

DM as a Portal to New Physics @ APCTP

Fermion portal dark matter and muon anomalies

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arXiv:2002.12534, 1706.04344

[JHEP]

[PRD]

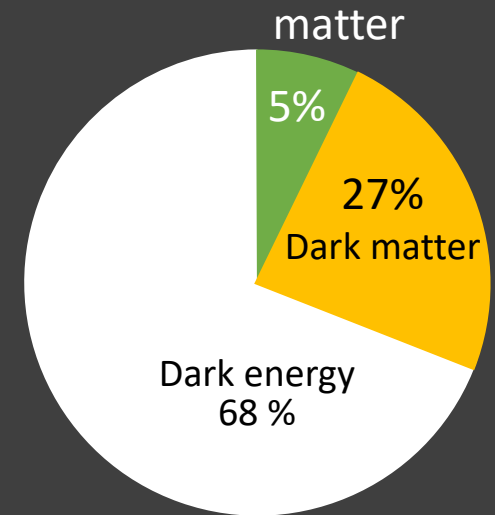
in collaboration with

Y.Omura [Kindai U., Japan] and S.Okawa [Victoria U., Canada]

Dark Matter [DM]

➤ dark matter

- dark and cold (particle)
- 27% of energy of the universe
- discovered only by gravitational int.

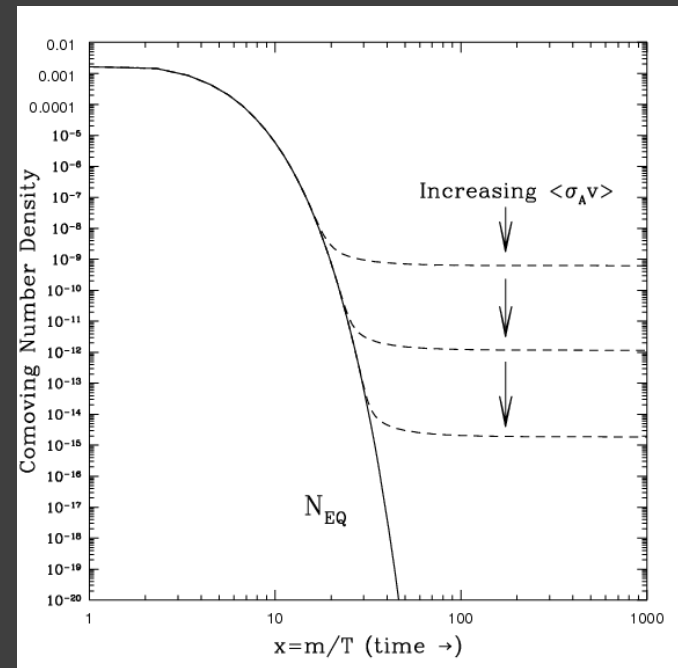
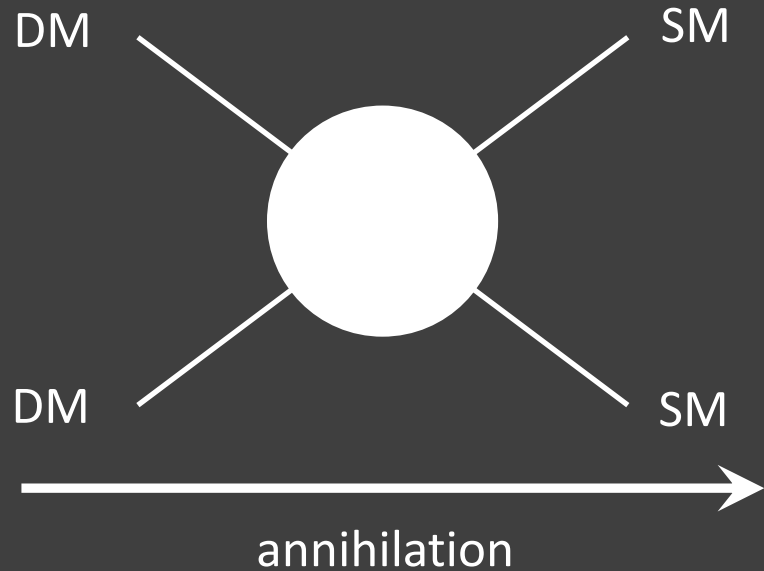


➤ particle candidates

- Weakly Interacting Massive Particle [WIMP]
- axion, ALP
- SIMP, FIMP, asymmetric, self-interacting, ...

WIMP is still an interesting candidate

Freeze-out of WIMP



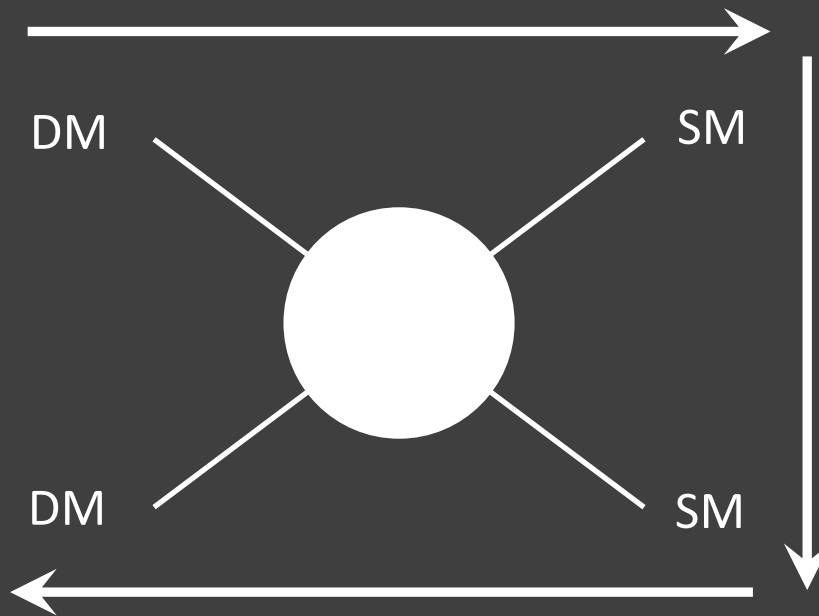
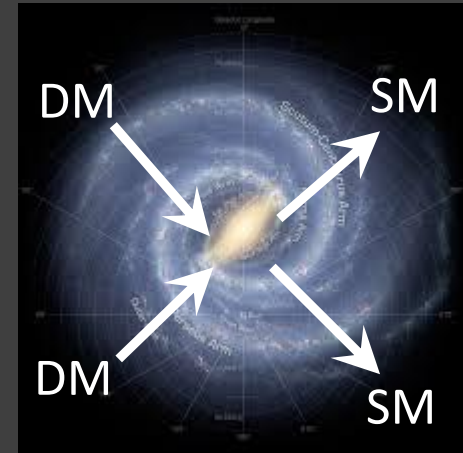
E.W.Kolb, M.S.Turner,
The Early Universe, '89

- DM decouples from thermal bath and “freeze-out”
- Electro-Weak [EW] coupling and mass can explain relic density
- WIMP can be in beyond SM e.g. models for muon anomalies

Probes of WIMP

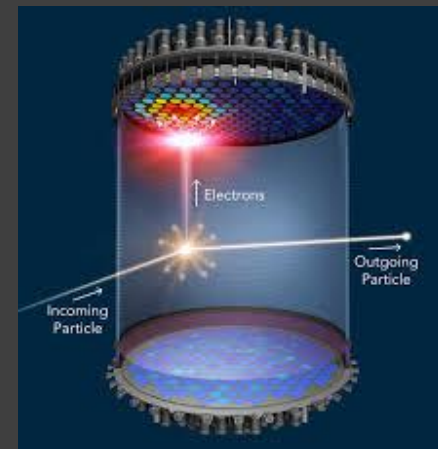
➤ annihilation

- indirect detection
- annihilation in DM rich env.
- e.g. Fermi-LAT, CTA, HESS,



➤ scattering

- direct detection
- scattering with nucleus/e
- e.g. XENON, PANDA, LZ



➤ production at collider

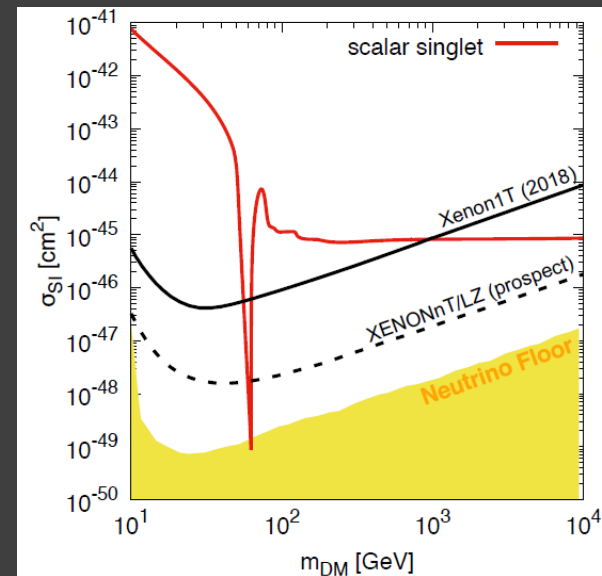
- usually by mono-X searches
- e.g. LHC, LEP, ILC(?) ...

Minimal WIMP models

➤ SM + EW singlet DM



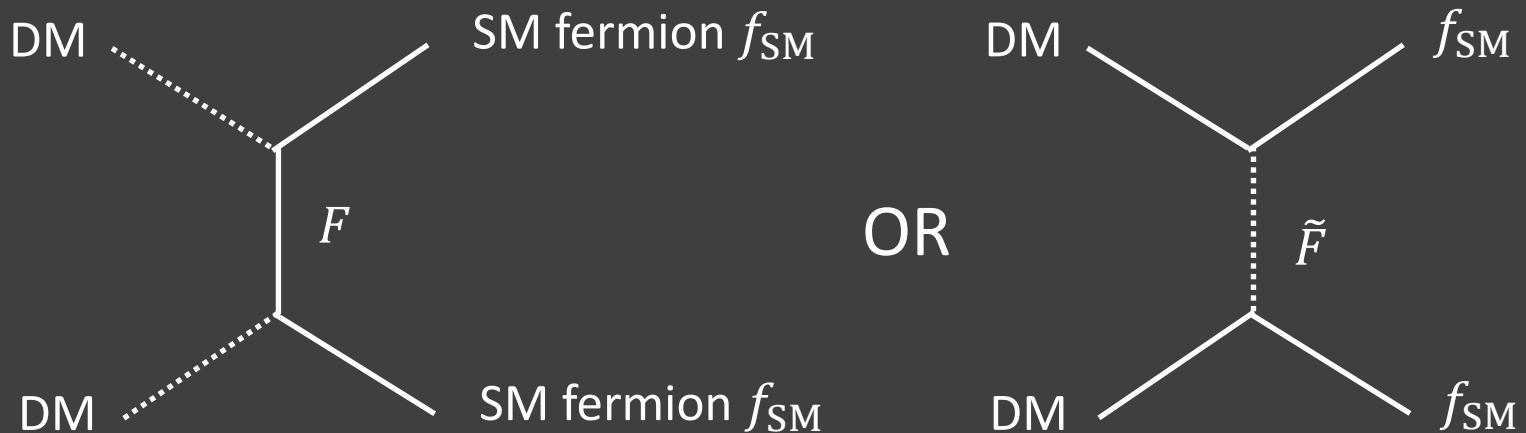
- quartic coupling $X^2 H^\dagger H$ and DM mass are the parameter
- direct detection excludes most region
- resonant or heavy region still alive



Fermion portal model

1308.0612, 1402.6696 Y.Bai, J.Berger

➤ SM + EW singlet DM + mediator



- Yukawa coupling, DM and mediator masses are parameter
- co-annihilation of DM and mediator occurs if degenerate
- pure bino + slepton in SUSY is in this class
- We focus on EW singlet DM cf. non-singlet case:

0512090 M.Cirelli, N.Fornengo, A.Strumia (DM)

1804.00009, L.Calibbi, R.Ziegler, J.Zupan (DM+g-2)

Outline

1. Introduction
2. minimal lepton portal dark matter
3. simultaneous explanation with muon anomalies
4. Conclusion

Minimal lepton portal model

➤ SM + EW singlet DM + 1 mediator (s)lepton

DM is

$\left\{ \begin{array}{l} 1. \text{ scalar} \\ 2. \text{ fermion} \end{array} \right.$ $\left\{ \begin{array}{l} a. \text{ self-conjugate} \\ b. \text{ complex} \end{array} \right.$ →

[1a] real scalar

1405.6917, A.Ibarra et.al

[1b] complex scalar

1812.07004, JK, S.Okawa et.al

[2a] Majorana fermion

1403.4634 Garny et.al ,
1401.6457 Kopp et.al

[2b] Dirac fermion

1503.03382 A.Ibarra, S.Wild

mediator is

$\left\{ \begin{array}{l} 1. \text{ fermion} \\ 2. \text{ scalar} \end{array} \right.$ $\left\{ \begin{array}{l} i. \text{ EW singlet} \\ ii. \text{ EW doublet} \end{array} \right.$

there are $2 \times 2 \times 2 = 8$ possibilities

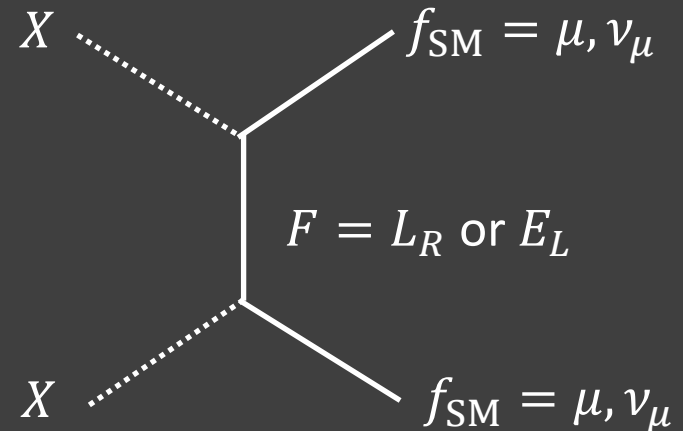
Scalar DM models

➤ singlet mediator E_L

$$\mathcal{L} \supset m_E \bar{E}_L E_R + \lambda_R \bar{E}_L X \mu_R$$

➤ doublet mediator L_R

$$\mathcal{L} \supset m_L \bar{L}_L L_R + \lambda_L \bar{\ell}_2 X L_R \quad \ell_2 = \begin{pmatrix} \mu_L \\ \nu_{\mu L} \end{pmatrix}$$



- fermion mediator should be vector-like
- Yukawa coupling is non-zero only for muon
- Higgs portal is neglected

➤ Fermion DM models

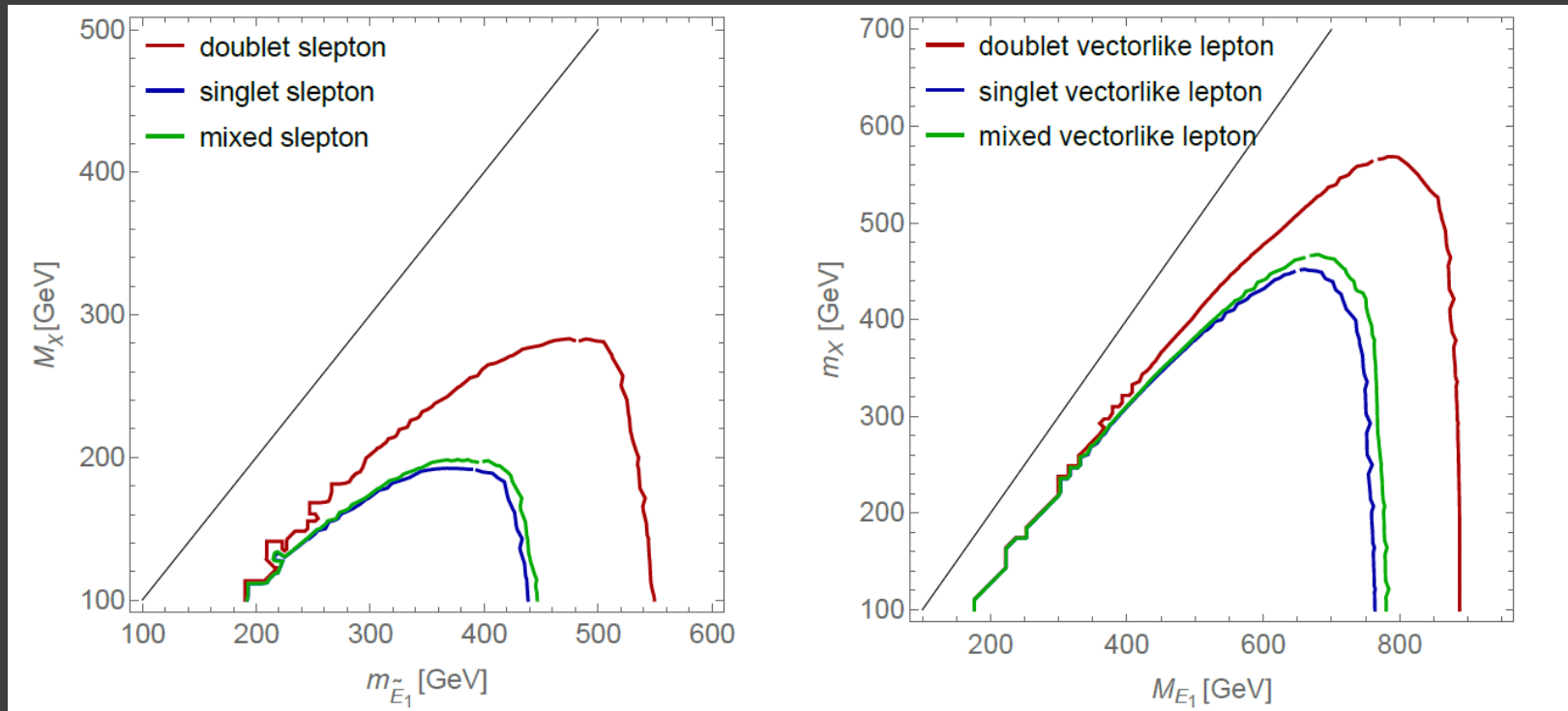
- mediator is “s”lepton (complex scalar)
- special case of Majorana DM (= bino) is realized in SUSY

LHC limits

mediator decays to DM and muon

→ $pp \rightarrow LL \rightarrow \mu\mu + \text{MET}$ is the same as SUSY slepton signal

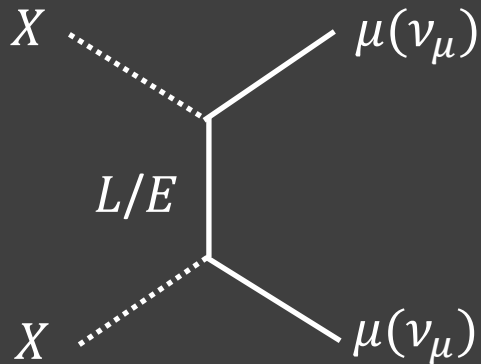
limit from 139 fb^{-1} data at ATLAS [1908.08215]



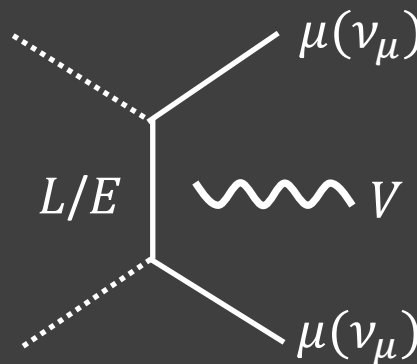
FeynRules, Madgraph5

Annihilation

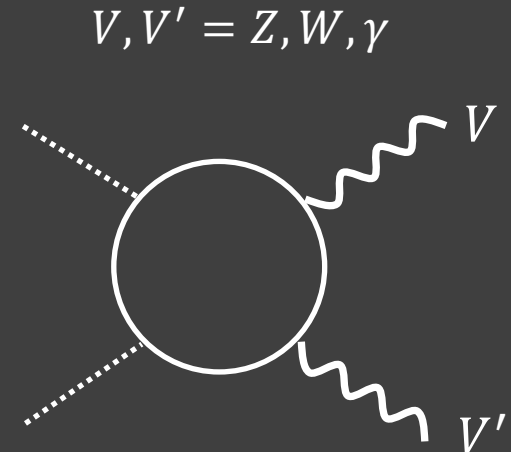
➤ Processes



$$XX^{(\dagger)} \rightarrow \mu\mu$$



$$XX^{(\dagger)} \rightarrow \mu\mu + V$$



$$XX^{(\dagger)} \rightarrow VV'$$

➤ 2-2 annihilation

velocity expansion: $\sigma v = a + b v^2 + c v^4 + \dots$

s-wave p-wave d-wave

$\langle v^2 \rangle \simeq 0.24, \langle v^4 \rangle \simeq 0.1$
at freeze-out

- s-wave is helicity suppressed, i.e. $\propto m_\mu^2/m_X^2$, except Dirac DM
- p-wave is also helicity suppressed for real DM

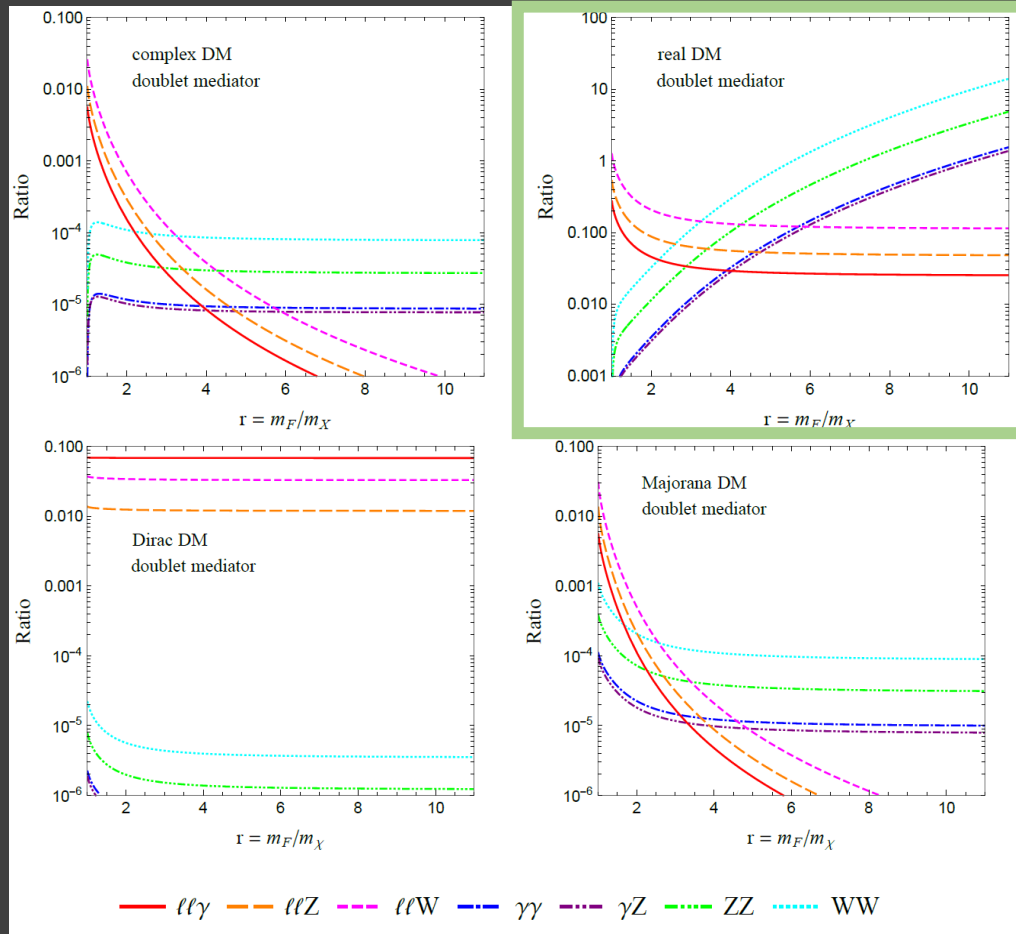
Annihilation

relative importance of higher-order processes

$$\text{Ratio} = \frac{\langle \sigma(XX \rightarrow \mu\mu V / VV') v \rangle}{\langle \sigma(XX \rightarrow \mu\mu) v \rangle}$$

$$m_X = 500 \text{ GeV}$$

$$r = m_L / m_X$$



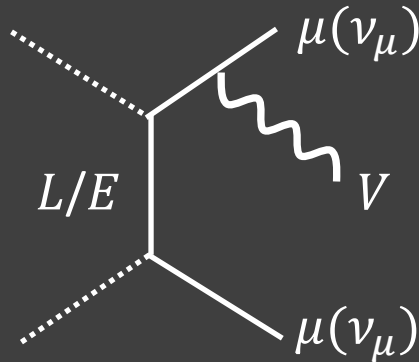
- higher-order processes can be sizable for real DM
- these are less than 0.1 for other cases

Virtual Internal Bremsstrahlung

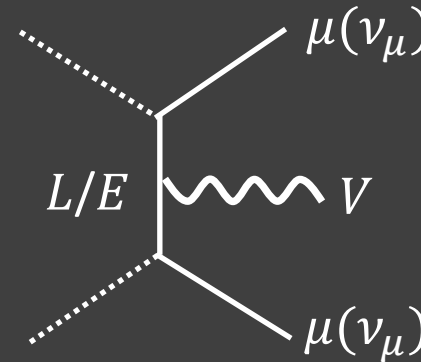
e.g. 1203.1312

T.Bringmann, X.Huang et.al

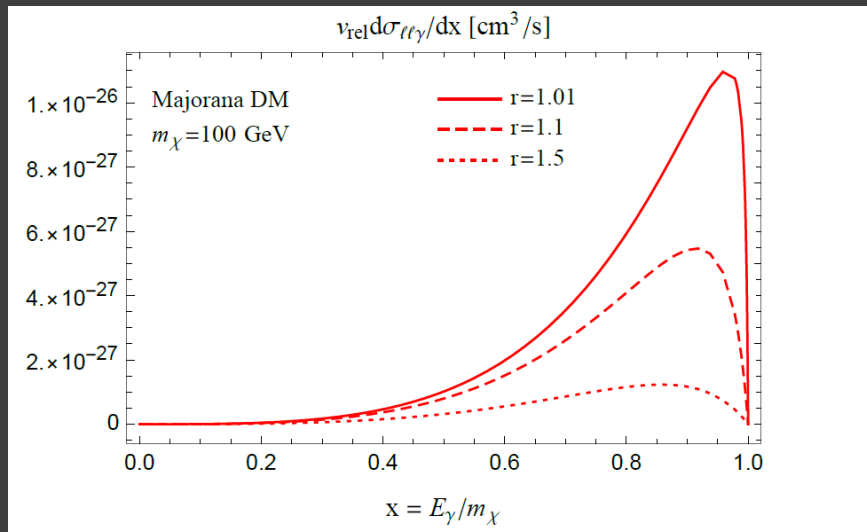
Final State Radiation [FSR]



Virtual Internal Bremsstrahlung [VIB]



➤ photon spectrum from VIB



$$r = m_L / m_X$$

- peak at $E_\gamma \sim m_X$ if $m_L \sim m_X$
- γ from $XX \rightarrow \gamma\gamma, Z\gamma$ also has sharp spectral structure

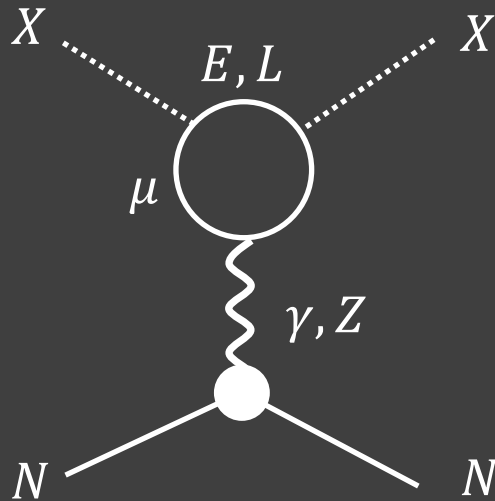
1405.6917

A.Ibarra, T.Toma et.al

Direct detection

0907.3159, J.Kopp et.al

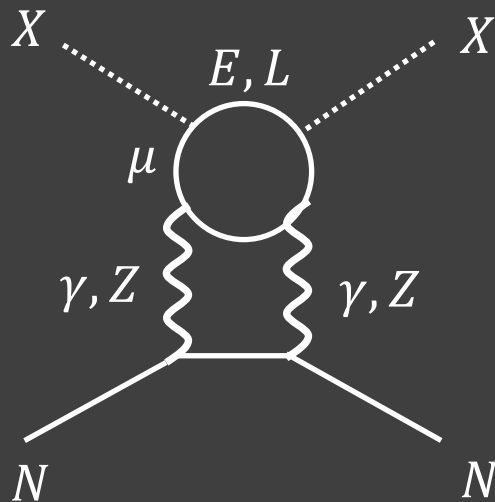
tree-level is absent



➤ 1-loop penguin

$$\rightarrow \mathcal{L}_{\text{eff}} \supset C i (X^\dagger \partial_\mu X - \partial_\mu X^\dagger \cdot X) \bar{N} \gamma^\mu N$$

- dominant in complex scalar DM
- vanishing for real scalar DM



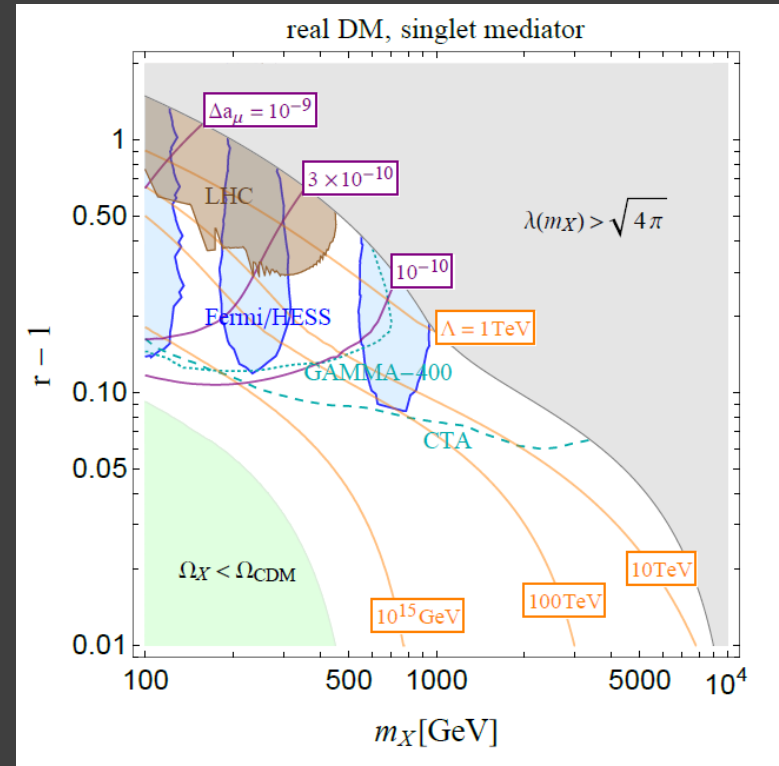
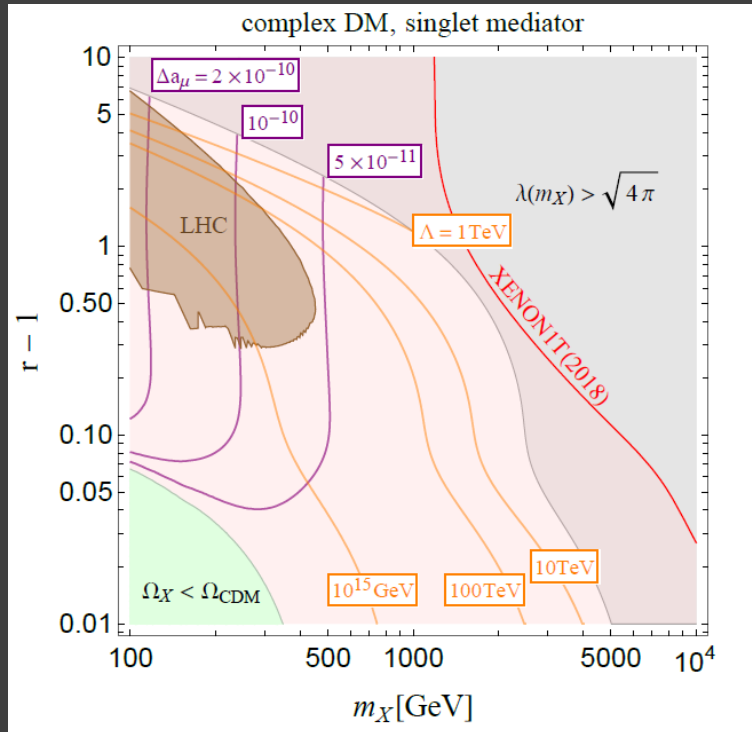
➤ 2-loop two photon exchange

- dominant in real scalar DM
- very much suppressed

Current status of scalar DM

$$r = m_E/m_X$$

Yukawa is fixed to explain thermal relic density via (co-)annihilation



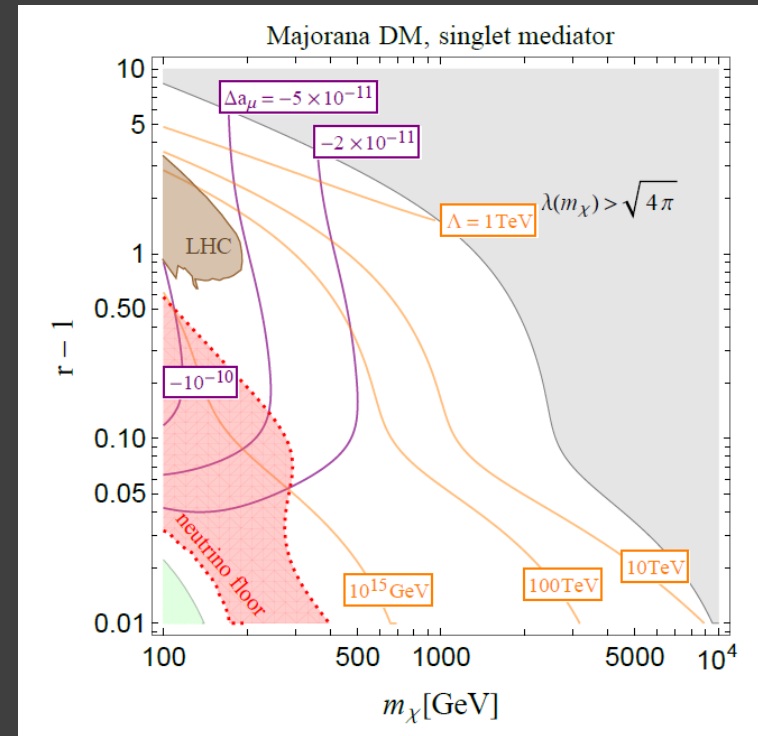
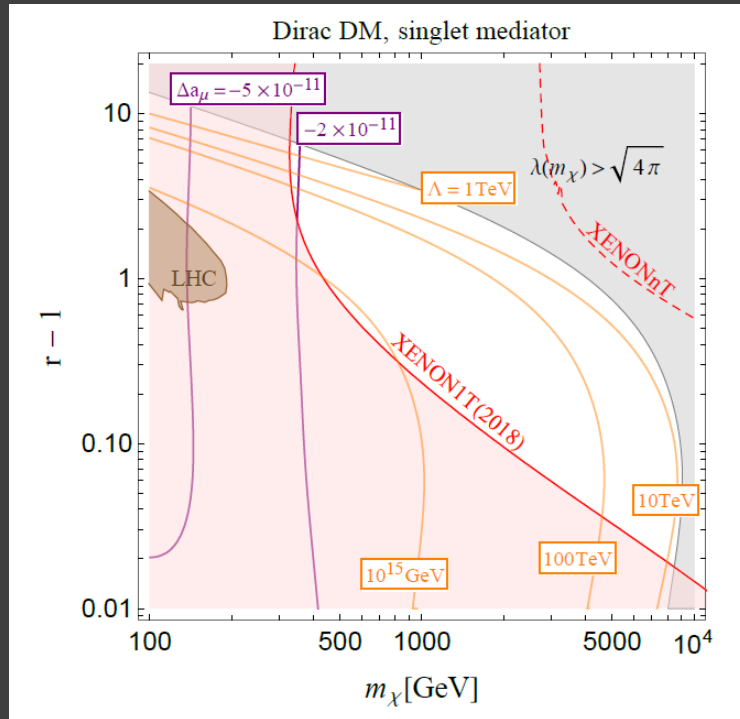
MicroOmegas

- ✓ excluded by direct detection
- ✓ Δa_μ is too small
- co-annihilation is needed for abundance
- direct detection bound is absent
- indirect detections give bounds

Current status of fermion DM

$$r = m_E/m_X$$

Yukawa is fixed to explain thermal relic density via (co-)annihilation



MicroOmegas

- ✓ XENON excludes wide region
- ✓ Δa_μ is too small

- p-wave allows larger mass difference
- direct detection bound is absent
- indirect detections give no bound

Summary of minimal models

	real	complex	Majorana	Dirac
relic density $XX \rightarrow \mu\mu$	d-wave	p-wave	p-wave	s-wave
direct det. $XN \rightarrow XN$	2-loop	1-loop	1-loop ν -suppressed	1-loop
indirect det. $\sigma_{\mu\mu\gamma}/\sigma_{\mu\mu}$	$\gtrsim 0.1$	$\lesssim 0.1$	$\lesssim 0.1$	$\lesssim 0.1$

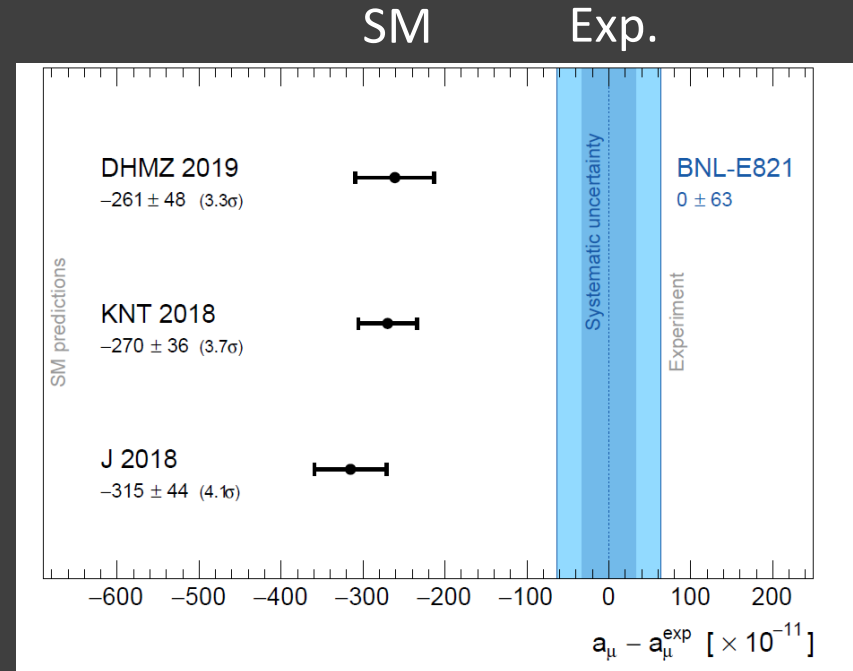
- complex/Dirac DM is strongly constrained by XENON
- real DM is partially constrained by indirect detections
- Majorana DM is less constrained
- Analytic formulas are in paper

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Muon $g - 2$

$$\begin{aligned}\Delta a_\mu &= a_\mu^{\text{exp}} - a_\mu^{\text{SM}} \\ &= 2.61 (63)(48) \times 10^{-9} \\ &\sim 3.3 \sigma\end{aligned}$$



PDG2020

- discrepancy is resolved if lattice result for hadronic contribution is true
- we would have new experimental result soon

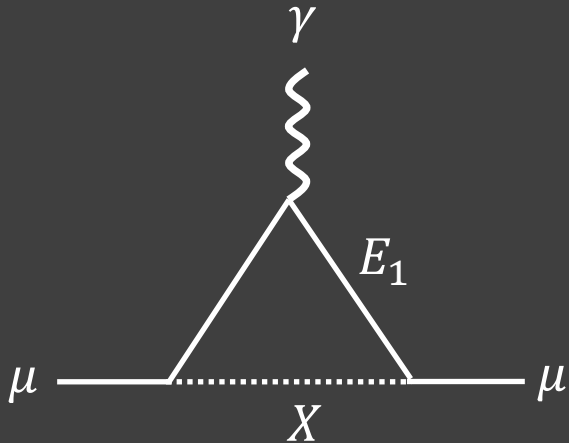
Δa_μ in lepton portal model

➤ SM + singlet DM + 2 mediator (s)leptons

$$\mathcal{L} \supset \lambda_L \bar{\ell}_L X L_R + \lambda_R \bar{E}_L X^* \mu_R + \kappa \bar{L}_L H E_R \quad E'_{L(R)} \in L_{L(R)}$$

$$\rightarrow \begin{pmatrix} E'_R \\ E_R \end{pmatrix} = \begin{pmatrix} c_R & s_R \\ -s_R & c_R \end{pmatrix} \begin{pmatrix} E_{R_1} \\ E_{R_2} \end{pmatrix}, \quad \begin{pmatrix} E'_L \\ E_L \end{pmatrix} = \begin{pmatrix} c_L & s_L \\ -s_L & c_L \end{pmatrix} \begin{pmatrix} E_{L_1} \\ E_{L_2} \end{pmatrix}$$

mixing is induced by Yukawa coupling κ



$$\Delta a_\mu \sim \frac{m_\mu}{16\pi^2 m_X^2} [\lambda_L \lambda_R c_R s_L m_{E_1} + \mathcal{O}(m_\mu)]$$

sizable Δa_μ comes only from mixing

Correlation to DM density

➤ Annihilation rate

$$\langle\sigma v\rangle\sim\frac{|\lambda_L\lambda_R|^2}{\pi}\left(\frac{c_{RS_L}m_{E_1}}{m_X^2+m_{E_1}^2}-\frac{c_{LS_R}m_{E_2}}{m_X^2+m_{E_2}^2}\right)^2$$

no suppression by muon mass in the s-wave contribution

➤ Correlation to Δa_μ

$$\langle\sigma v\rangle\sim 3\times 10^{-26}\text{ [cm}^3\text{/s]}$$

➔ $\Delta a_\mu\sim\frac{m_\mu}{16\pi^2}\sqrt{2\pi\langle\sigma v\rangle}\sim 5\times 10^{-8}$ is too **large** if maximal mixing

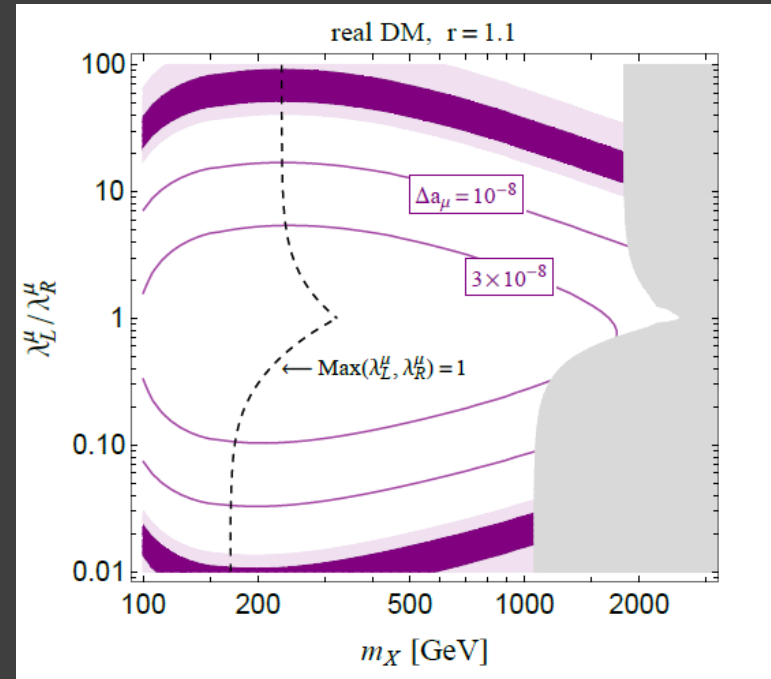
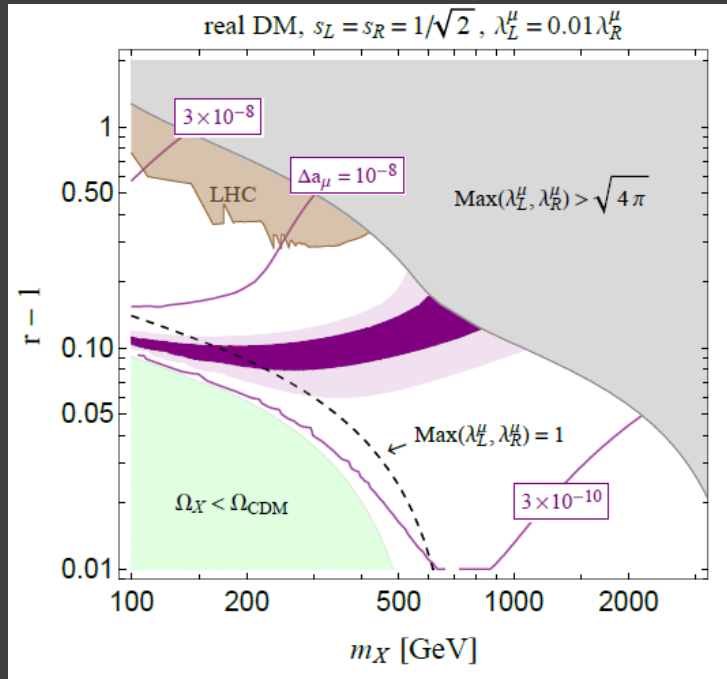
➔ co-annihilation and/or $\lambda_L\ll\lambda_R$ ($\lambda_R\ll\lambda_L$)
and/or non-maximal mixing is/are needed

Result in real DM

λ_R is fixed to explain relic density

$$m_{E_2} - m_{E_1} = 100 \text{ GeV}$$

$$r = m_{E_1}/m_X$$



MicroOmegas

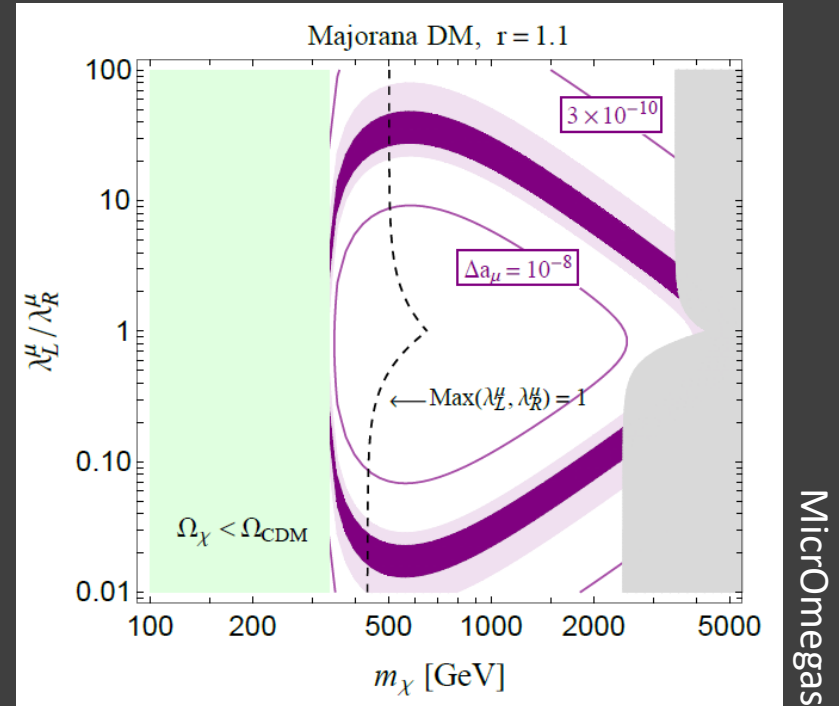
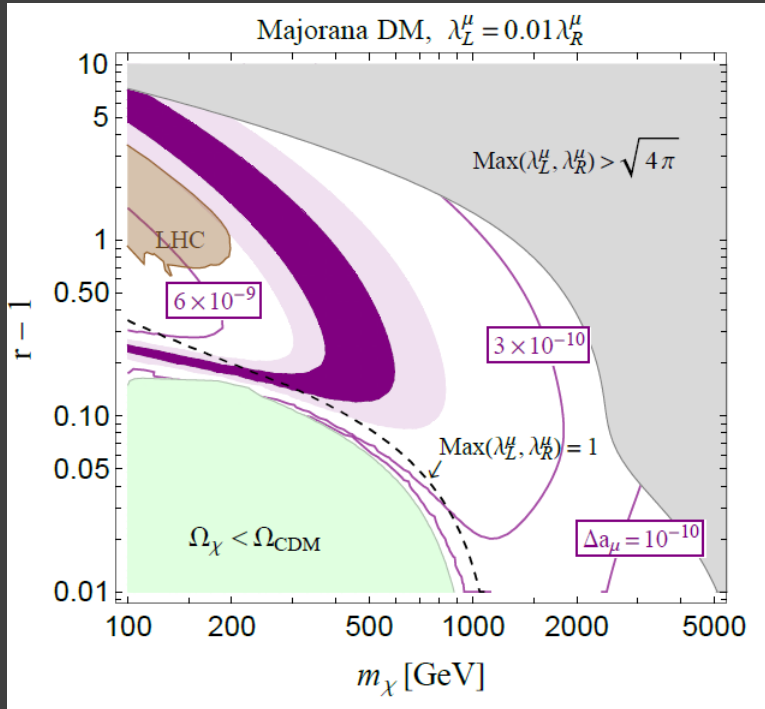
Δa_μ can be explained if $m_{E_1} \sim 1.1 \times m_X$ and $\lambda_L \sim 0.01 \times \lambda_R$

Result in Majorana DM

λ_R is fixed to explain relic density

$$m_{E_2} - m_{E_1} = 100 \text{ GeV}$$

$$r = m_{E_1} / m_X$$



- Δa_μ can be explained if $m_{E_1} \sim 1.1 \times m_X$ and $\lambda_L \sim 0.01 \times \lambda_R$
- requirement for degeneracy is relaxed due to p-wave contribution

$b \rightarrow s\ell\ell$ anomaly

$$\mathcal{H}_{eff} = -\frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* \frac{\alpha}{4\pi} \sum_{j=9,10} (C_j \mathcal{O}_j + C'_j \mathcal{O}'_j) + h.c.$$

$$\mathcal{O}_9^{(\prime)\mu} = (\bar{s}\gamma_\mu P_{L(R)} b)(\bar{\mu}\gamma^\mu \mu) \quad \mathcal{O}_{10}^{(\prime)\mu} = (\bar{s}\gamma_\mu P_{L(R)} b)(\bar{\mu}\gamma^\mu \gamma_5 \mu)$$

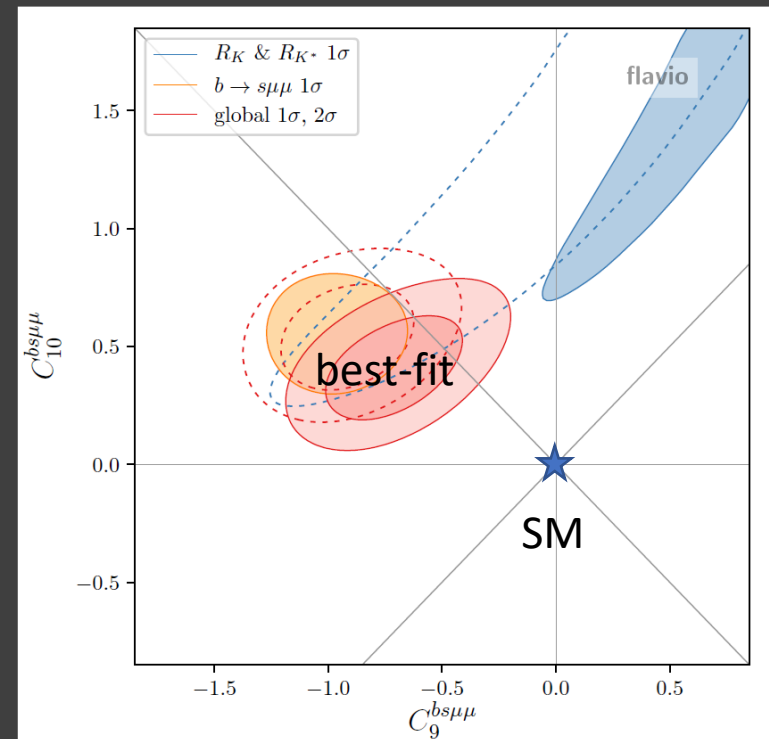
➤ anomalies in B decays

- $R_K = 0.846^{+0.060}_{-0.054} \quad ^{+0.016}_{-0.014}$ is 2.5σ below the SM prediction
- Branching ratios in $B \rightarrow \phi\mu\mu, K\mu\mu$ are $(2 - 3)\sigma$ below the SM pred.
- discrepancy in angular observables

combined



$$\sqrt{\chi_{SM}^2 - \chi^2} > 6\sigma$$



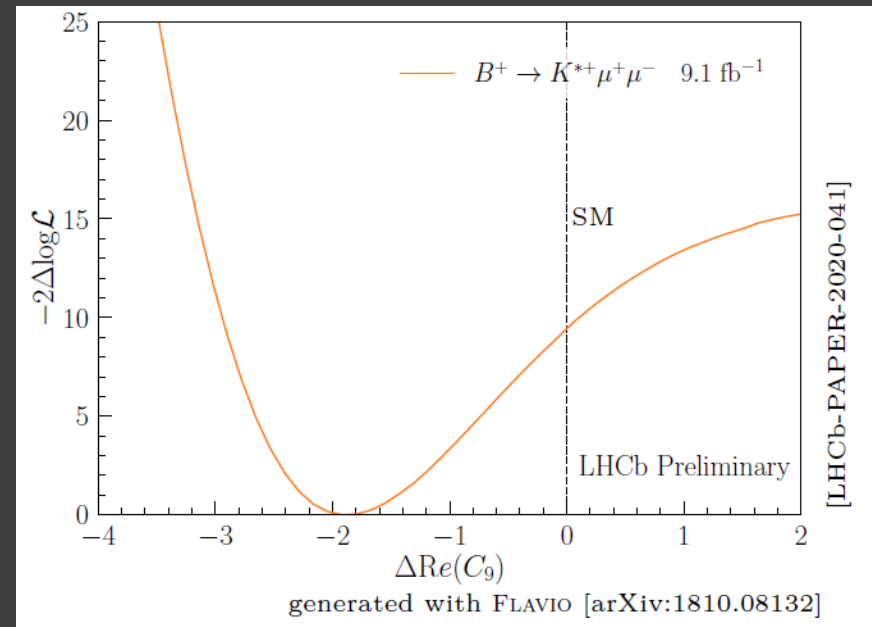
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➤ anomalies in B decays

- new result on $B^+ \rightarrow K^{*+} \mu^+ \mu^-$ also favors $\text{Re } C_9 \sim -1.9$
- Significance from SM is 3.1σ



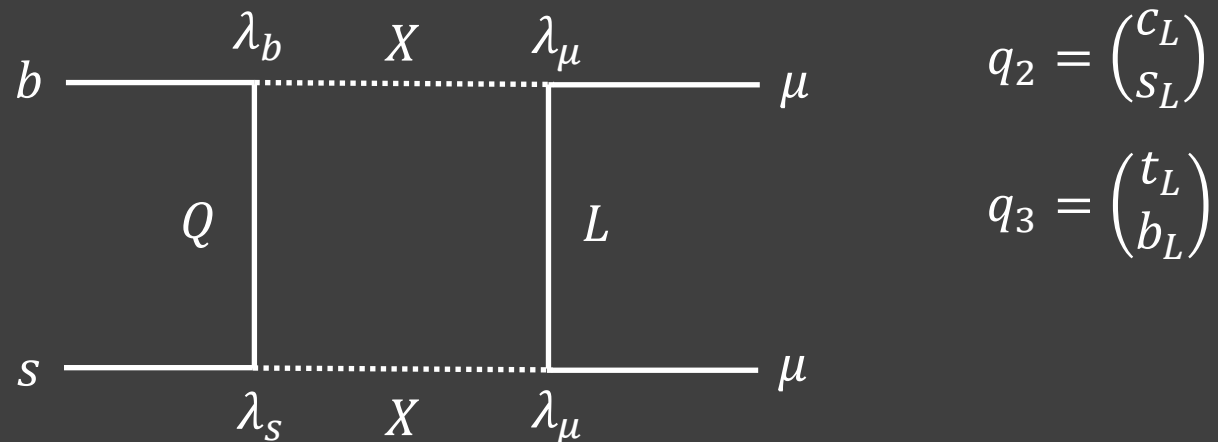
Explanation in fermion portal

preferred pattern may be LL-type: $C_9 = -C_{10} \sim -0.5$

$$\mathcal{O}_9^\mu = (\bar{s}\gamma_\mu P_L b)(\bar{\mu}\gamma^\mu \mu) \quad \mathcal{O}_{10}^\mu = (\bar{s}\gamma_\mu P_L b)(\bar{\mu}\gamma^\mu \gamma_5 \mu)$$

➤ Complex DM X + doublet VL quark Q + VL lepton L

Yukawa coupling: $\mathcal{L} \supset \lambda_\mu \bar{\ell}_2 X L_R + \lambda_b \bar{q}_3 X Q_R + \lambda_s \bar{q}_2 X Q_R$

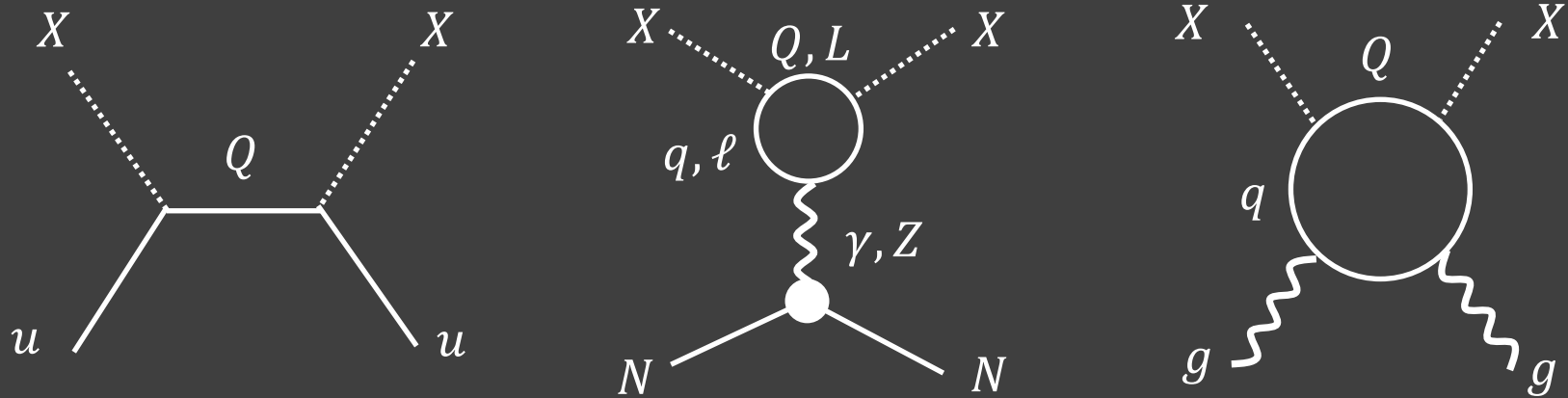


flavor violation is necessary in quark sector $\longrightarrow B_s - \bar{B}_s, D - \bar{D}$ mixing

Direct detection

VL quark mediator affects to direct detection significantly

➤ Processes



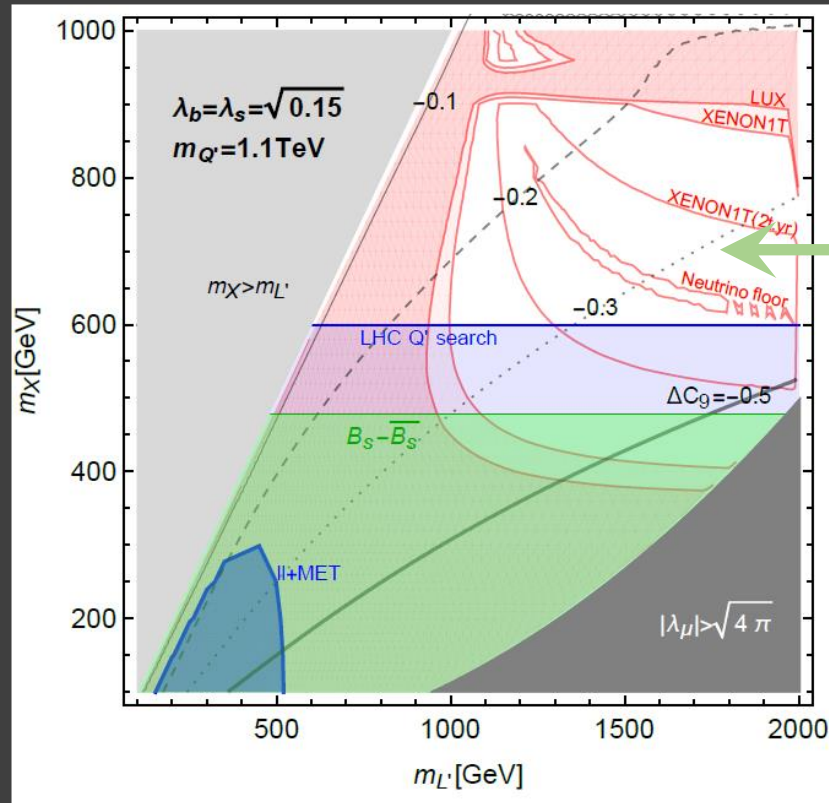
- there is, in general, tree-level scattering via CKM mixing $\propto \lambda_s V_{uc}$
- γ/Z penguin tends to dominate, Z -penguin enhanced by top mass
- γ and Z penguins are destructive
- gluon scattering is subdominant

Result

λ_μ is fixed to explain relic density. Typically $\lambda_\mu \sim 2$

1706.04344

JK, Y.Omura, S.Okawa



LHC limit: 36 fb^{-1}

$C_9 = -0.3$

* complex DM

- $C_9 = -C_{10} \sim -0.3$ is compatible with LHC limit and direct detection
- cancellation in direct detection rate happens

Summary

➤ Muon $g - 2$

- both singlet and doublet mediators are necessary for sizable Δa_μ
- can be explained with DM in real scalar and Majorana cases
- tends to be too big, mild tuning $O(0.1)$ may be needed

➤ $b \rightarrow s\ell\ell$

- both doublet VL quark and VL lepton are necessary
- we considered complex scalar DM
- $C_9 = -C_{10} \sim -0.3$ is possible where direct detection rate is canceled

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Conclusion

➤ Minimal lepton portal models

- we studied real, complex, Majorana and Dirac singlet DM w/ 1 mediator
- complex and Dirac DM are almost excluded by direct detection
- real DM may predict peaked signal
- Majorana DM is tough to be tested

➤ Simultaneous explanation with muon anomalies

- Δa_μ can be explained in models with singlet and doublet mediators
- $b \rightarrow s\mu\mu$ can be partially explained in narrow parameter space

Thank you !!

Backup

Direct detection of fermion DM

charge radius

magnetic dipole

anapole

electric dipole

$$\mathcal{L}_{\text{multipole}}^F = b_\chi \bar{\chi} \gamma^\mu \chi \partial^\nu F_{\mu\nu} + \frac{\mu_\chi}{2} \bar{\chi} \sigma^{\mu\nu} \chi F_{\mu\nu} + a_\chi \bar{\chi} \gamma^\mu \gamma^5 \chi \partial^\nu F_{\mu\nu} + i \frac{d_\chi}{2} \bar{\chi} \sigma^{\mu\nu} \gamma^5 \chi F_{\mu\nu},$$

$$\mathcal{L}_{\text{eff}}^F = \sum_{N=p,n} (C_{S,N} \bar{\chi} \chi \bar{N} N + C_{V,N} \bar{\chi} \gamma^\mu \chi \bar{N} \gamma_\mu N).$$

1503.03382 A.Ibarra et.al

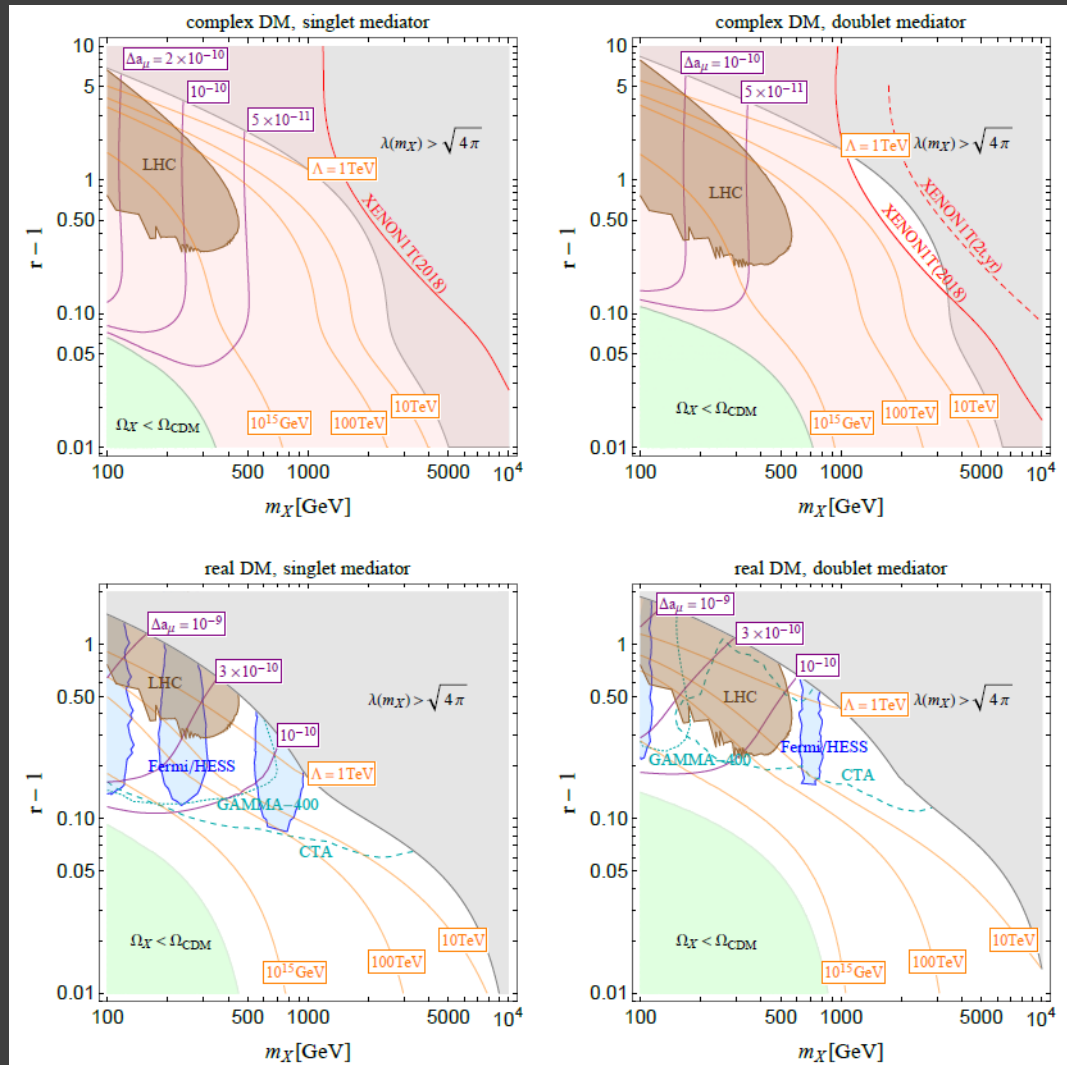


$$\begin{aligned} \frac{d\sigma}{dE_R} = & \frac{\alpha Z^2}{v^2} \left[\mu_\chi^2 \left(\frac{v^2}{E_R} - \frac{m_N}{2\mu_{\text{red}}^2} \right) + d_\chi^2 \left(\frac{1}{E_R} - \frac{1}{m_\chi} \right) \right] |F(E_R)|^2 + \frac{m_N f_A^2}{2\pi v^2} |F(E_R)|^2 \\ & + \frac{\alpha Z^2}{v^2} a_\chi^2 \left[2m_N v^2 - \frac{(m_N + m_\chi)^2}{m_\chi^2} E_R \right] |F(E_R)|^2 \\ & + \frac{m_N \mu_A^2}{2\pi v^2} (2\mu_\chi^2 + d_\chi^2 v^2 + 4m_N E_R a_\chi^2) \frac{J_A + 1}{3J_A} |F_{\text{spin}}(E_R)|^2, \\ f_A = & Z (C_{S,p} + C_{V,p} - e b_\chi - e \mu_\chi / (2m_\chi)) + (A - Z) (C_{S,n} + C_{V,n}) \end{aligned}$$

- $b_\chi = \mu_\chi = d_\chi = 0$ for Majorana DM
- anapole a_χ contribution is suppressed by velocity v or recoil energy E_R

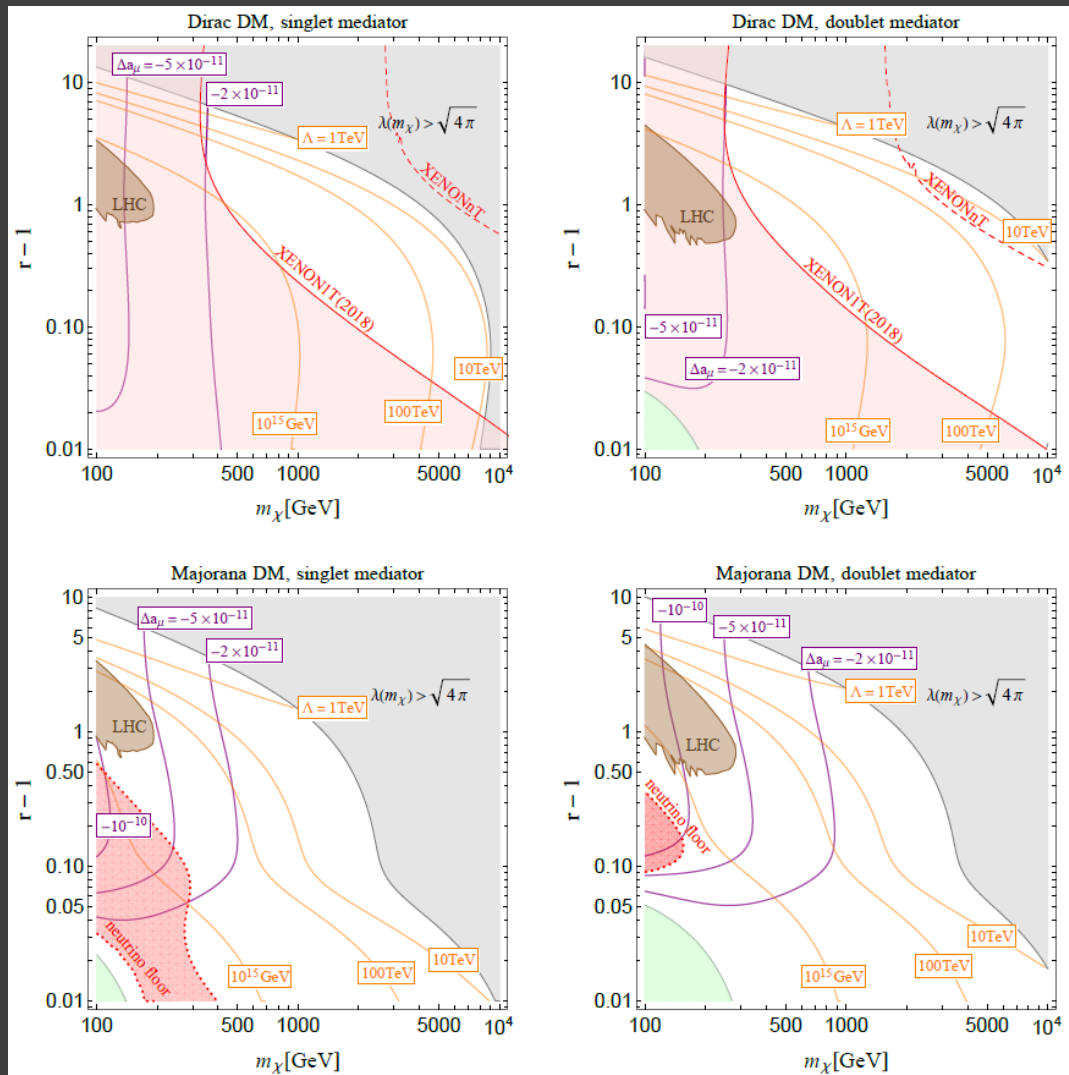
Current status of scalar DM

Yukawa is fixed to explain thermal relic density via (co-)annihilation



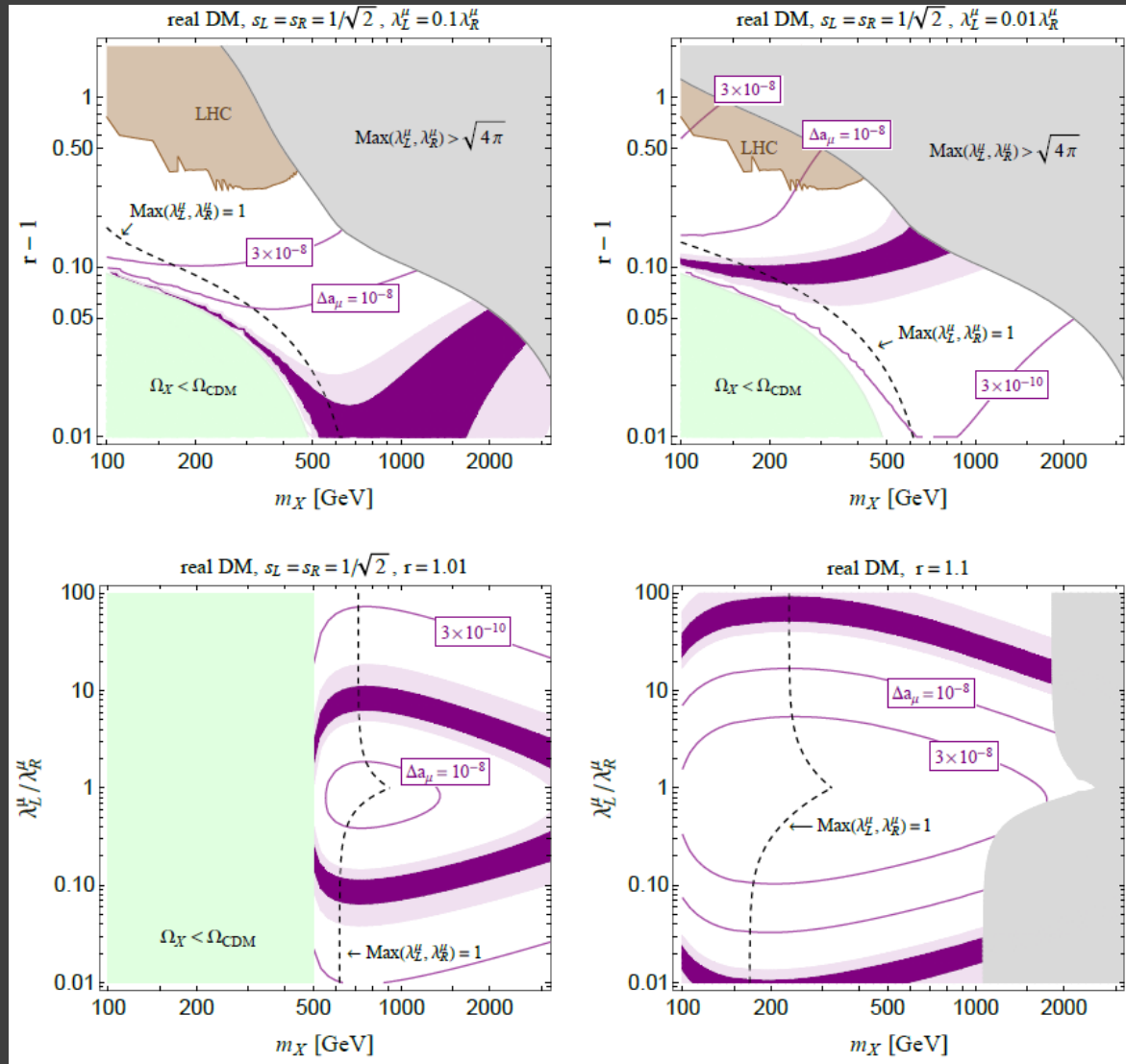
Current status of fermion DM

Yukawa is fixed to explain thermal relic density via (co-)annihilation



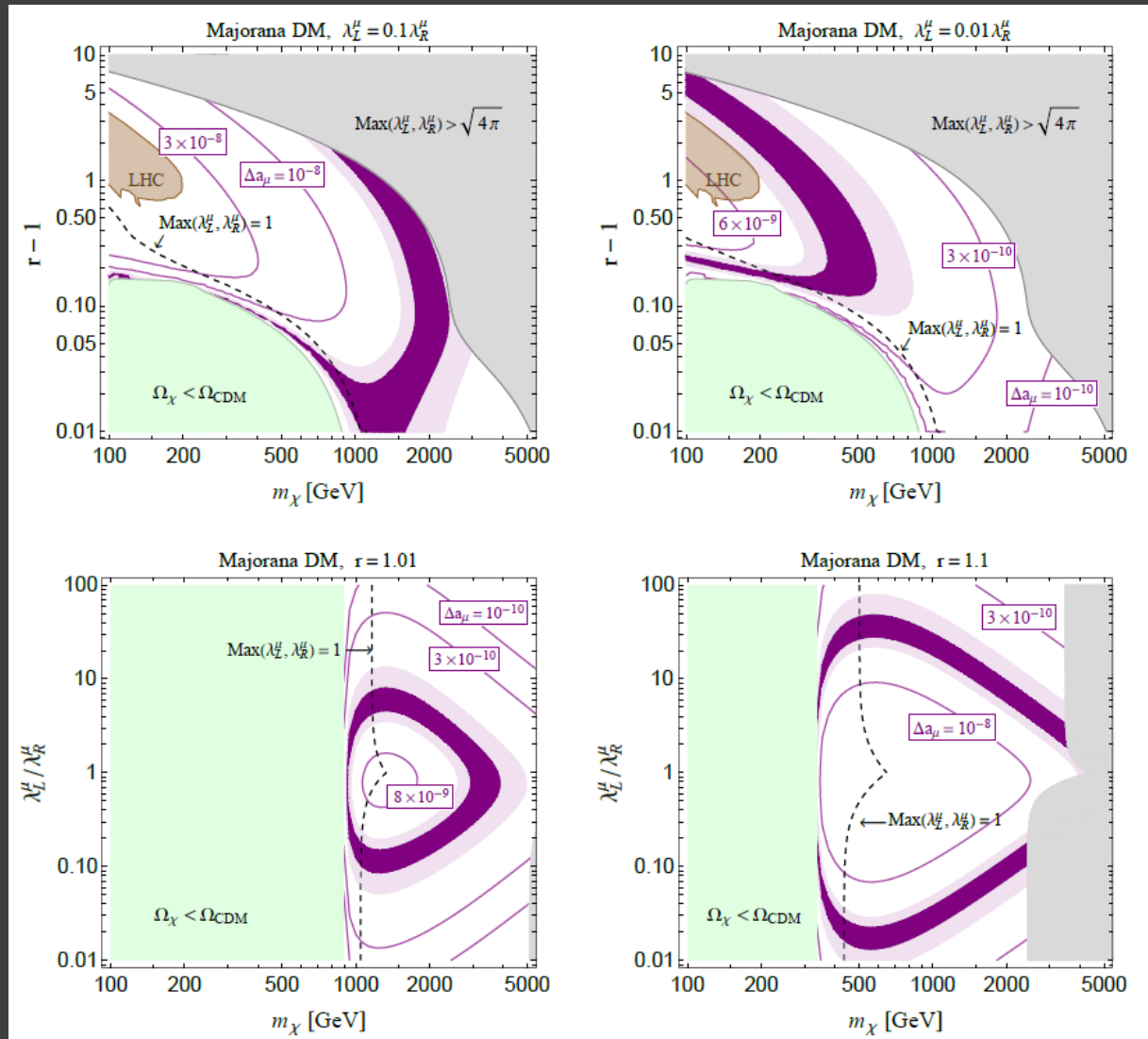
g-2 in scalar DM

Yukawa is fixed to explain thermal relic density via (co-)annihilation



g-2 in fermion DM

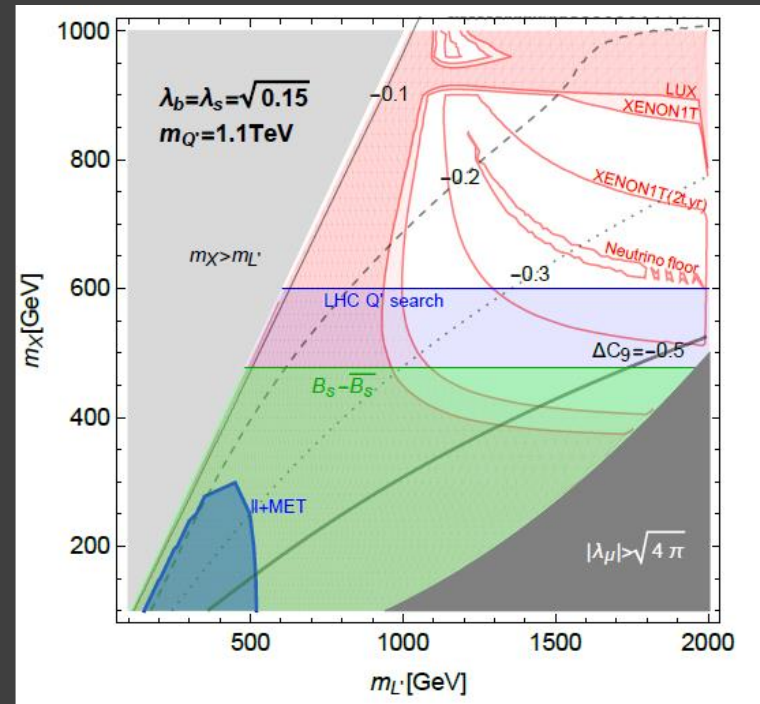
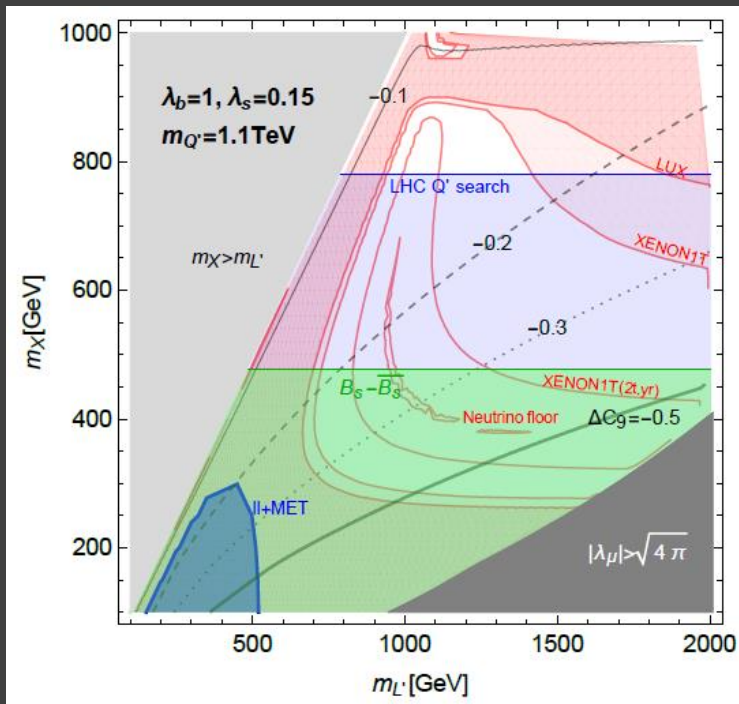
Yukawa is fixed to explain thermal relic density via (co-)annihilation



Result

λ_μ is fixed to explain relic density. Typically $\lambda_\mu \sim 2$

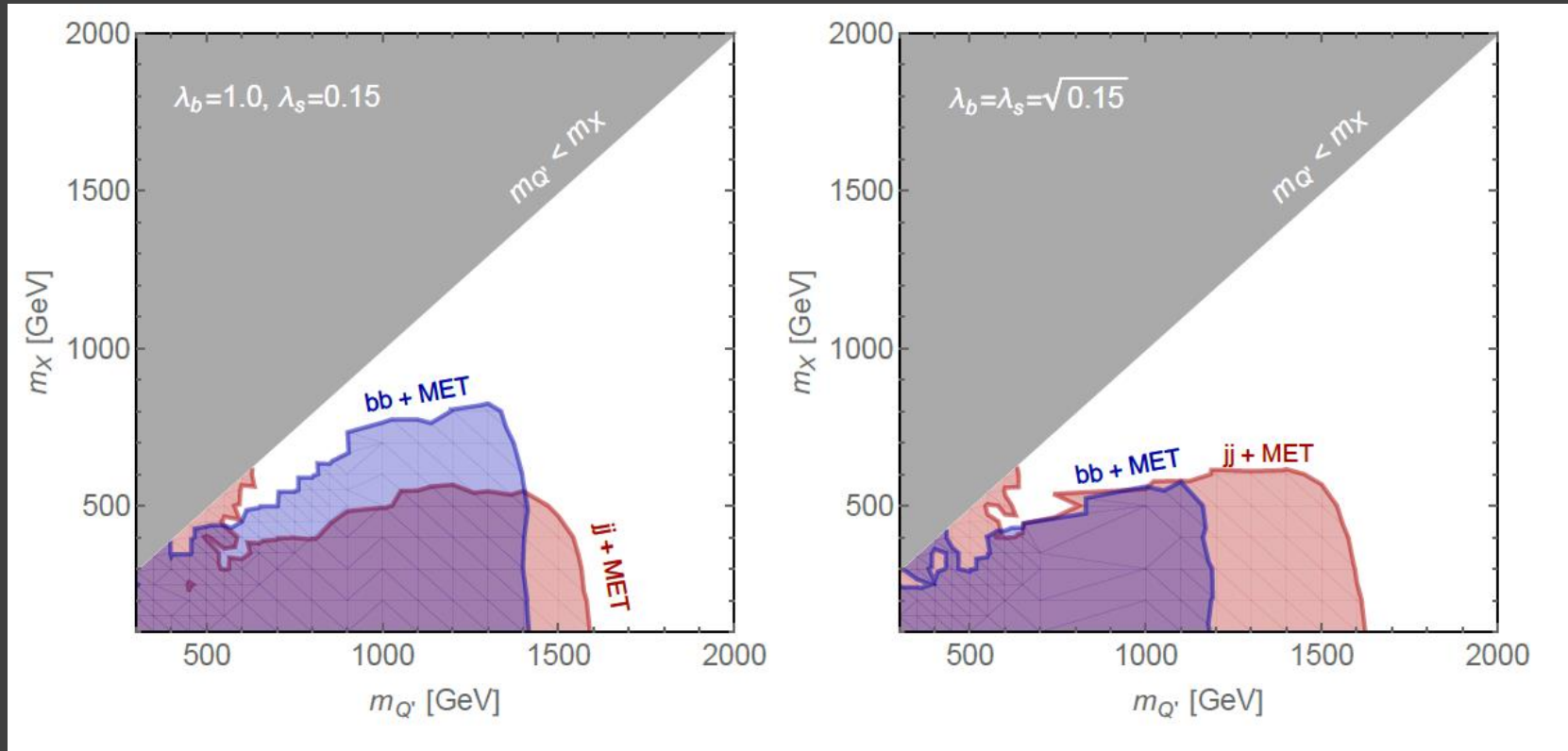
LHC limit: 36 fb^{-1}



- $C_9 = -C_{10} \sim 0.3$ is compatible with LHC limit and direct detection
- cancellation in direct detection rate happens

LHC limit on VL quark

integrated luminosity is 36 fb^{-1}



ΔC_9 vs collider constraints

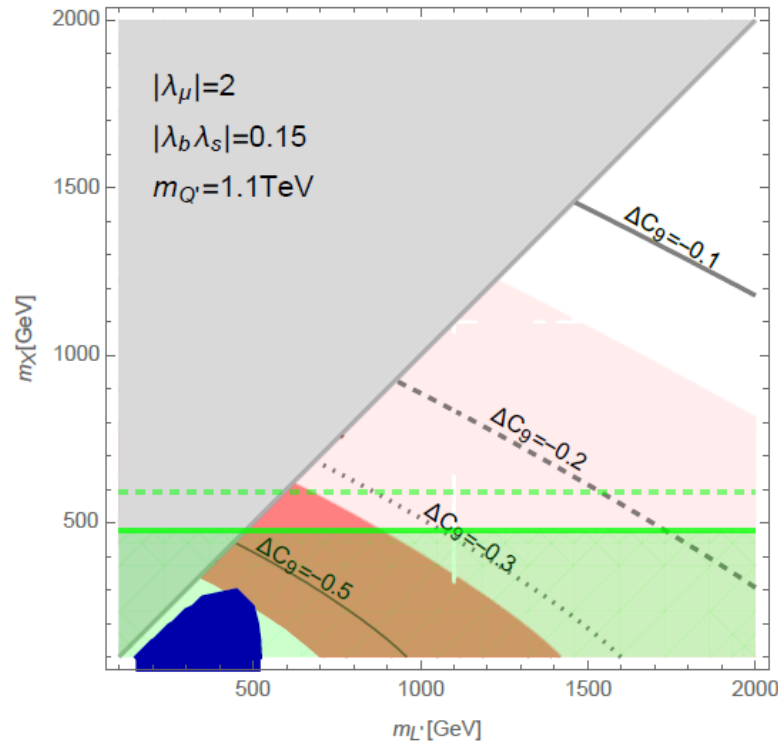


Figure 3: ΔC_9 on the plane of $m_{L'}$ and m_X with $|\lambda_\mu| = 2$, $|\lambda_b\lambda_s| = 0.15$ and $m_{Q'} = 1.1\text{ TeV}$. The size of $\Delta C_9 = -\Delta C_{10}$ on each black line is -0.1 (thick), -0.2 (dashed), -0.3 (dotted), and -0.5 (solid), respectively. The (light) red region is the 1σ (2σ) region of R_K . The (dashed) green line depicts the lower limit from $B_s - \overline{B}_s$ mixing in Eq. (7) at $m_{Q'} = 1.1\text{ TeV}$ (1 TeV). The blue region is excluded by $\mu\mu + E_T^{\text{miss}}$ at the LHC [31].