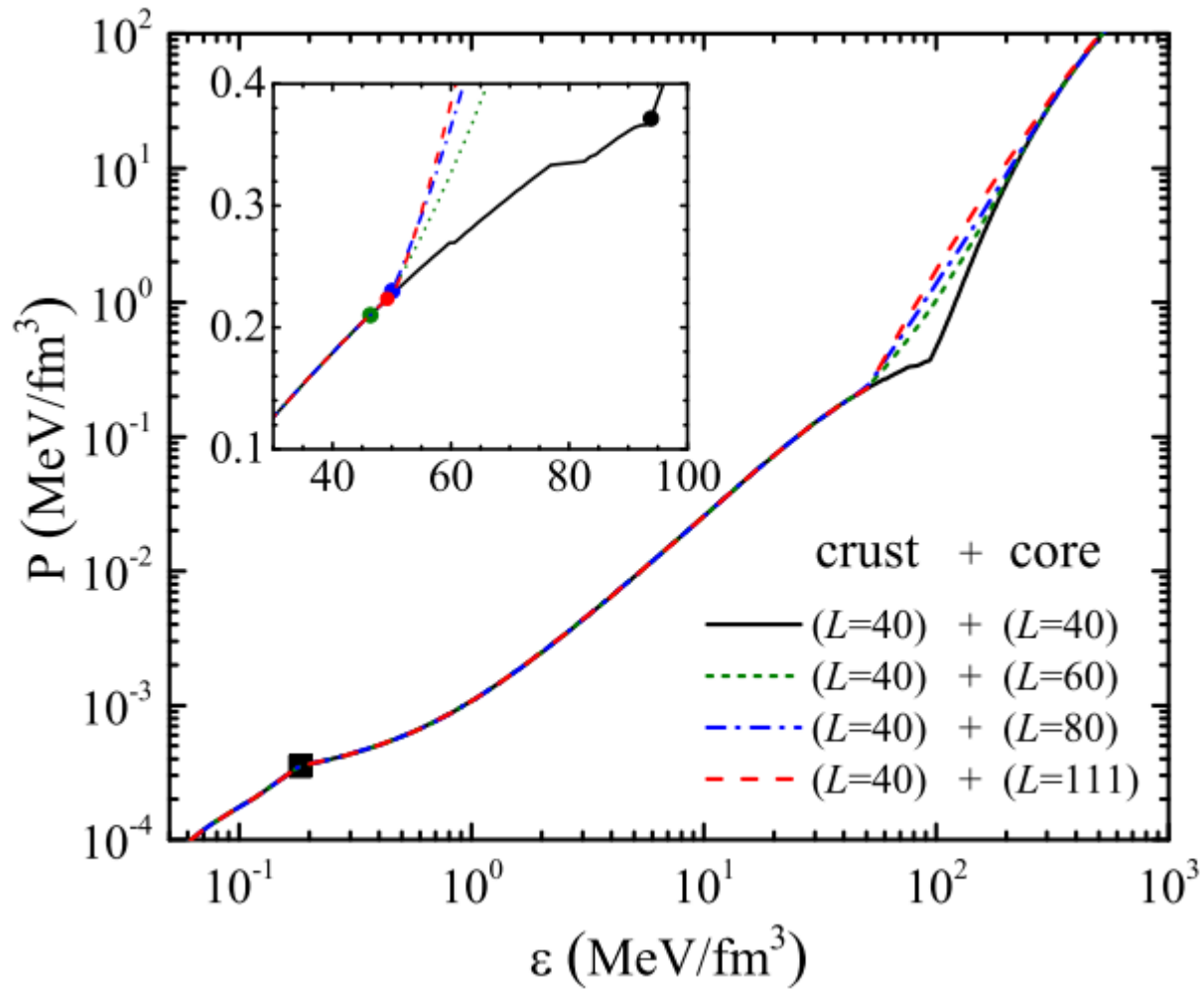


Love number  $k_2$ Tidal deformability  $\Lambda$ 

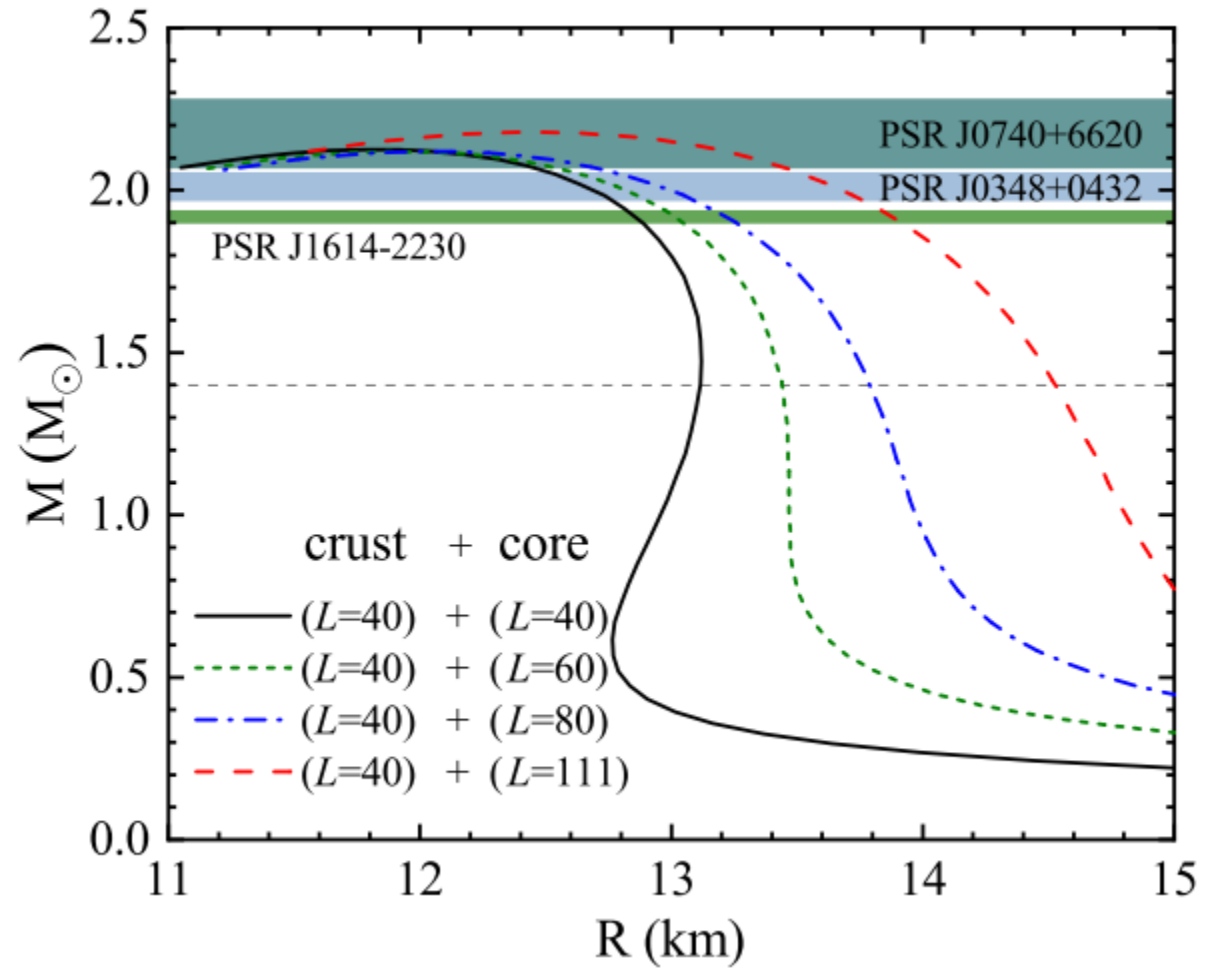
Love number  $k_2$ Tidal deformability  $\Lambda$  **$k_2$  is sensitive to crust EOS**

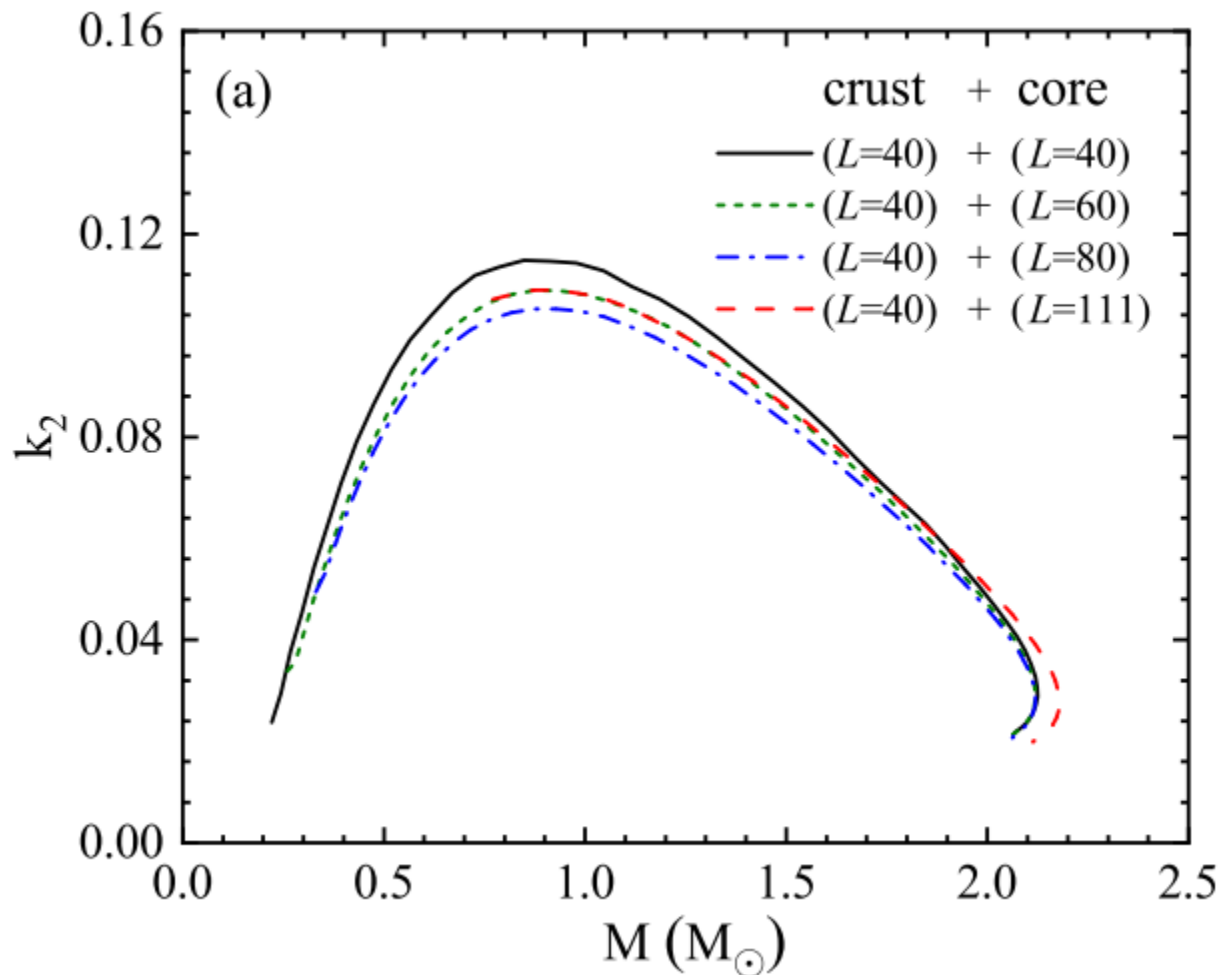
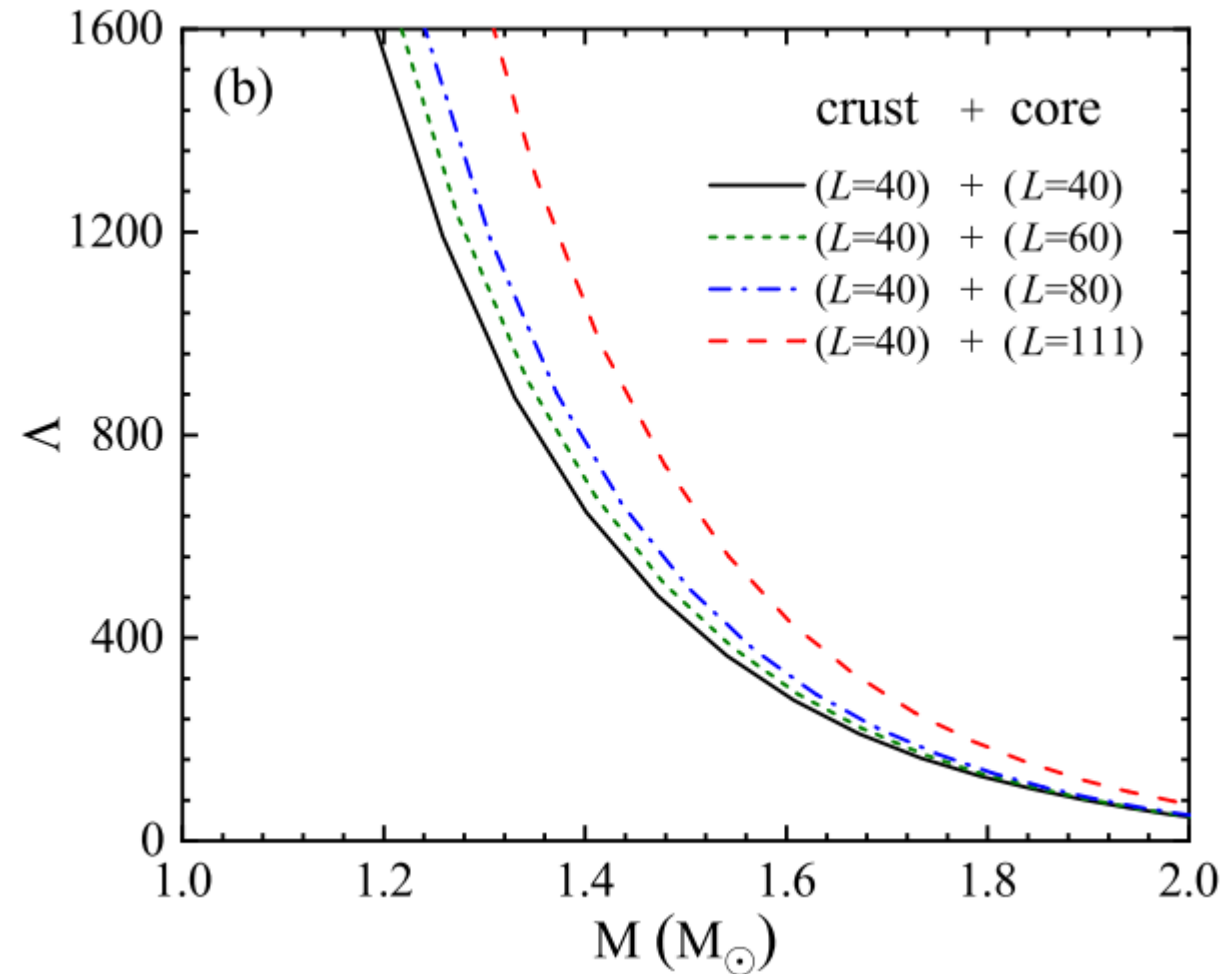
Love number  $k_2$  **$k_2$  is sensitive to crust EOS**Tidal deformability  $\Lambda$  **$\Lambda$  is insensitive to crust EOS**

## EOSs



## Mass-radius relations



Love number  $k_2$ Tidal deformability  $\Lambda$ 



- ◆ The model with a **small  $L$**  predicts a **large crust-core transition density**.
- ◆ A **small  $L$**  corresponds to a **small neutron-star radius** and a **small tidal deformability**.
- ◆ The effect of the core EOS on the tidal deformability  $\Lambda$  is more significant than the one of the crust EOS .
- ◆ Both the crust and core EOSs could significantly affect neutron star properties such as the radius and tidal deformability.



*Thank you!*