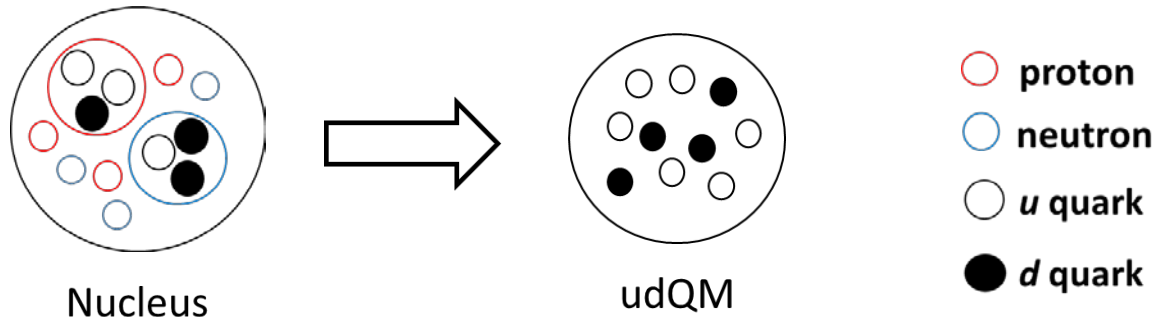


Are giant nuclei in supernova matter stable with respect to deconfinement?

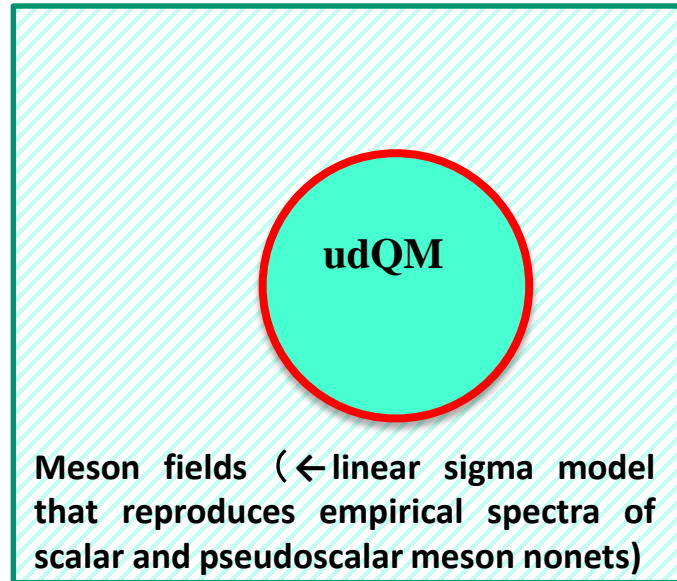
Tsukiho (月歩) Fujie (藤江), Kei Iida (Kochi University, Japan)

We consider whether or not nuclei in supernova cores with mass number far exceeding superheavy nuclei are stable against two-flavor quark matter.



From a nucleus to udQM via deconfinement

Stability of ud quark matter ($udQM$)



ud quark matter is predicted to be more stable than uds quark matter!

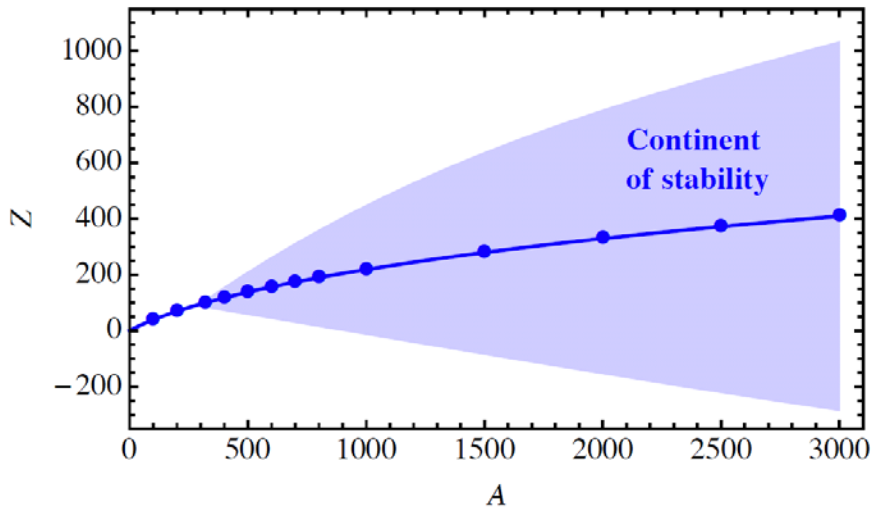


FIG. 3: The electric charge of $udQM$: full result (blue dots) and the bulk approximation (blue line).

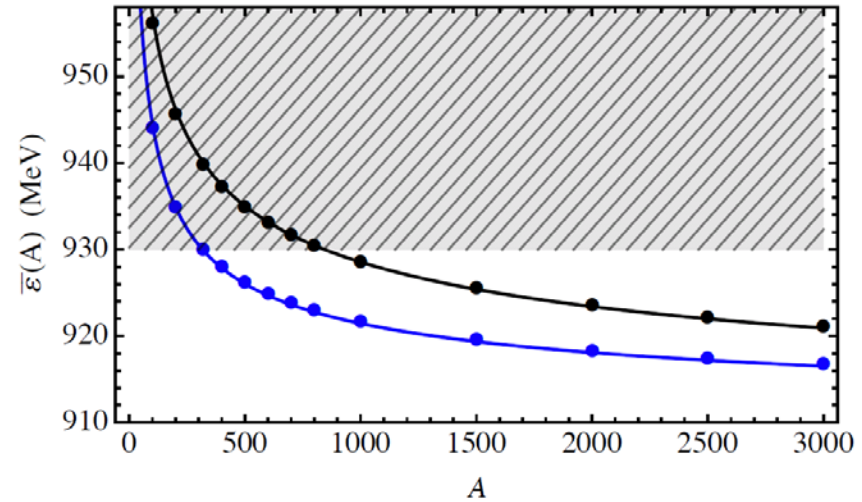


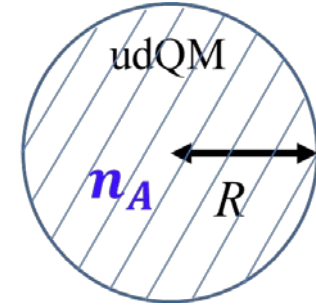
FIG. 4: The minimal energy per baryon $\bar{\epsilon}(A)$ for $udQM$ (lower), compared to the charge neutral configuration (upper).

Mass formula

A typical udQM mass formula (per baryon) [1]:

$$\varepsilon_0(A, Z) = 3\bar{p}_F \frac{n_u^{4/3} + n_d^{4/3}}{(3n_A)^{4/3}} + \frac{4\pi\Sigma R^2}{A} + \frac{3Z^2 e^2}{5AR}$$

Bulk **Surface** **Coulomb**



Averaged Fermi momentum:

$$\bar{p}_F = (3\pi^2 n_A)^{1/3}$$

Surface tension:

$$\Sigma = 19.4 \text{ MeV} \cdot \text{fm}^{-2}$$

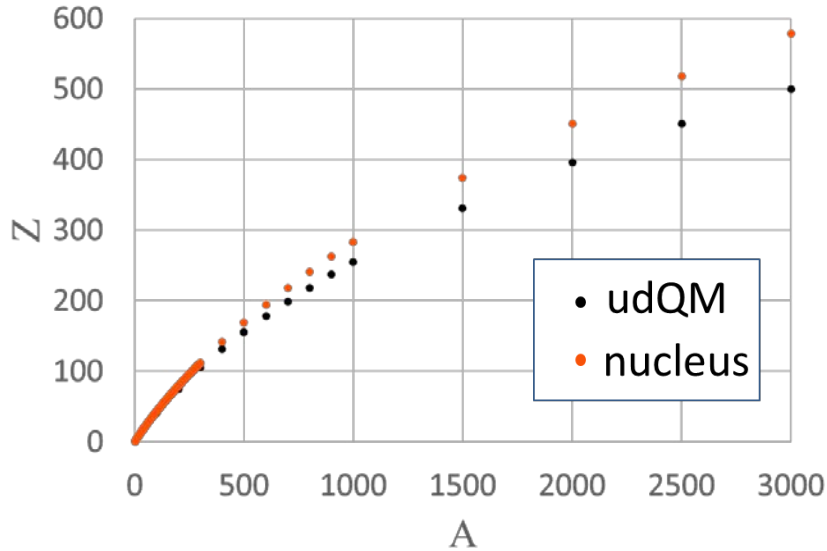
Baryon density:

$$n_A = \frac{1}{3}(n_u + n_d) = 0.23 \text{ fm}^{-3}$$

Weizsäcker-Bethe (WB) mass formula:

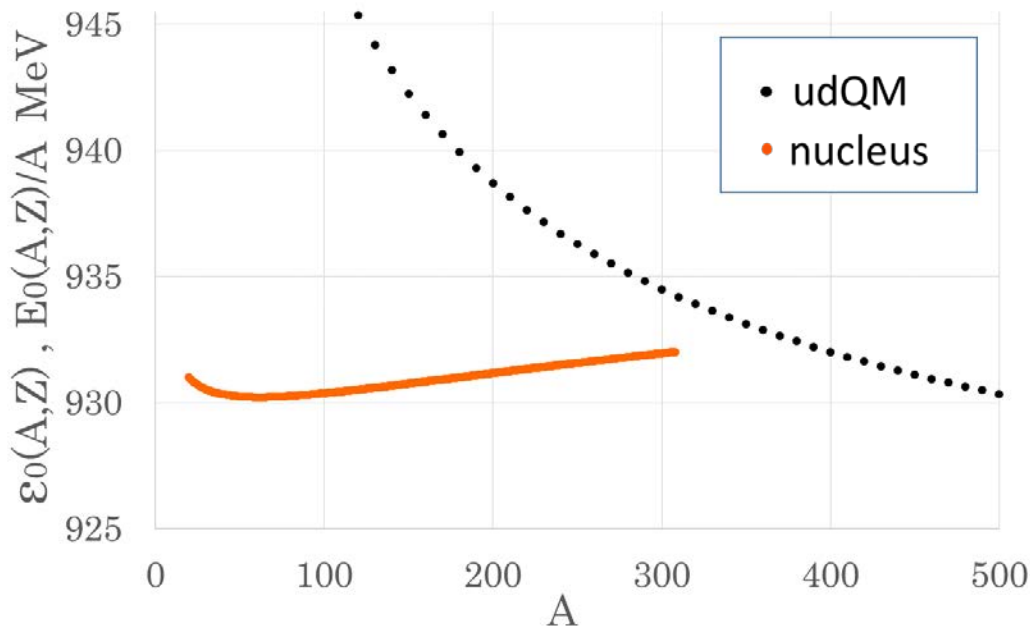
$$E_0 = NM_n + ZM_p - a_v A + a_s A^{2/3} \left[1 - b_s \left(1 - \frac{2Z}{A} \right)^2 \right] + a_I \left(1 - \frac{2Z}{A} \right)^2 A + a_c \frac{Z^2}{A^{1/3}}$$

β stability line and mass in vacuum



β stability line

Both lines are close to each other.
This is because the symmetry energy coefficient is of the same order.



Mass on the β stability line

Nuclei are more stable than udQM up to a superheavy regime.

udQM is possibly more stable for even larger mass as encountered in supernova cores, thanks to the large surface tension.

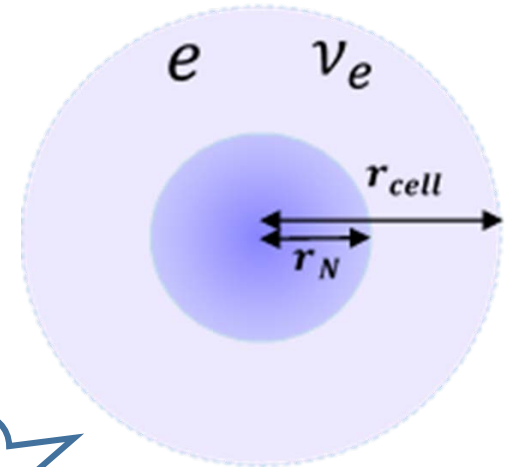
In supernova matter

In the Wigner-Seitz approximation:

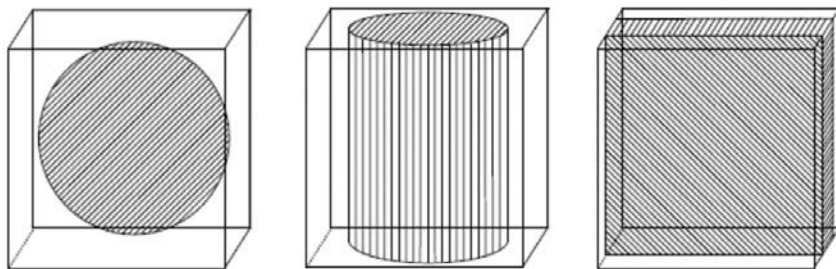
Coulomb term in the WB formula modified by electrons by a factor of

$$f(u) = 1 - \frac{3}{2}u^{1/3} + \frac{1}{2}u$$

A sphere in which a nucleus is embedded in a uniform neutralizing background of electrons.



Wigner-Seitz cell [2]



Sphere

Rod

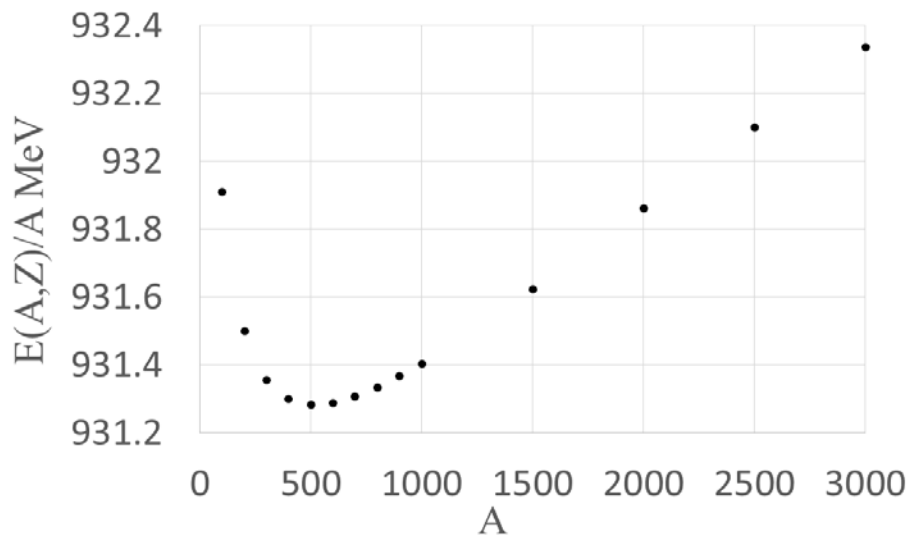
Slab

Changes in nuclear shape

$$\text{Volume fraction: } u = \left(\frac{r_N}{r_{\text{cell}}} \right)^3$$

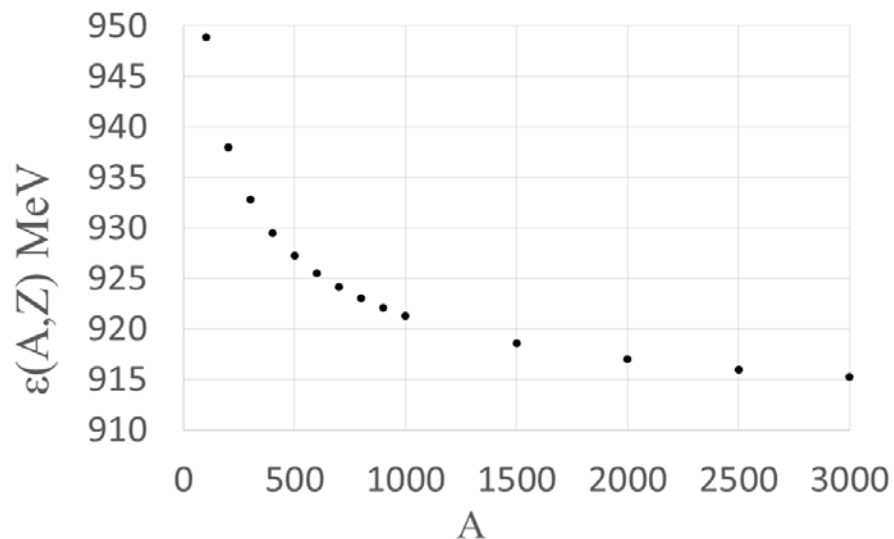
Shape of nuclei in supernova matter changes from sphere to rod around $u = 0.2$.

In supernova matter



Nuclear mass

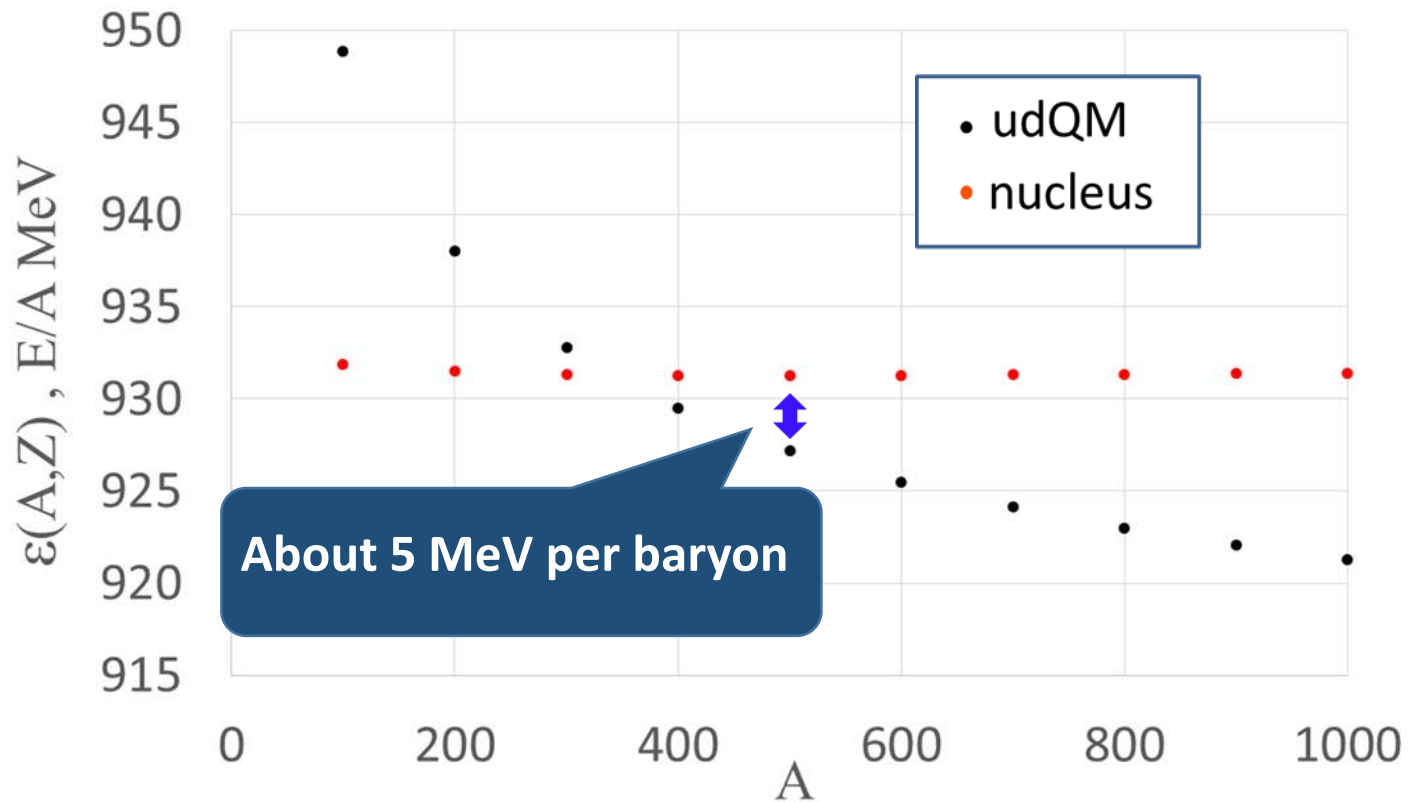
Most stable around $A \sim 500$
(minimum $E/A = 931.28$ MeV)



Deconfined udQM mass

Energy per baryon of udQM of the same A and Z in supernova matter; the Coulomb term is modified by electrons of the same density.

Comparison of nuclear mass and deconfined udQM mass



Astrophysical implications

- As a result of deleptonization and cooling, the neutron star might have a crust of which the deepest region is composed of udQM.
- Electron screening might play a role in determining the optimal A of the nucleus and udQM in supernova matter.
- We will reconstruct the mass formulas by including the effect of electron screening.