



Fermi-ball dark matter from a first-order phase transition

Ke-Pan Xie (谢柯盼) Seoul National University, Korea 2021.2.3, APCTP dark matter workshop (online)

In collaboration with Jeong-Pyong Hong and Sunghoon Jung Phys.Rev.D 102 (2020) 7, 075028 [arXiv: 2008.04430]

Dark matter as a puzzle in particle physics

• Evidences of dark matter



WIMPs and freeze-out

The "standard explanation" for DM [Lee & Weinberg, PRL1977]



The relic density is estimated as

$$\Omega_{\rm DM} h^2 \sim 0.1 \left(\frac{0.01}{\alpha_{\rm DM}}\right)^2 \left(\frac{M_{\rm DM}}{100 \text{ GeV}}\right)^2$$

Motivating the <u>weak interacting massive particles</u> (WIMPs)— "WIMP miracle"! WIMPs and freeze-out

We have been searching for WIMPs for several decades...



But only obtained null results!! We need new mechanisms?

Beyond WIMPs and freeze-out



Beyond WIMPs and freeze-out

Dark Sector Candidates, Anomalies, and Search Techniques



Ke-Pan Xie (谢柯盼), Seoul Nat'l U.



A FOPT is the decay between two vacua separated by a barrier;



Vacuum expectation values of the scalar are different inside and outside the bubbles => Mass of particles are different!

This could provide a background for very rich DM production mechanisms!

• How can we achieve a FOPT?

Unfortunately, there is no FOPT in the SM!

Two phase transitions in the SM:

- 1. Electroweak phase transition;
- 2. QCD confinement phase transition. Both are smooth crossover.

Continuous Crossover

 $0\,\mathrm{GeV}$



• How can we achieve a FOPT?

Unfortunately, there is no FOPT in the SM!

Two phase transitions in the SM:

- 1. Electroweak phase transition;
- 2. QCD confinement phase transition. Both are smooth crossover.

To get a FOPT, we need that a barrier for the (finite temperature) scalar potential.



But the SM Higgs potential doesn't have such a barrier!

Ke-Pan Xie (谢柯盼), Seoul Nat'l U.



 $0 \,\mathrm{GeV}$

• How can we achieve a FOPT?

Adding a barrier (via new physics) to trigger a FOPT!



(Use Higgs as an illustration but also apply to new physics scalars.)

• What can a FOPT do for the DM production?

The mass of a particle is discontinuous when crossing the bubble wall. This could –

□ Alter the decay of DM [Baker *et al*, PRL2017]

- □ Filter DM to the true vacuum ^[Baker et al, PRL2020; Chway et al, PRD2020]
- □ Confine quarks into DM nuggets [Witten, PRD1984; Bai et al, JHEP2018]



• What can a FOPT do for the DM production?

The mass of a particle is discontinuous when crossing the bubble wall. This could –

□ Alter the decay of DM [Baker *et al*, PRL2017]

- □ Filter DM to the true vacuum ^[Baker et al, PRL2020; Chway et al, PRD2020]
- □ Confine quarks into DM nuggets [Witten, PRD1984; Bai et al, JHEP2018]



Here we propose a novel mechanism: Fermi-ball from a FOPT.



• Summary

During a FOPT, fermions are trapped into the false vacuum to form the non-topological soliton macroscope DM candidate.



- We propose a general mechanism which requires three necessary conditions;
- Our mechanism applies to a wide varieties of new physics models.

<u>Condition 0</u>: A FOPT triggered by a scalar field ϕ .

The standard FOPT description, satisfied in a lot of models.





<u>Condition 1.1</u>: A Dirac fermion field χ interacting with ϕ .

 χ is massless outside the bubble, while massive inside the bubble.

$$\mathcal{L} \supset -g_{\chi} \bar{\chi} \chi \phi$$





<u>Condition 1.2</u>: Mass gap much larger than kinetic energy: $M_{\chi} = g_{\chi} w_* >> T_*$.

i) Large coupling g_χ >> 1; ^[Carena et al, NPB2005; Angelescu et al, PRD2019; ...]
ii) Supercooling w_{*} >> T_{*}. ^[Creminelli et al, JHEP2002; Ellis et al, JCAP2019; ...]



<u>Condition 1.2</u>: Mass gap much larger than kinetic energy: $M_{\chi} = g_{\chi} w_* >> T_*$.

i) Large coupling g_χ >> 1; ^[Carena et al, NPB2005; Angelescu et al, PRD2019; ...]
ii) Supercooling w_{*} >> T_{*}. ^[Creminelli et al, JHEP2002; Ellis et al, JCAP2019; ...]



<u>Condition 1.2</u>: Mass gap much larger than kinetic energy: $M_{\chi} = g_{\chi} w_* >> T_*$.

i) Large coupling g_χ >> 1; ^[Carena et al, NPB2005; Angelescu et al, PRD2019; ...]
ii) Supercooling w_{*} >> T_{*}. ^[Creminelli et al, JHEP2002; Ellis et al, JCAP2019; ...]







<u>Condition 2</u>: There is a χ -asymmetry: $n(\chi) > n(\overline{\chi})$,

Generally achieved in asymmetric DM models^[Kaplan et al, PRD2009; Petraki et al, IJMPA2013; ...]





<u>Condition 3</u>: χ carries a conserved <u>U(1) charge</u> Q, so that the Fermi-balls are stable.



Satisfied in $\mathcal{L} \supset -g_{\chi} \bar{\chi} \chi \phi$, which is general.



• Quantitative calculation: condition 1 -- trapping

1) In wall frame: χ in equilibrium

$$\tilde{f}_{\chi}^{\text{f.v.}}(\mathbf{p}) = \frac{1}{e^{(\gamma_b|\mathbf{p}| + \gamma_b v_b p_z - \mu_{\chi})/T_*} + 1}$$

2) Particle current

$$\tilde{J}_{\chi} = 2 \int \frac{d^3 \mathbf{p}}{(2\pi)^3} \frac{-p_z}{|\mathbf{p}|} \tilde{f}_{\chi}^{\text{f.v.}}(\mathbf{p}) \Theta(-p_z - M_{\chi}^*)$$

$$M_{\chi} = g_{\chi} w_* \qquad M_{\chi} = 0$$

Wall velocity v_b

3) Back to plasma frame: trapping fraction [Chway et al, PRD2020]



Quantitative calculation: condition 2 -- χ-asymmetry









p(T): the fraction of false vacuum in the Universe [Guth *et al* PRD1981]

$$p(T) = e^{-I(T)}, \quad I(T) = \frac{4\pi}{3} \int_{T}^{T_{c}} dT' \frac{\Gamma(T')}{T'^{4}H(T')} \left[\int_{T}^{T'} d\tilde{T} \frac{v_{b}}{H(\tilde{T})} \right]^{3}$$

p(T) decreases monotonically from 1 to 0 as the FOPT proceeds.

There are several important milestones during a FOPT.

The processing of a FOPT



1. Nucleation

p(T): the fraction of false vacuum in the Universe [Guth *et al* PRD1981]

1) True vacuum bubbles start to nucleate: $p(T_n) < 1$;

The processing of a FOPT



1. Nucleation 2. Percolation

p(T): the fraction of false vacuum in the Universe [Guth et al PRD1981]

- 1) True vacuum bubbles start to nucleate: $p(T_n) < 1$;
- 2) Bubbles form an infinite connected cluster: $p(T_p) = 0.71$;

The processing of a FOPT



1. Nucleation2. Percolation3. Fermi-ball formation

p(T): the fraction of false vacuum in the Universe [Guth et al PRD1981]

- 1) True vacuum bubbles start to nucleate: $p(T_n) < 1$;
- 2) Bubbles form an infinite connected cluster: $p(T_p) = 0.71$;
- 3) <u>False vacuum remnants are not able to form an infinite</u> <u>connected cluster</u>, and Fermi-balls are formed: $p(T_*) = 0.29$;

The processing of a FOPT



1. Nucleation2. Percolation3. Fermi-ball formation4. Todayp(T): the fraction of false vacuum in the Universe [Guth et al PRD1981]

- 1) True vacuum bubbles start to nucleate: $p(T_n) < 1$;
- 2) Bubbles form an infinite connected cluster: $p(T_p) = 0.71$;
- 3) <u>False vacuum remnants are not able to form an infinite</u> <u>connected cluster</u>, and Fermi-balls are formed: $p(T_*) = 0.29$;
- 4) Fermi-balls survive today: $p(T_0) \approx 0$.

At the 3) step, the false vacuum remnants first split then shrink:





The critical size R_* of a remnant at the end of splitting and the beginning of shrinking:

It shrinks to negligible size before another bubble containing the true vacuum is created inside it.

At the 3) step, the false vacuum remnants first split then shrink:





The critical size R_* of a remnant at the end of splitting and the beginning of shrinking:

It shrinks to negligible size before another bubble containing the true vacuum is created inside it.

Therefore

$$\Gamma(T_*)V_*\Delta t \sim 1, \quad V_* = \frac{4\pi}{3}R_*^3, \quad \Delta t = \frac{R_*}{v_b}$$

Hence the critical size

$$R_* = \left(\frac{3v_b}{4\pi\Gamma(T_*)}\right)^{1/4}, \quad V_* = \left(\frac{4\pi}{3}\right)^{1/4} \left(\frac{v_b}{\Gamma(T_*)}\right)^{3/4}$$

• Fermi-ball profiles right after formation

At the 3) step, the false vacuum remnants first split then shrink:





The critical size R_* of a remnant at the end of splitting and the beginning of shrinking

$$R_* = \left(\frac{3v_b}{4\pi\Gamma(T_*)}\right)^{1/4}, \quad V_* = \left(\frac{4\pi}{3}\right)^{1/4} \left(\frac{v_b}{\Gamma(T_*)}\right)^{3/4}$$

And at this point we have

$$n_{\rm FB}^* V_* = p(T_*) = 0.29$$

Therefore

$$n_{\rm FB}^* = \left(\frac{3}{4\pi}\right)^{1/4} \left(\frac{\Gamma(T_*)}{v_b}\right)^{3/4} p(T_*), \quad Q_{\rm FB}^* = F_{\chi}^{\rm trap.} \frac{c_{\chi} \eta_B s_*}{n_{\rm FB}^*}$$

• Fermi-ball profiles today

Linking the profiles at *T*^{*} to today:

$$n_{\rm FB} = \frac{n_{\rm FB}^*}{s_*} s_0, \quad Q_{\rm FB} = Q_{\rm FB}^*$$
s: entropy density of the universe

A single Fermi-ball
$$\int False vacuum \langle \phi \rangle = w_0$$

$$U_0$$

$$U_0$$

$$T = 0$$
True vacuum
$$\phi$$

The energy of a Fermi-ball:

Surface tension (negligible)

$$E = \frac{3\pi}{4} \left(\frac{3}{2\pi}\right)^{2/3} \frac{Q_{\text{FB}}^{4/3}}{R} + 4\pi\sigma_0 R^2 + \frac{4\pi}{3} U_0 R^3$$
Fermi-gas kinetic energy Volume energy

The radius is determined by dE/dR = 0.

Fermi-ball profiles today

Minimizing E yields the profile

$$M_{\rm FB} = Q_{\rm FB} \left(12\pi^2 U_0 \right)^{1/4}, \quad R_{\rm FB} = Q_{\rm FB}^{1/3} \left[\frac{3}{16} \left(\frac{3}{2\pi} \right)^{2/3} \frac{1}{U_0} \right]^{1/4}$$

Density of a single Fermi-ball

$$M_{\rm FB}/V_{\rm FB} = 9.15 \times 10^{28} \text{ kg/m}^3 \left(\frac{U_0^{1/4}}{100 \text{ GeV}}\right)^4$$

Very compact!





is more compact than



But not as compact as a *Q*-ball ^[Krylov et al, PRD2013]: $\rho_{QB} \approx 10^{36} \text{ kg/m}^3$, due to the Pauli exclusion principle.

Fermi-ball as DM candidate

Relic density of the Fermi-balls [c_{χ} is the χ -asymmetry factor]

$$\Omega_{\rm FB} h^2 = \frac{n_{\rm FB} M_{\rm FB}}{\rho_c} h^2 = 0.12 \times \left(\frac{c_{\chi} U_0^{1/4}}{1.146 \text{ GeV}}\right)$$

To achieve the **DM density**:

□ $c_{\chi} \approx 1, U_0^{1/4} \approx 1 \text{ GeV}$? □ $c_{\chi} \approx 0.01, U_0^{1/4} \approx 100 \text{ GeV}$?

The former case is stringently constrained; we consider the latter.

• Fermi-ball as DM candidate

Relic density of the Fermi-balls [c_{χ} is the χ -asymmetry factor]

$$\Omega_{\rm FB} h^2 = \frac{n_{\rm FB} M_{\rm FB}}{\rho_c} h^2 = 0.12 \times \left(\frac{c_{\chi} U_0^{1/4}}{1.146 \text{ GeV}}\right)$$

To achieve the **DM density**: $\Box c_{\chi} \approx 1, U_0^{1/4} \approx 1 \text{ GeV}$? $\Box c_{\chi} \approx 0.01, U_0^{1/4} \approx 100 \text{ GeV}$? The former case is stringently constrained: we consider the

The former case is stringently constrained; we consider the latter.

• Fermi-ball as DM candidate

Reminder: vacuum decay rate $T_*^4 e^{-S_3(T_*)/T_*}$

For a EW scale phase transition & a radiation-dominated universe

$$\frac{S_3(T_*)}{T_*} \sim 140$$

Hence we can normalize the profiles to

$$\begin{split} M_{\rm FB} &\approx 4.84 \times 10^{11} \text{ kg} \times \left(\frac{c_{\chi}}{0.0146}\right) \left(\frac{U_0^{1/4}}{100 \text{ GeV}}\right) \left(\frac{v_b}{0.6}\right)^{3/4} \exp\left\{\frac{3}{4} \left(\frac{S_3(T_*)}{T_*} - 140\right)\right\},\\ R_{\rm FB} &\approx 1.08 \times 10^{-6} \text{ m} \times \left(\frac{c_{\chi}}{0.0146}\right)^{1/3} \left(\frac{100 \text{ GeV}}{U_0^{1/4}}\right) \left(\frac{v_b}{0.6}\right)^{1/4} \exp\left\{\frac{1}{4} \left(\frac{S_3(T_*)}{T_*} - 140\right)\right\},\\ Q_{\rm FB} &\approx 8.26 \times 10^{35} \times \left(\frac{c_{\chi}}{0.0146}\right) \left(\frac{v_b}{0.6}\right)^{3/4} \exp\left\{\frac{3}{4} \left(\frac{S_3(T_*)}{T_*} - 140\right)\right\},\\ n_{\rm FB} &\approx 4.60 \times 10^{-39} \text{ m}^{-3} \times \left(\frac{0.6}{v_b}\right)^{3/4} \exp\left\{-\frac{3}{4} \left(\frac{S_3(T_*)}{T_*} - 140\right)\right\}. \end{split}$$

But the pre-factors are only very rough estimations, because of the <u>exponents</u> behind them!

• Stability of the Fermi-ball

Decay: a Fermi-ball should not emit a χ fermion



Effective mass per
$$\chi$$

 $M_{\rm FB} = Q_{\rm FB} \left(12\pi^2 U_0 \right)^{1/4}$
 $dM_{\rm FB}$

$$\frac{dM_{\rm FB}}{dQ_{\rm FB}} < M_{\chi} \equiv g_{\chi} w_0$$

Need to be satisfied in a concrete model.

• Stability of the Fermi-ball

Decay: a Fermi-ball should not emit a χ fermion



 $M_{\rm FB} = Q_{\rm FB} \left(12\pi^2 U_0 \right)^{1/4}$ $\frac{dM_{\rm FB}}{dQ_{\rm FB}} < M_{\chi} \equiv g_{\chi} w_0$

Need to be satisfied in a concrete model.

Fission: a Fermi-ball should not split to two smaller ones



Satisfied when the surface tension ($\propto Q_{FB}^{2/3}$) is included.

• For a concrete (toy) model...

The scalar potential $U(\phi,T) = \frac{1}{2}(\mu^2 + cT^2)\phi^2 + \frac{\mu_3}{3}\phi^3 + \frac{\lambda}{4}\phi^4$

The μ_3 term: tree level barrier. Benchmark parameters:

$$w_0 = \langle \phi \rangle |_{T=0} = 400 \text{ GeV}, \quad M_\phi = 100 \text{ GeV}, \quad c = 0.4,$$

 $T > T_c$ $T = T_c$

 $T < T_c$

 $\mathcal{I}_{T}(\phi)$

 $\mu_3 < 0$

FOPT (vacuum decay)

φ

 ΔU_T

WT

FOPT profile & Fermi-ball profile



• For a concrete (toy) model...

Fermi-ball (trapped χ in false vacuum)



$$n_{\rm FB} = 1.1 \times 10^{-37} \text{ m}^{-3} \sim 9.3 \times 10^{-34} \text{ m}^{-3},$$

$$Q_{\rm FB} = 3.9 \times 10^{34} \sim 4.0 \times 10^{30},$$

$$M_{\rm FB} = 2.4 \times 10^{10} \text{ kg} \sim 2.6 \times 10^{6} \text{ kg},$$

$$R_{\rm FB} = 3.7 \times 10^{-7} \text{ m} \sim 1.8 \times 10^{-8} \text{ m}$$

 $g_{\chi}w_0$: mass of free χ in the true vacuum; O(TeV).

In the <u>true vacuum</u>, free χ can be produced thermally ($\mathcal{L} \supset -g_{\chi} \bar{\chi} \chi \phi$) and experiences freeze-out!

It's necessary to check the Fermi-ball fraction of the Universe.



Direct detection $[v_{DM} = 10^{-3}, L = 10 \text{ m}]$?

 $n_{\rm FB} \sim 10^{-37} \text{ m}^{-3}$: $n_{\rm FB} v_{\rm DM} L^2 \sim 10^{-22} / \text{year}$

Hopeless!!

$$n_{\rm FB} = 1.1 \times 10^{-37} \text{ m}^{-3} \sim 9.3 \times 10^{-34} \text{ m}^{-3},$$

$$Q_{\rm FB} = 3.9 \times 10^{34} \sim 4.0 \times 10^{30},$$

$$M_{\rm FB} = 2.4 \times 10^{10} \text{ kg} \sim 2.6 \times 10^{6} \text{ kg},$$

$$R_{\rm FB} = 3.7 \times 10^{-7} \text{ m} \sim 1.8 \times 10^{-8} \text{ m}$$



"Yes, a bole in space three bundred million light-years across does make me pause and feel tiny and insignificant, but a glance around at my peers usually restores my equanimity."

Direct detection $[v_{DM} = 10^{-3}, L = 10 \text{ m}]$?

 $n_{\rm FB} \sim 10^{-37} \text{ m}^{-3}$: $n_{\rm FB} v_{\rm DM} L^2 \sim 10^{-22} / \text{year}$

Hopeless!!

Gravitational effects?

A single Fermi-ball is too light $(10^{-20} M_{\odot})$ and not compact enough to provide signals such as lensing.

$$n_{\rm FB} = 1.1 \times 10^{-37} \text{ m}^{-3} \sim 9.3 \times 10^{-34} \text{ m}^{-3},$$

$$Q_{\rm FB} = 3.9 \times 10^{34} \sim 4.0 \times 10^{30},$$

$$M_{\rm FB} = 2.4 \times 10^{10} \text{ kg} \sim 2.6 \times 10^{6} \text{ kg},$$

$$R_{\rm FB} = 3.7 \times 10^{-7} \text{ m} \sim 1.8 \times 10^{-8} \text{ m}$$



"Yes, a bole in space three hundred million light-years across does make me pause and feel tiny and insignificant, but a glance around at my peers usually restores my equanimity."

Gravitational waves?

Fermi-balls are produced in association with a FOPT.

Large w_*/T_* implies significant supercooling and hence strong stochastic GW signals.

The FOPT GWs:

- 1. Collision of the bubbles;
- 2. Sound waves in plasma;
- 3. Turbulance in plasma.

Hopefully to be detected in the future space-based detectors.





Collider signals?

For a concrete model, there might be additional signals, e.g.

- 1. The portal coupling or even mixing between the Higgs and the ϕ field;
- 2. The production of χ at the collider;
- 3. Mono-X signal; displayed vertices; disappearing tracks, etc.

Not so different from the searches for the O(TeV) WIMPs.





Conclusion

We propose a novel DM mechanism:

- □ Fermions are trapped into the false vacuum during a FOPT to form non-topological solitons, i.e. the Fermi-ball DM;
- The formation condition is generally satisfied in many new physics models.

Fermi-ball itself doesn't yield interesting experimental signals; but the FOPT GWs can be an indirect probe.

For a concrete model we might have collider signals.

