

# On the rate and gravitational wave emission of short and long GRBs

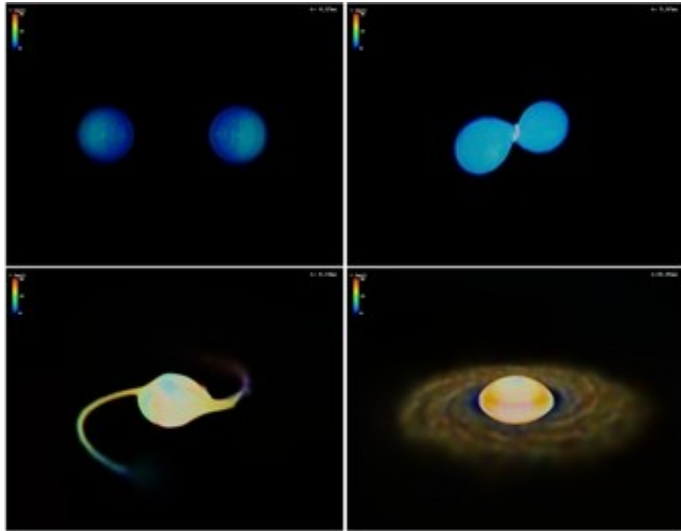
Jorge Armando Rueda Hernández - ICRA Net  
(On behalf of a larger collaboration)

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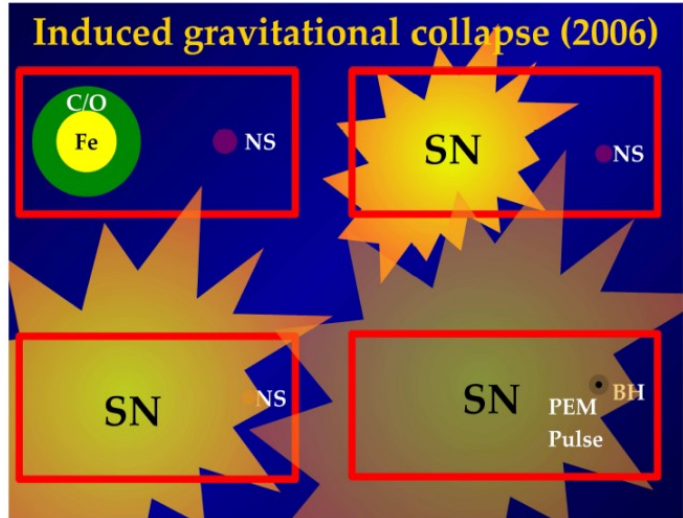
International Conference on Gravitation: Joint Conference of ICGAC-XIII and IK15  
July 3-7, Seoul 2017

# Gamma-ray bursts and neutron-star physics

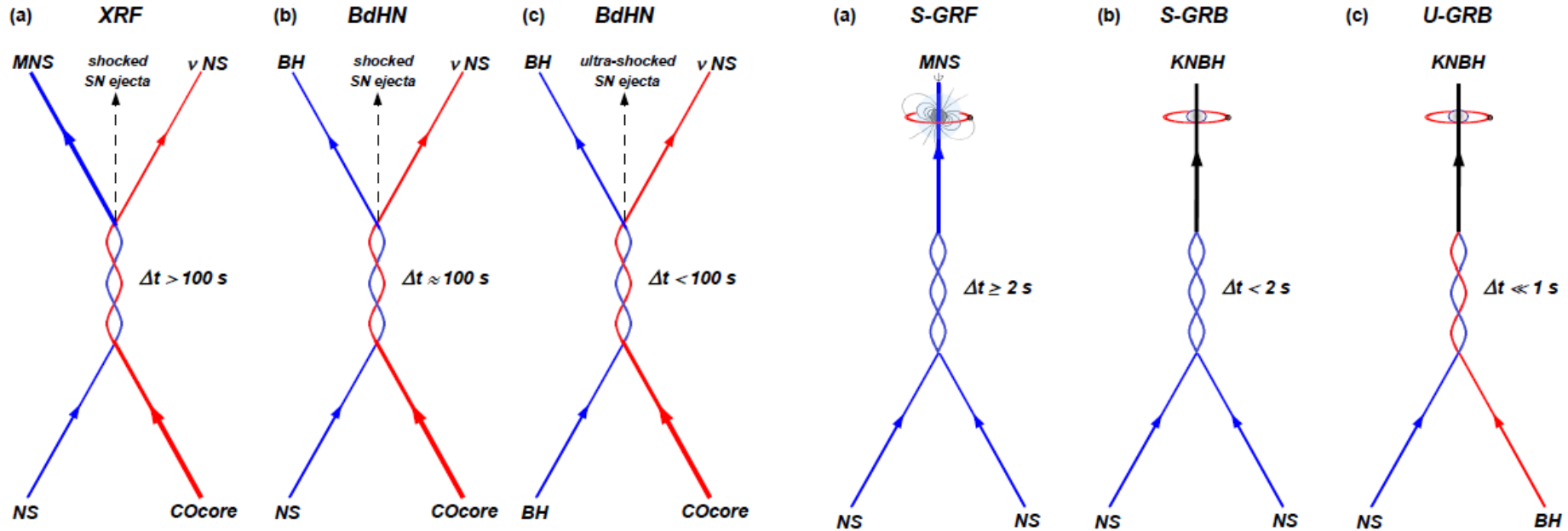
## Short GRBs: NS-NS and NS-BH Mergers



## Long GRB-SN: Induced Gravitational Collapse



# Long and short GRB subclasses



# Short and long GRB sub-classes

**Table 1.** Summary of the astrophysical aspects of the different GRB sub-classes and of their observational properties. In the first four columns we indicate the GRB sub-classes and their corresponding *in-states* and the *out-states*. In columns 5–8 we list the ranges of  $E_{p,i}$  and  $E_{\text{iso}}$  (rest-frame 1–10<sup>4</sup> keV),  $E_{\text{iso},X}$  (rest-frame 0.3–10 keV), and  $E_{\text{iso,GeV}}$  (rest-frame 0.1–100 GeV). Columns 9 and 10 list, for each GRB sub-class, the maximum observed redshift and the local observed rate  $\rho_{\text{GRB}}$  obtained in [Ruffini et al. \(2016b\)](#).

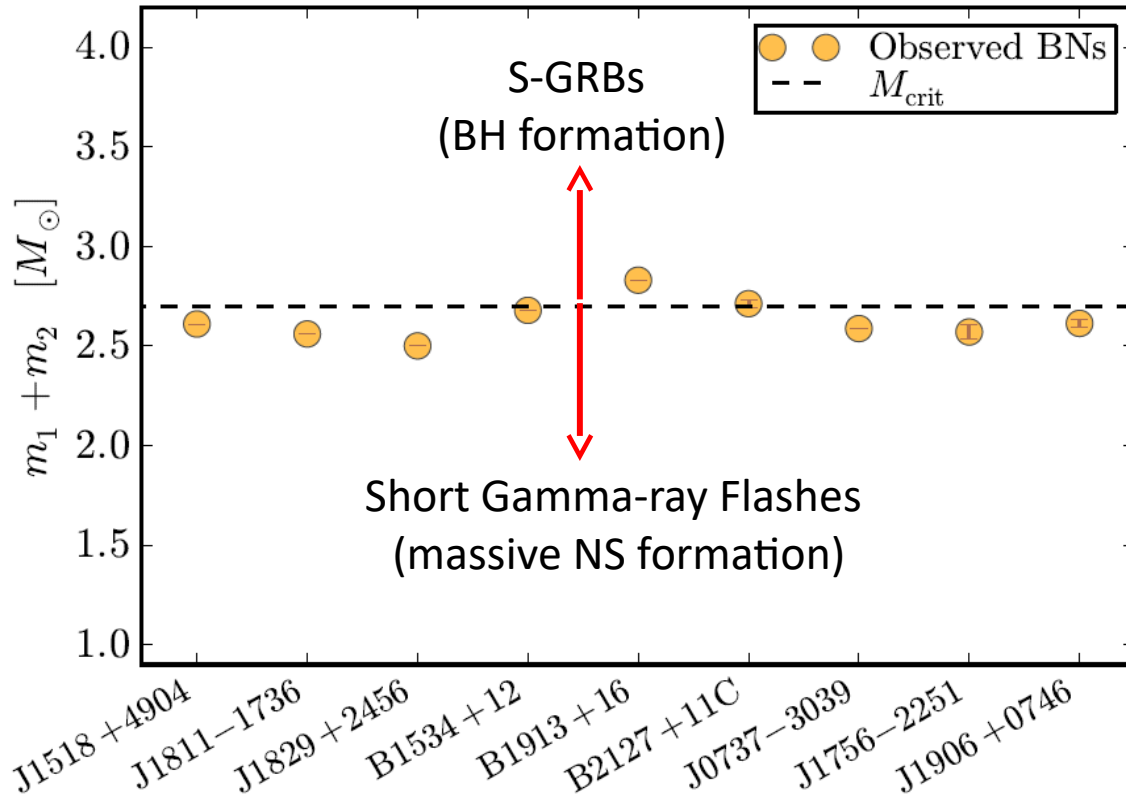
	Sub-class	<i>In-state</i>	<i>Out-state</i>	$E_{p,i}$ (MeV)	$E_{\text{iso}}$ (erg)	$E_{\text{iso},X}$ (erg)	$E_{\text{iso,GeV}}$ (erg)	$z_{\text{max}}$	$\rho_{\text{GRB}}$ (Gpc <sup>-3</sup> yr <sup>-1</sup> )
I	XRFs	CO <sub>core</sub> -NS	$\nu$ NS-NS	$\lesssim 0.2$	$\sim 10^{48}\text{--}10^{52}$	$\sim 10^{48}\text{--}10^{51}$	–	1.096	$100^{+45}_{-34}$
II	BdHNe	CO <sub>core</sub> -NS	$\nu$ NS-BH	$\sim 0.2\text{--}2$	$\sim 10^{52}\text{--}10^{54}$	$\sim 10^{51}\text{--}10^{52}$	$\lesssim 10^{53}$	9.3	$0.77^{+0.09}_{-0.08}$
III	BH-SN	CO <sub>core</sub> -BH	$\nu$ NS-BH	$\gtrsim 2$	$> 10^{54}$	$\sim 10^{51}\text{--}10^{52}$	$\gtrsim 10^{53}$	9.3	$\lesssim 0.77^{+0.09}_{-0.08}$
IV	S-GRFs	NS-NS	MNS	$\lesssim 2$	$\sim 10^{49}\text{--}10^{52}$	$\sim 10^{49}\text{--}10^{51}$	–	2.609	$3.6^{+1.4}_{-1.0}$
V	S-GRBs	NS-NS	BH	$\gtrsim 2$	$\sim 10^{52}\text{--}10^{53}$	$\lesssim 10^{51}$	$\sim 10^{52}\text{--}10^{53}$	5.52	$(1.9^{+1.8}_{-1.1}) \times 10^{-3}$
VI	U-GRBs	$\nu$ NS-BH	BH	$\gtrsim 2$	$> 10^{52}$	–	–	–	$\gtrsim 0.77^{+0.09}_{-0.08}$
VII	GRFs	NS-WD	MNS	$\sim 0.2\text{--}2$	$\sim 10^{51}\text{--}10^{52}$	$\sim 10^{49}\text{--}10^{50}$	–	2.31	$1.02^{+0.71}_{-0.46}$

# Short GRBs

**NS+NS  $\rightarrow$  MNS**

**NS+NS  $\rightarrow$  BH**

# Two sub-classes of short GRBs



NS mass distribution in BNS peaks at  
 $1.32 M_{\text{sun}}$

(Kiziltan et al. 2013)

So:

$M_{\text{BNS}} \sim 2.64 M_{\text{sun}}$

(neglecting NS binding energy  
and angular momentum)

# Neutron Star Binding Energy

(Cipolletta et al., PRD 2015; arXiv: 1506.05926; Cipolletta et al., PRD in press; arXiv:1612.02207)

Static Configurations

$$\frac{M_b}{M_\odot} \approx \frac{M}{M_\odot} + \frac{13}{200} \left( \frac{M}{M_\odot} \right)^2$$

$c J / (G M_{\text{sun}}^2)$

Rotating Configurations

$$\frac{M_b}{M_\odot} = \frac{M}{M_\odot} + \frac{13}{200} \left( \frac{M}{M_\odot} \right)^2 \left( 1 - \frac{1}{130} j^{1.7} \right)$$

# Which are the mass and angular momentum of the merged core: NS+NS $\rightarrow$ MNS?

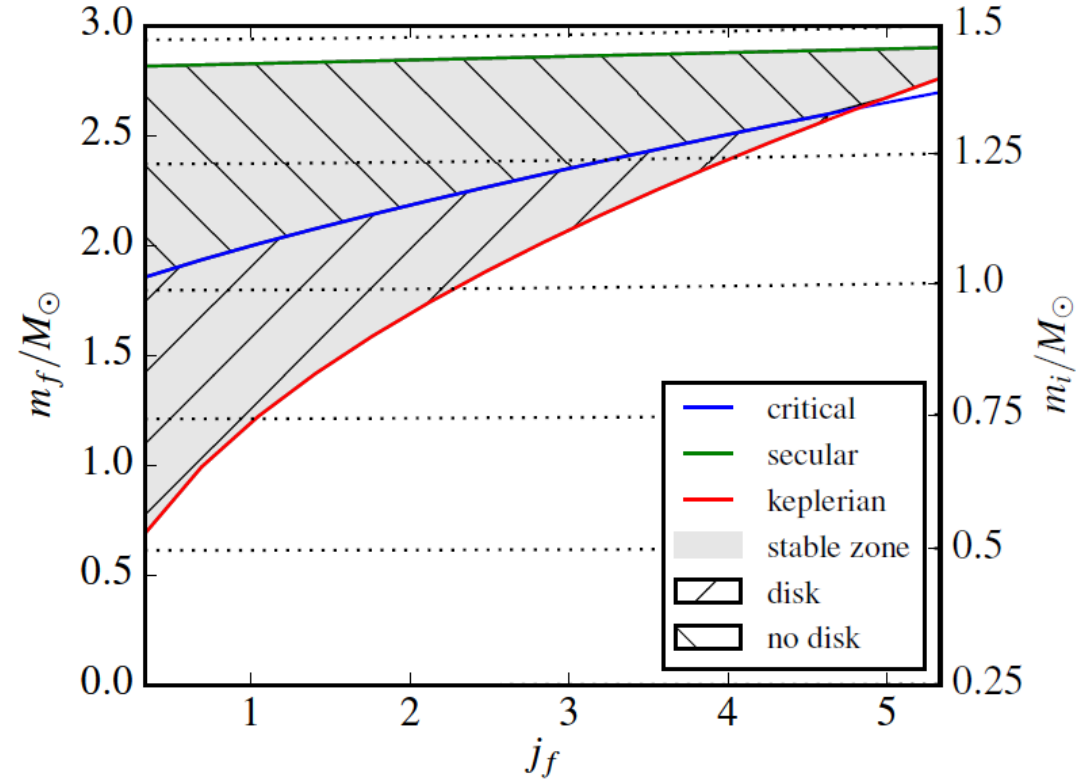
Depends on:

- 1) Mass-ratio of the binary ( $M_1/M_2 \sim 1$  for the galactic BNS)
- 2) Degree at which baryon mass is conserved
- 3) Degree at which angular momentum is conserved

$$(M_1, M_2) \rightarrow (M_{b1}, M_{b2})$$

$$M_{bf} = \alpha (M_{b1} + M_{b2}); \quad \alpha \sim 1$$

$$J_{mc} = \eta J_i \sim \eta J_{bin} \text{ (merger instant)}$$



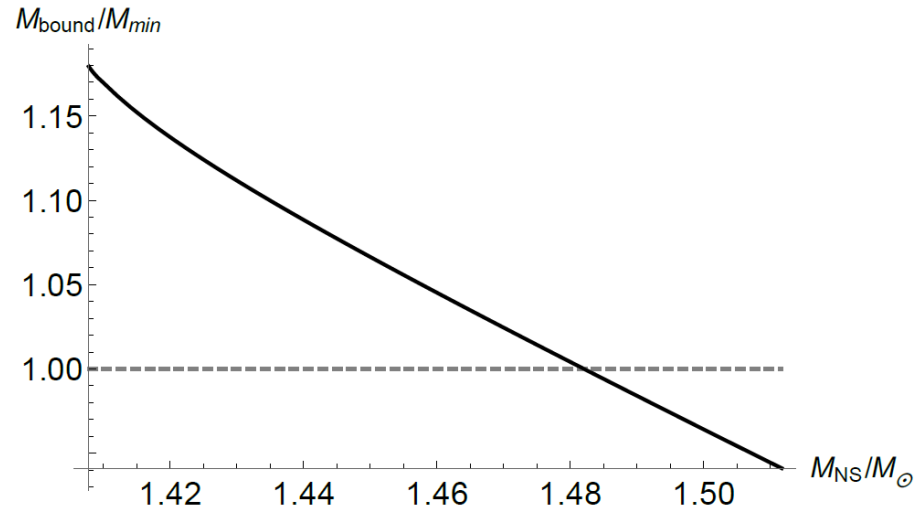
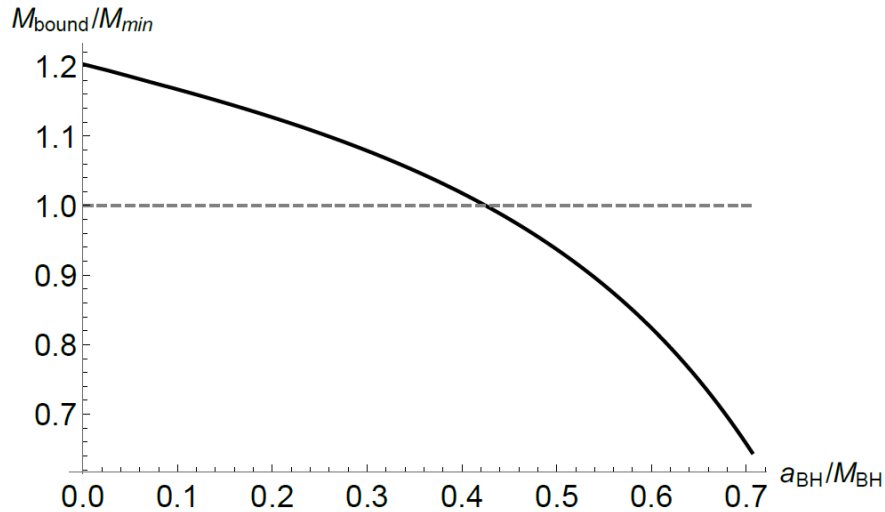
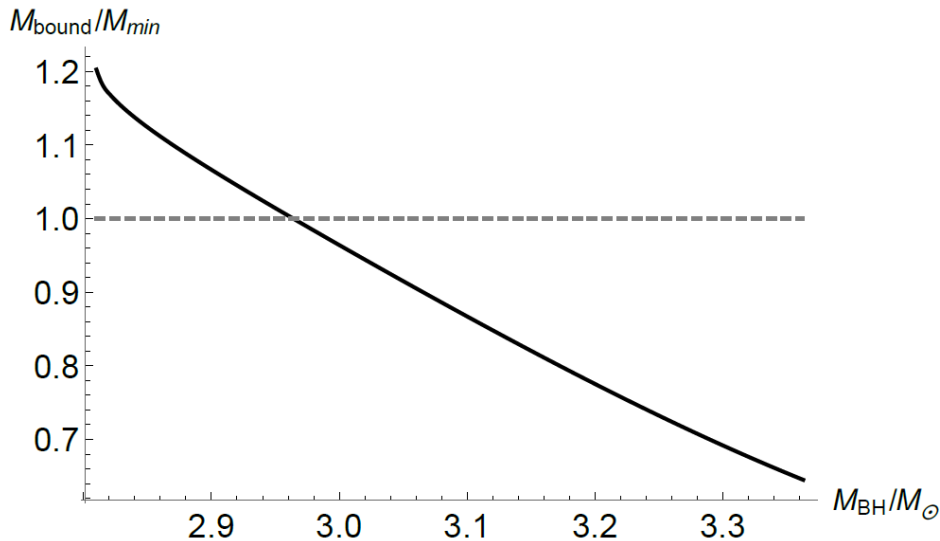


# NS+NS → BH ?

The explanation of the observed GeV emission in S-GRBs by accretion onto the formed BH may constraint the BH properties and the merging NS masses !

Aimuratov, Ruffini, et al.; ApJ in press; arXiv:1704.08179  
Ruffini, Muccino, et al.; ApJ 2016; arXiv:1607.02400  
Ruffini, Muccino, et al.; ApJ 2016; arXiv:1412.1018

See also M. Muccino's talk; Friday 06/07/2017

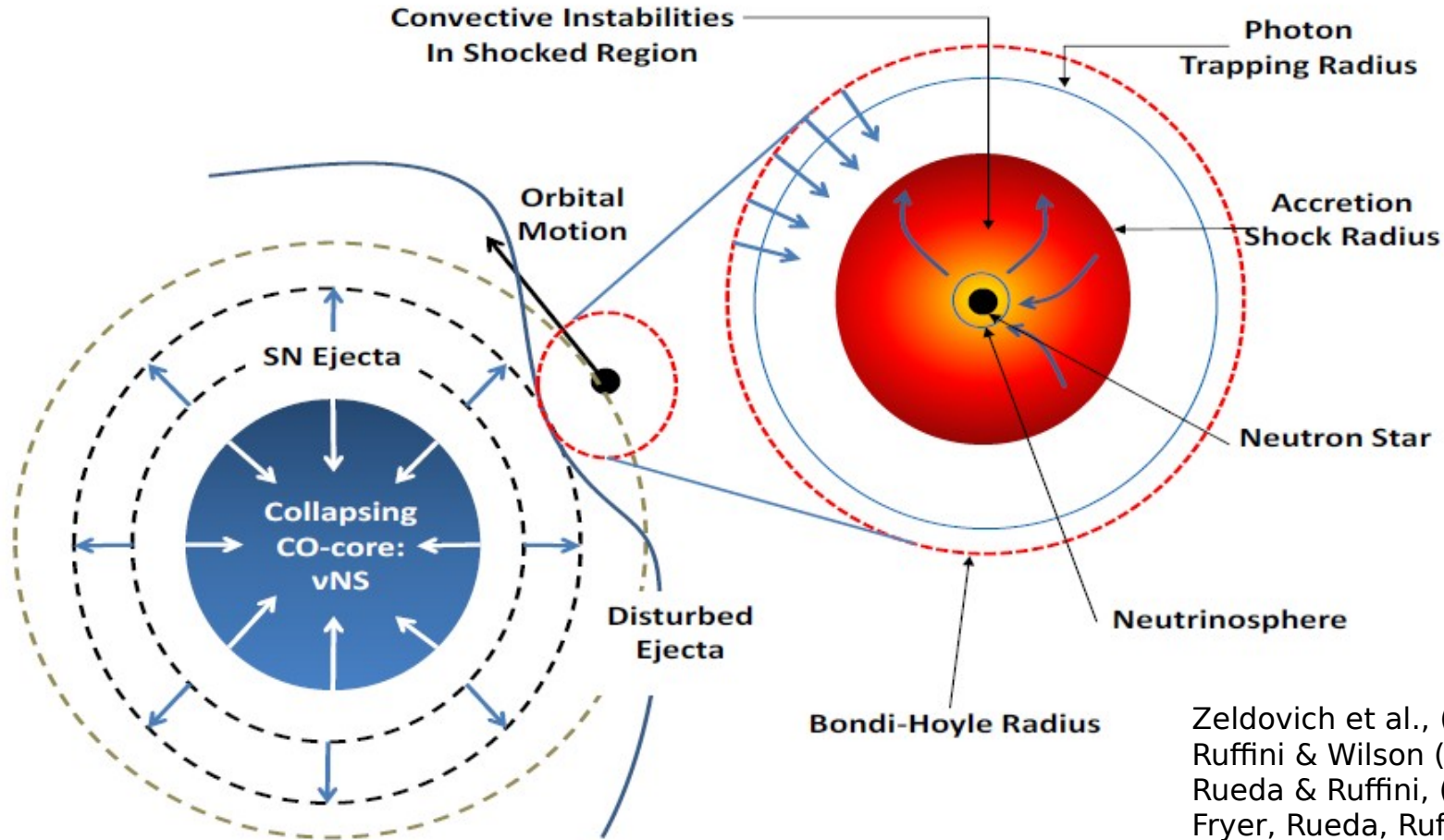


# Long GRBs

**CO+NS  $\rightarrow$  NS+MNS**

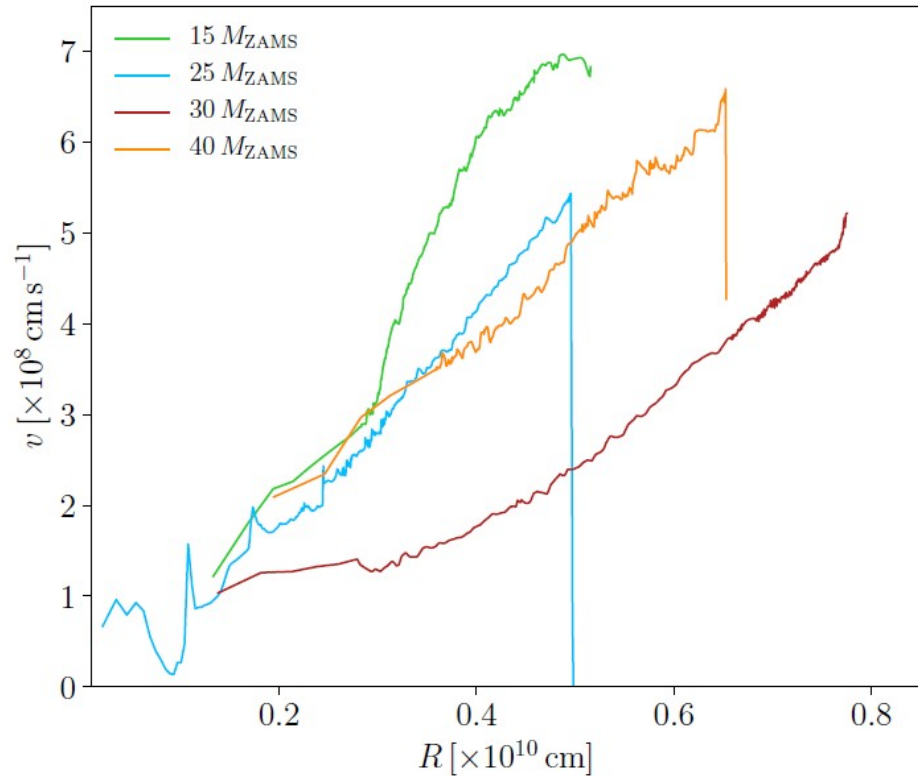
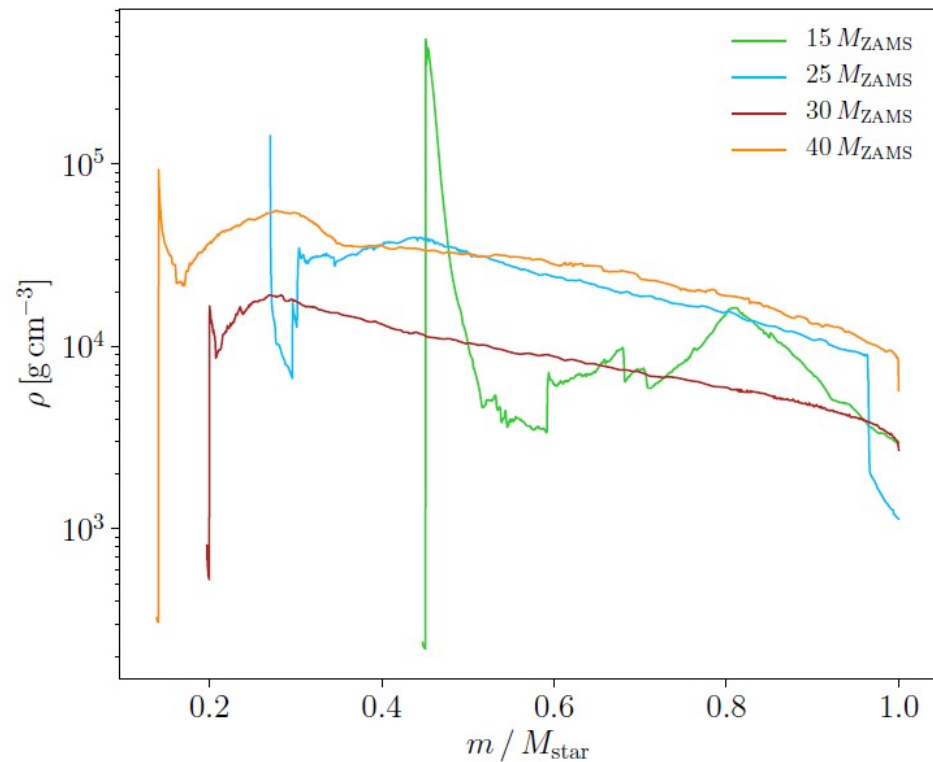
**CO+NS  $\rightarrow$  NS+BH**

# Binary-Driven Hypercritical Accretion



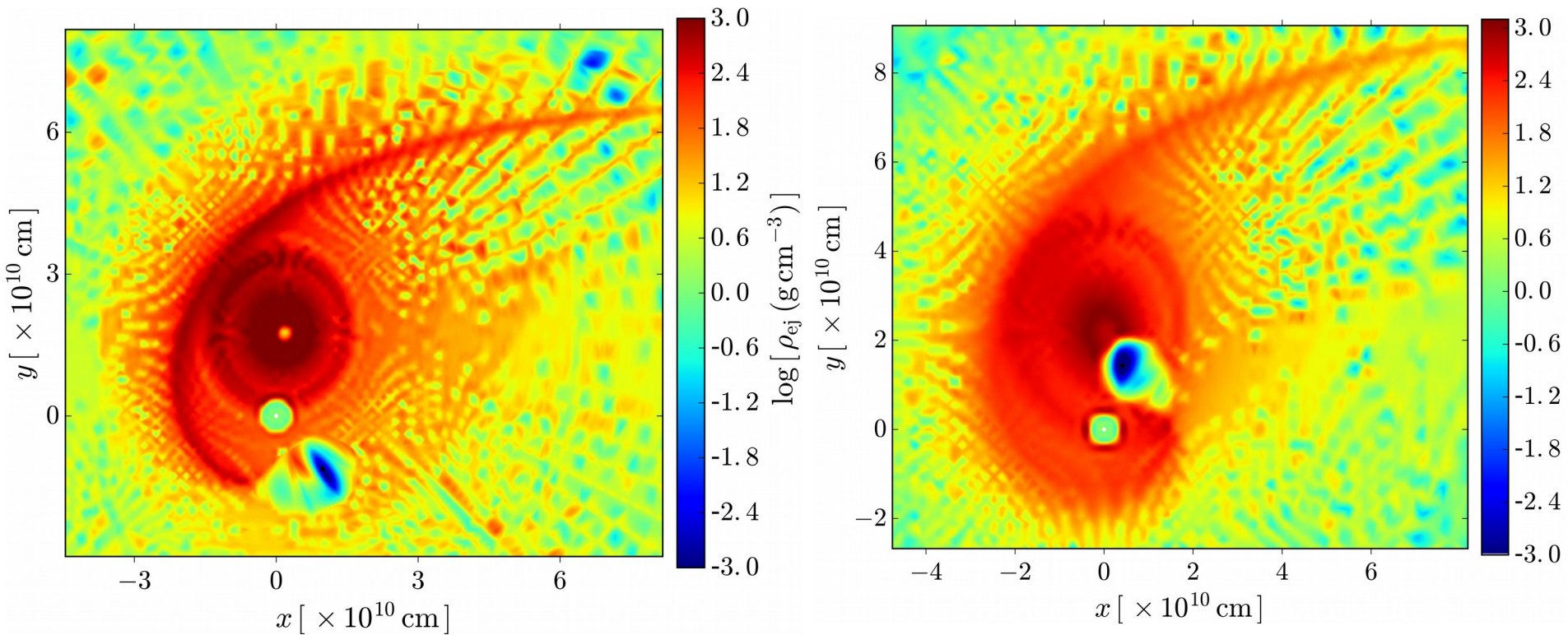
Zeldovich et al., (1972)  
Ruffini & Wilson (1973)  
Rueda & Ruffini, (2012)  
Fryer, Rueda, Ruffini, ApJL (2014)

# Supernova ejecta at $t=0$

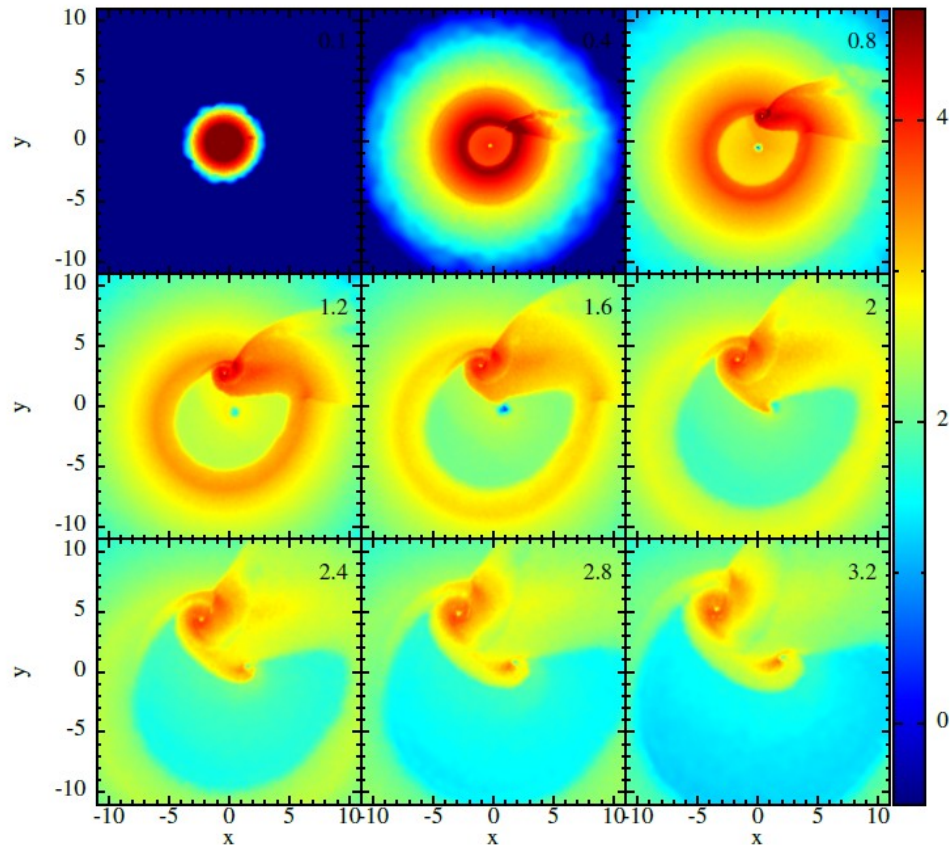
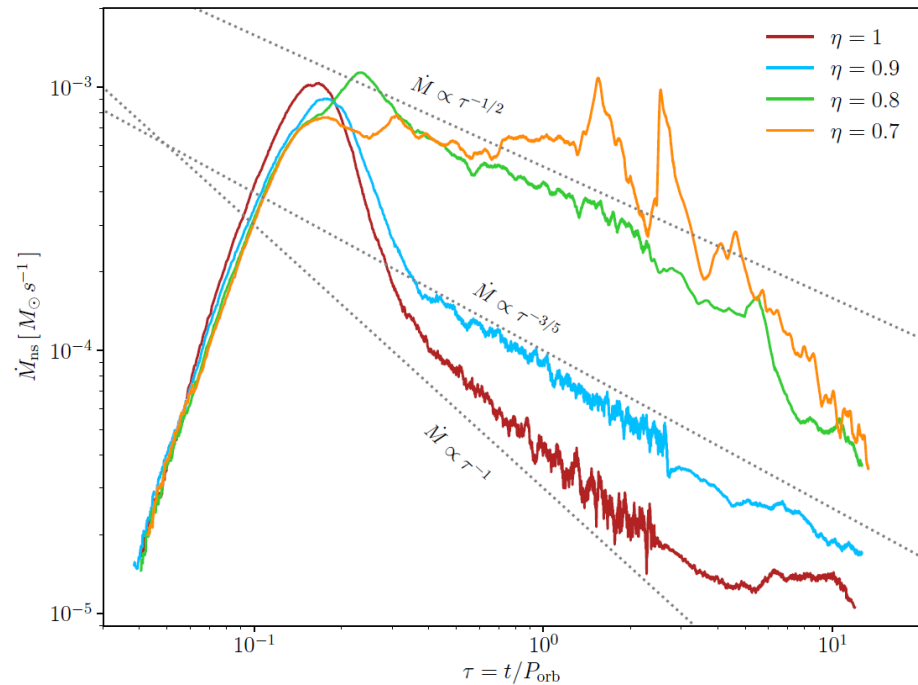


Becerra, et al., in preparation  
L. Becerra's talk on Monday 03/07/2017

# Visualizing the IGC process

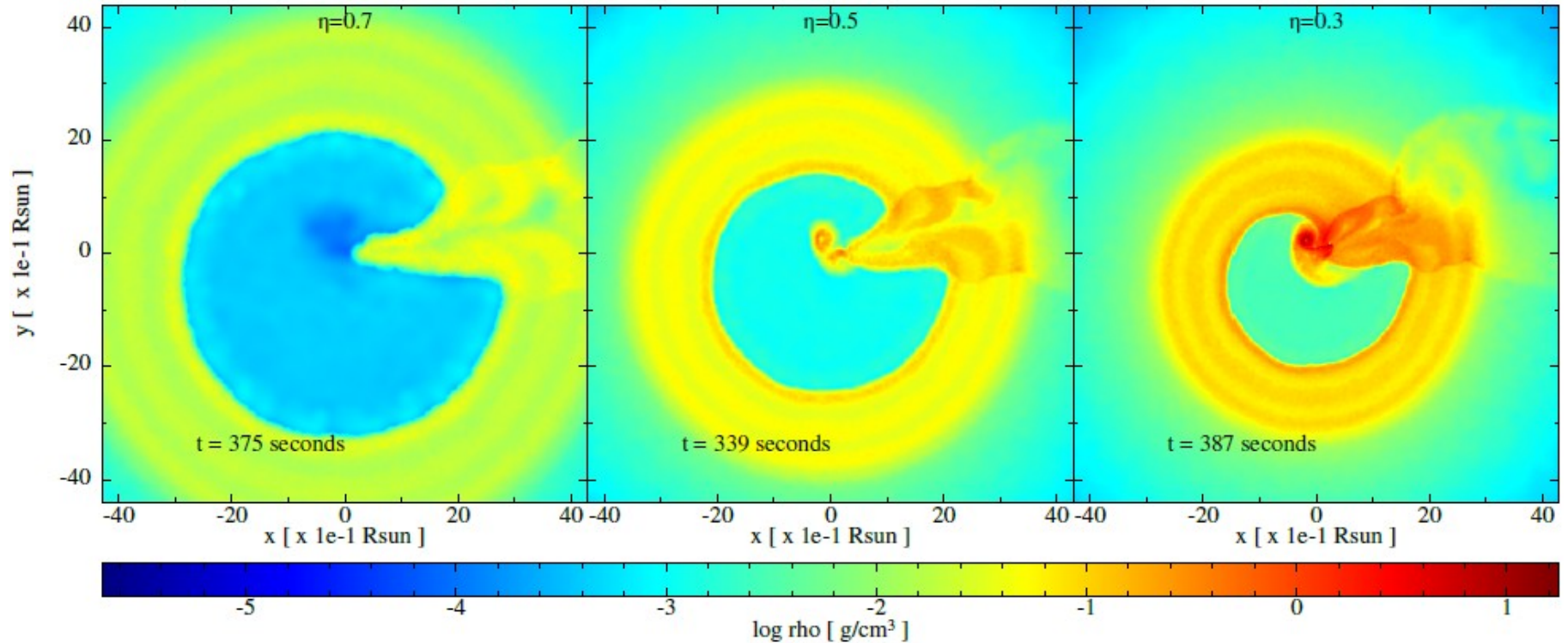


# Latest ICRAANet-LANL simulations



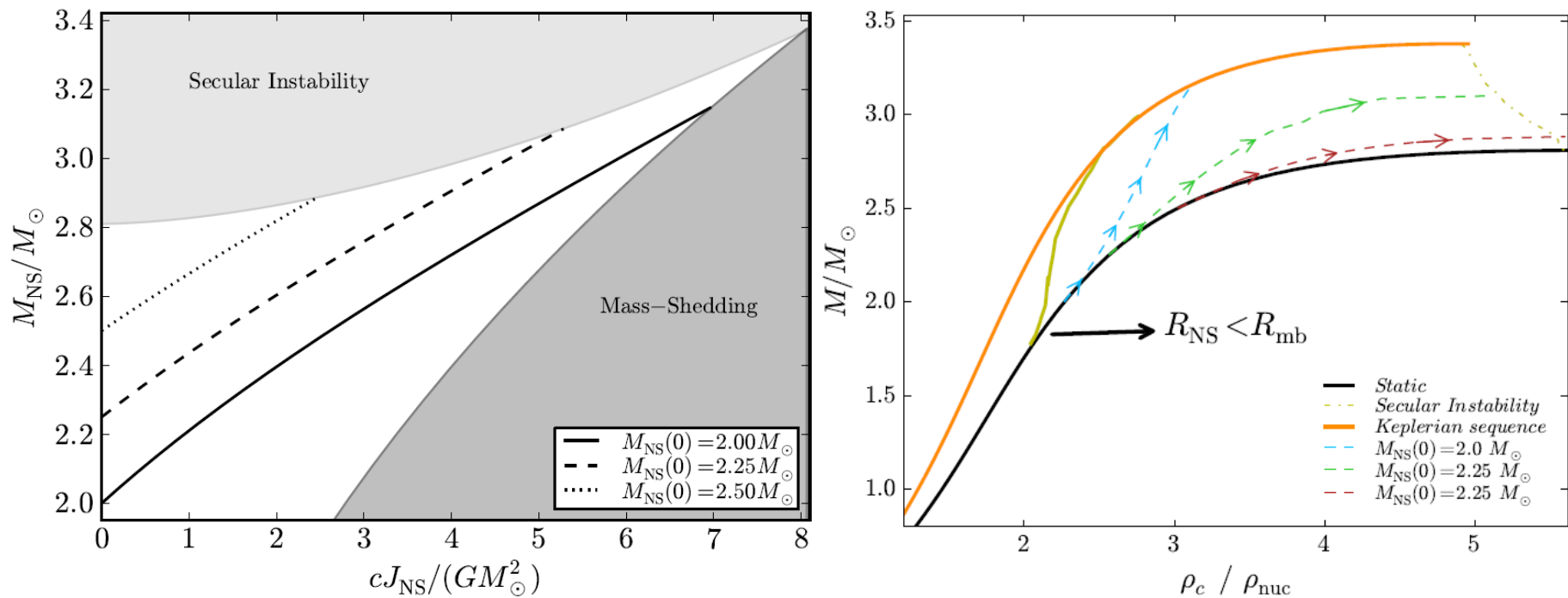
Becerra, et al., in preparation  
L. Becerra's talk on Monday 03/07/2017

# Latest ICRANet-LANL simulations



Becerra, et al., in preparation  
L. Becerra's talk on Monday 03/07/2017

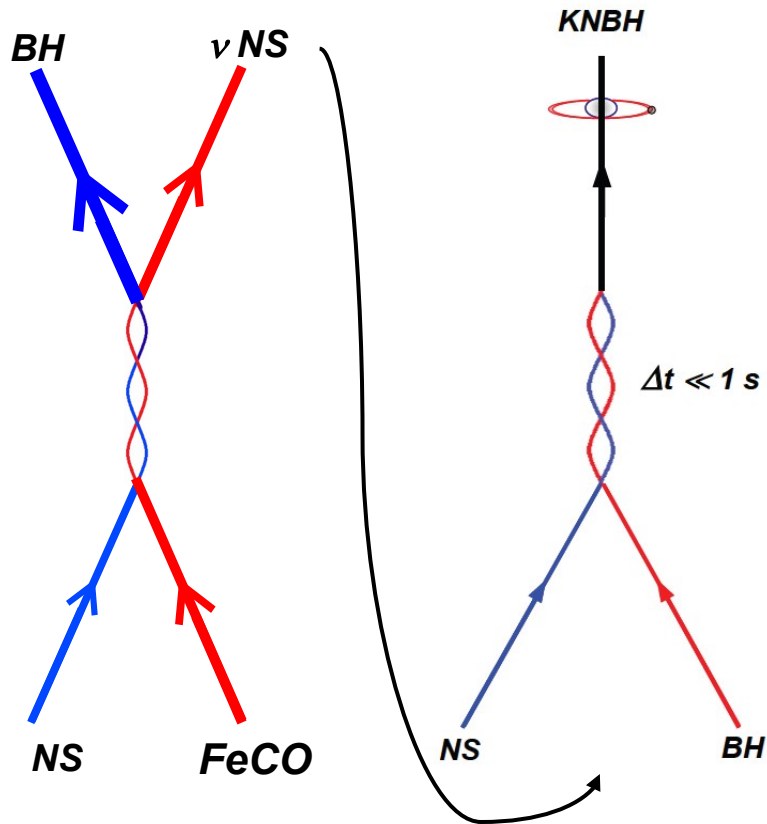
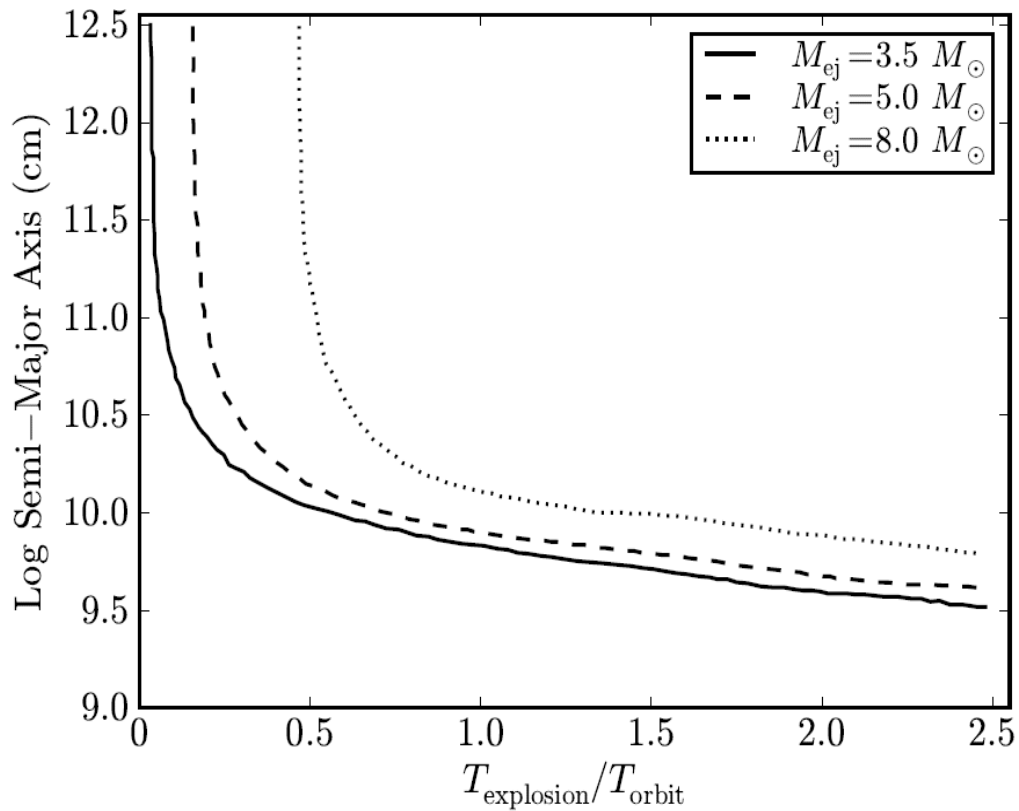
# NS evolution up to the instability point





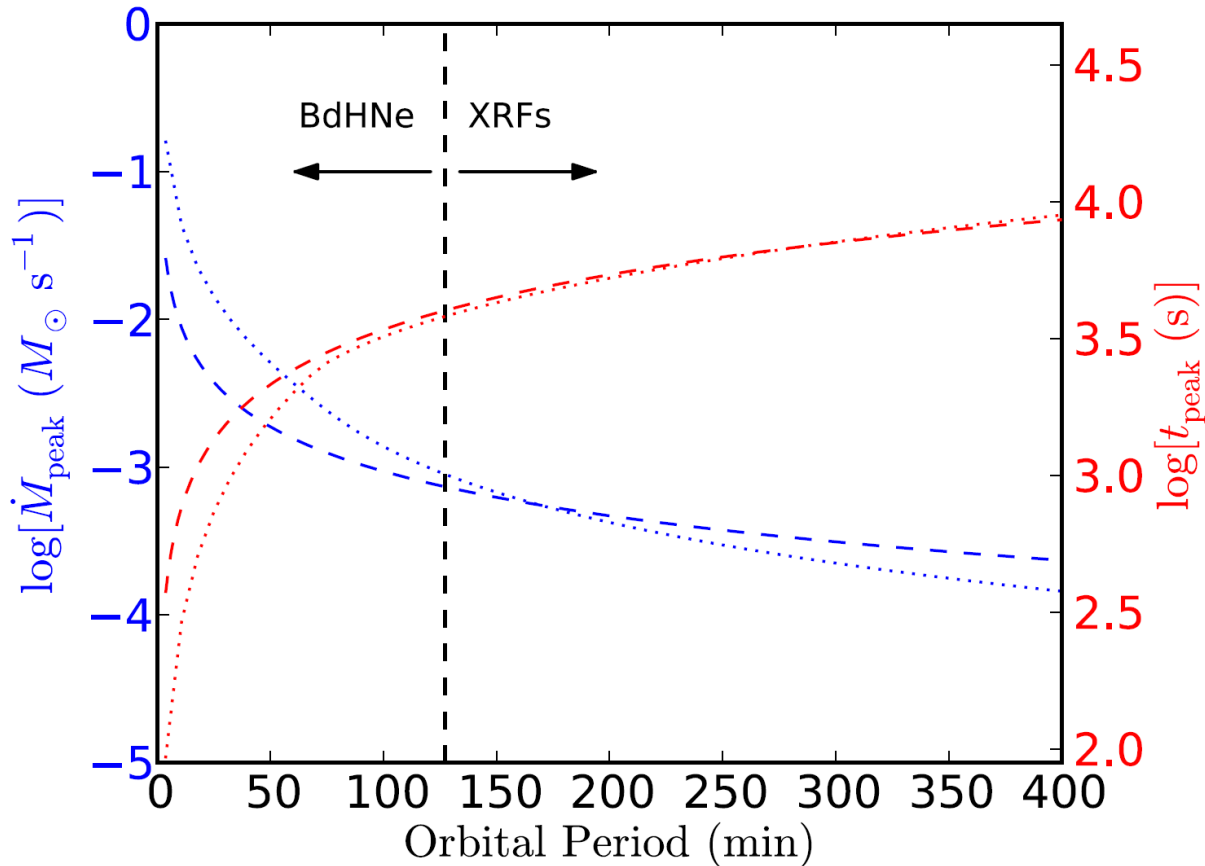
# NS-BH binaries produced by BdHNe

(Fryer, Oliveira, Rueda, Ruffini, Phys. Rev. Lett 2015; arXiv:1505.02809)

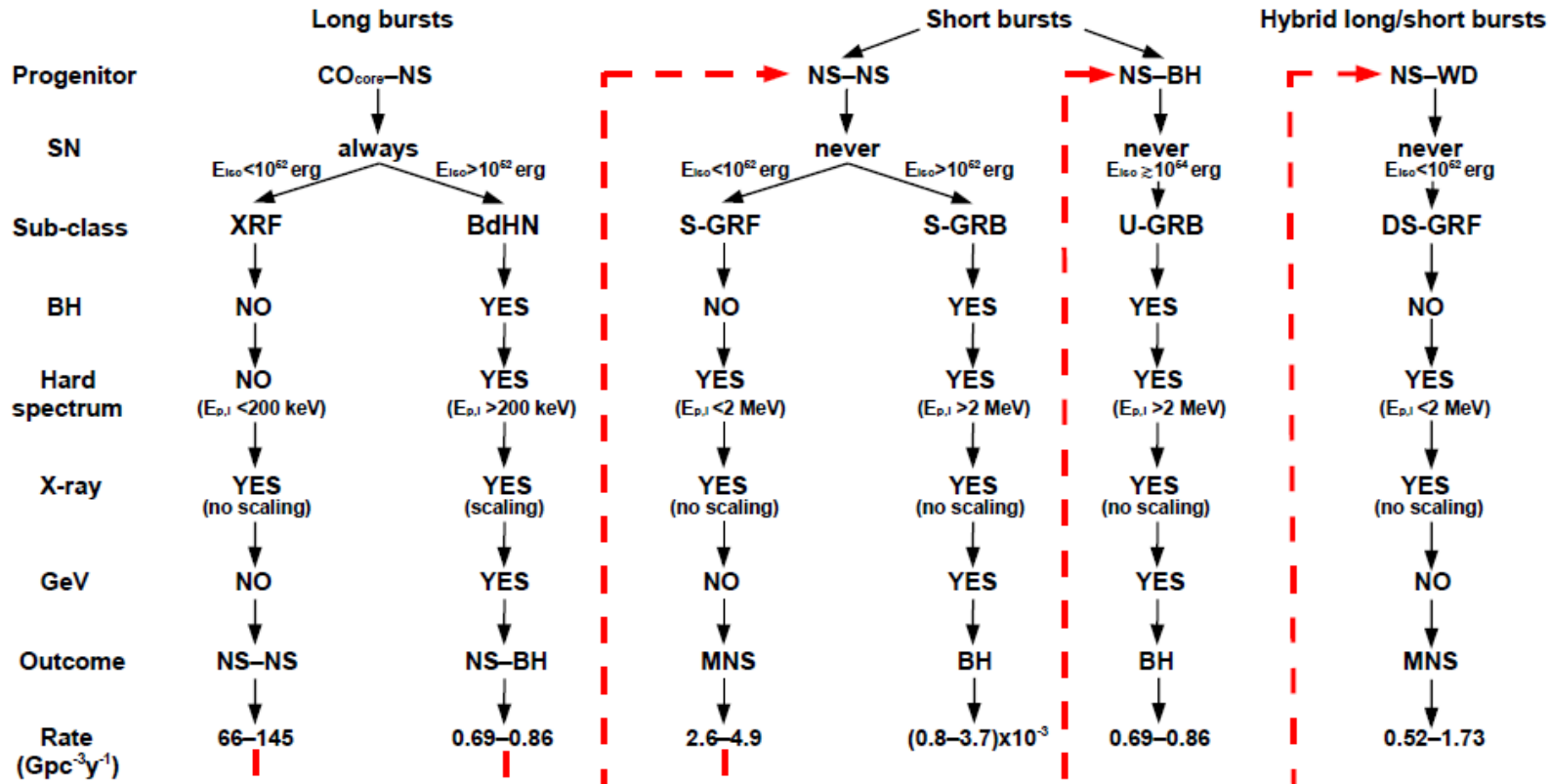


# X-ray Flashes - BdHNe Separatrix

(Becerra, Bianco, Fryer, Rueda, Ruffini, ApJ 2016; arXiv:1606.02523)



# Short and long GRB subclasses



Ruffini et al., ApJ (2015,2016)

# Gravitational-wave detectability of GRBs

$$\rho^2 = 4 \int_0^\infty \frac{|\tilde{h}(f)|^2}{S_n(f)} df$$

$$\langle \rho^2 \rangle = 4 \int_0^\infty \frac{\langle |\tilde{h}(f)|^2 \rangle}{S_n(f)} df = 4 \int_0^\infty \frac{h_c^2(f)}{f^2 S_n(f)} df.$$

$$h_c = \frac{(1+z)}{\pi d_l} \sqrt{\frac{\langle F_+^2 \rangle}{2} \frac{G}{c^3} \frac{dE}{df_s} [(1+z)f]}.$$

We can estimate the signal-to-noise ratio with the gravitational-wave spectrum

# Strong-field GW emission in Schwarzschild and Kerr geometries: some general considerations

J. F. Rodriguez' talk  
Monday 4/07

$$H = -P_t = -N^i P_i + N \sqrt{m^2 + \gamma^{ij} P_i P_j},$$

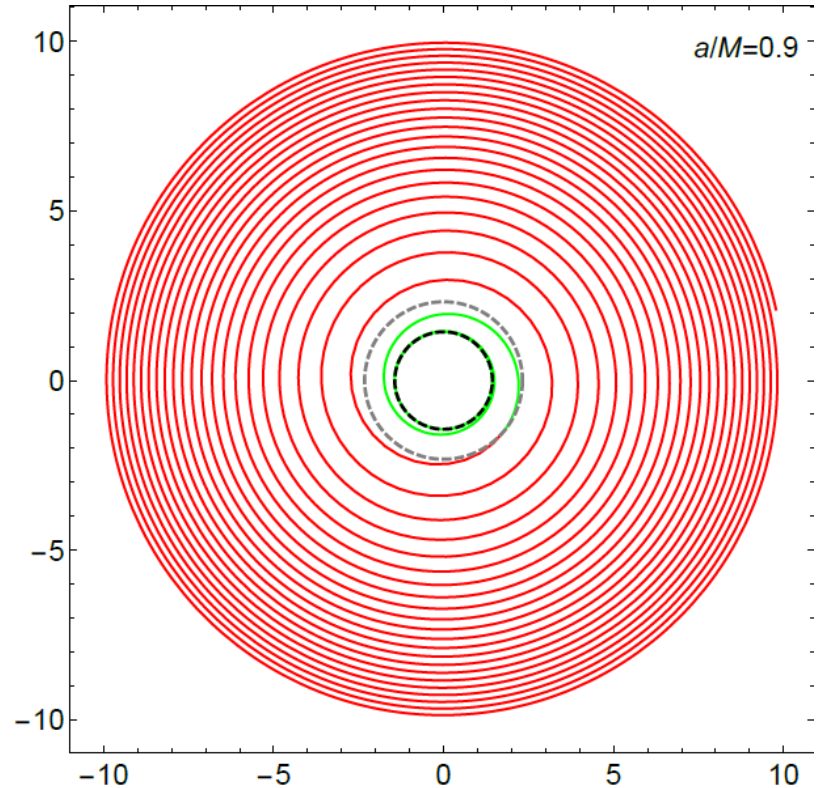
$$\frac{dr}{dt} = \frac{\partial H}{\partial P_r},$$

$$\frac{d\phi}{dt} = \frac{\partial H}{\partial P_\phi},$$

$$\frac{dP_r}{dt} = -\frac{\partial H}{\partial r},$$

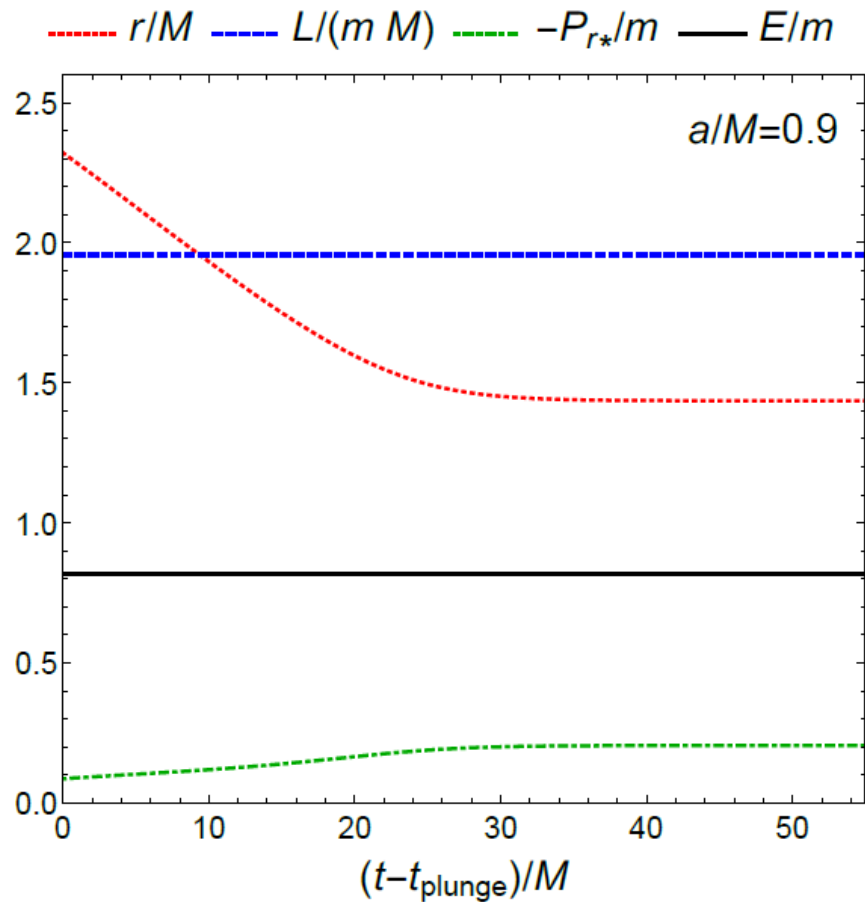
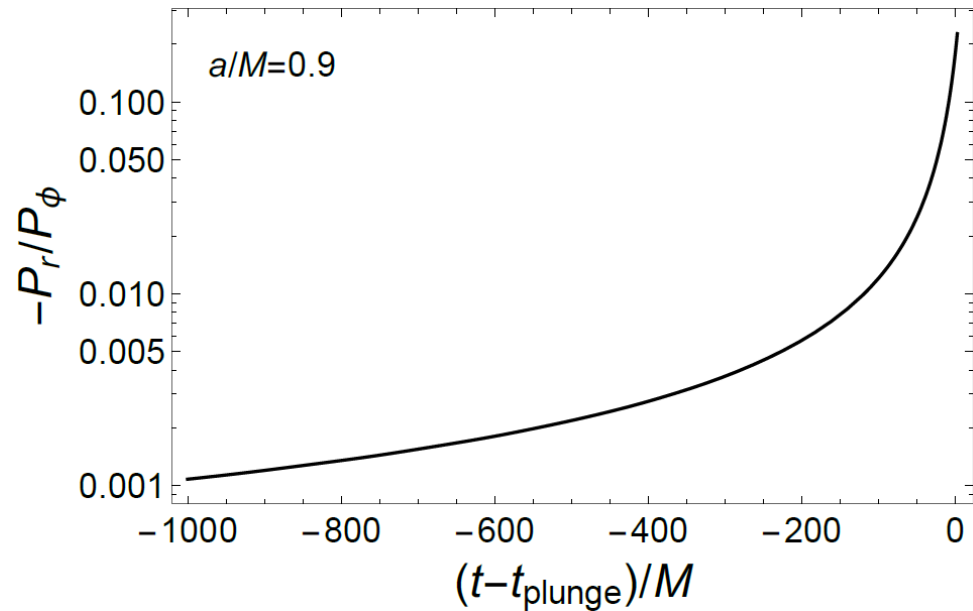
$$\frac{dP_\phi}{dt} = -\frac{1}{\omega} \frac{dE}{dt}.$$

Computed via  
Sasaki-  
Nakamura  
Method

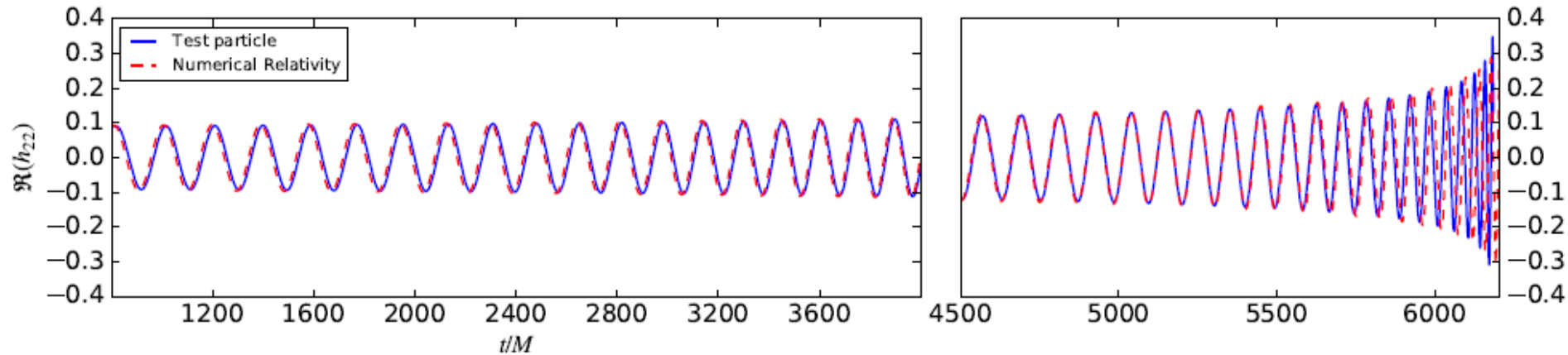


# Strong-field GW emission in Schwarzschild and Kerr geometries: some general considerations

J. F. Rodriguez' talk  
Monday 4/07



# Test-particle helicoidal-drifting-sequence in the Kerr geometry vs. numerical-relativity waveform



Rodriguez, Rueda, Ruffini, arXiv: 1706.07704  
(last-week post)

J. F. Rodriguez' talk  
Monday 4/07

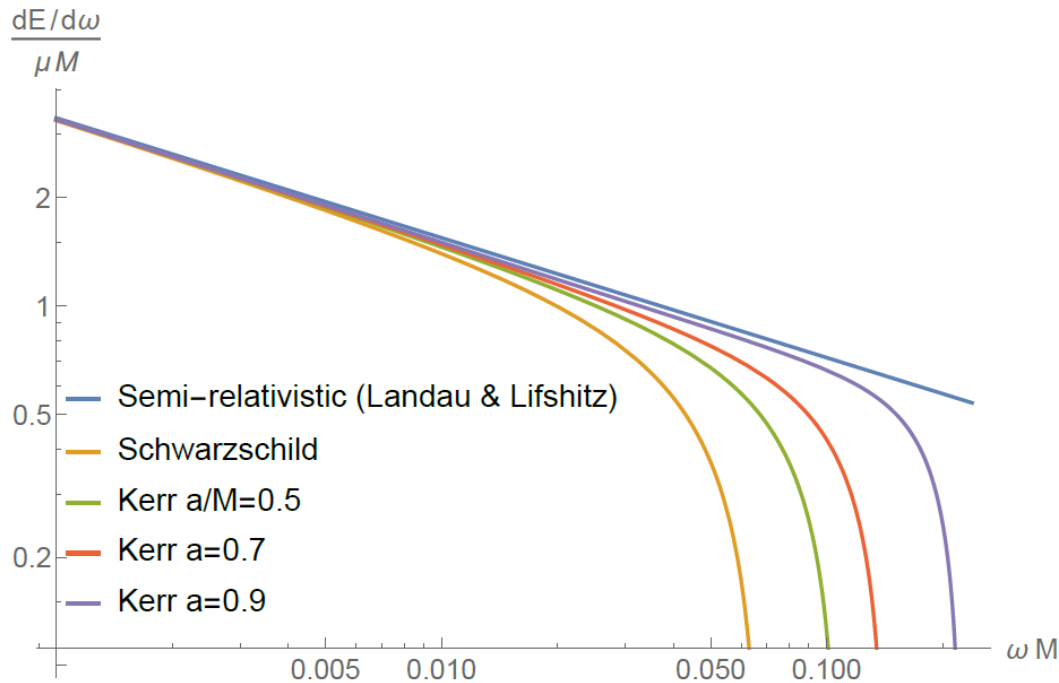
# Gravitational-wave spectrum during the helicoidal-drifting-sequence

$$\frac{dE}{df_s} = \frac{1}{3}(\pi G)^{2/3} M_c^{5/3} f_s^{-1/3}$$

$$f_s = 2f_{\text{orb}}$$

$$M_c = \mu^{3/5} M^{2/5} = \nu^{3/5} M$$

~ power-law spectrum up to near the last circular orbit (LCO) or up to the “contact” distance in the case of NS-NS mergers





# GW spectrum during the final smooth merger?

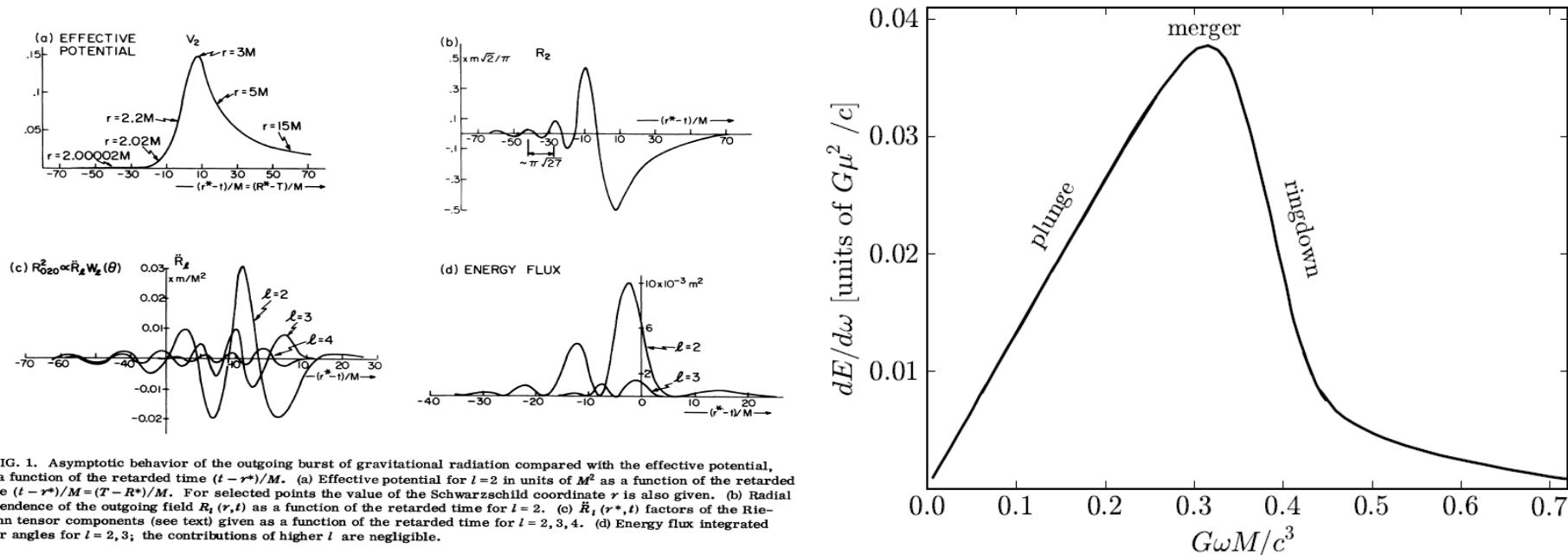


FIG. 1. Asymptotic behavior of the outgoing burst of gravitational radiation compared with the effective potential, as a function of the retarded time  $(t-r^*)/M$ . (a) Effective potential for  $l=2$  in units of  $M^2$  as a function of the retarded time  $(t-r^*)/M = (T-R^*)/M$ . For selected points the value of the Schwarzschild coordinate  $r$  is also given. (b) Radial dependence of the outgoing field  $R_i(r, t)$  as a function of the retarded time for  $l=2$ . (c)  $\tilde{R}_{\alpha\beta}(r^*, t)$  factors of the Riemann tensor components (see text) given as a function of the retarded time for  $l=2, 3, 4$ . (d) Energy flux integrated over angles for  $l=2, 3$ ; the contributions of higher  $l$  are negligible.

Davis, Ruffini, Press, Price, Phys. Rev. Lett. 27, 1466 (1971)

Davis, Ruffini, Tiomno, Phys. Rev. D 5, 2932 (1972)

# Helicoidal-drifting-sequence (HDS)

$$\frac{dE}{df_s} = \frac{1}{3} (\pi G)^{2/3} M_c^{5/3} f_s^{-1/3}$$

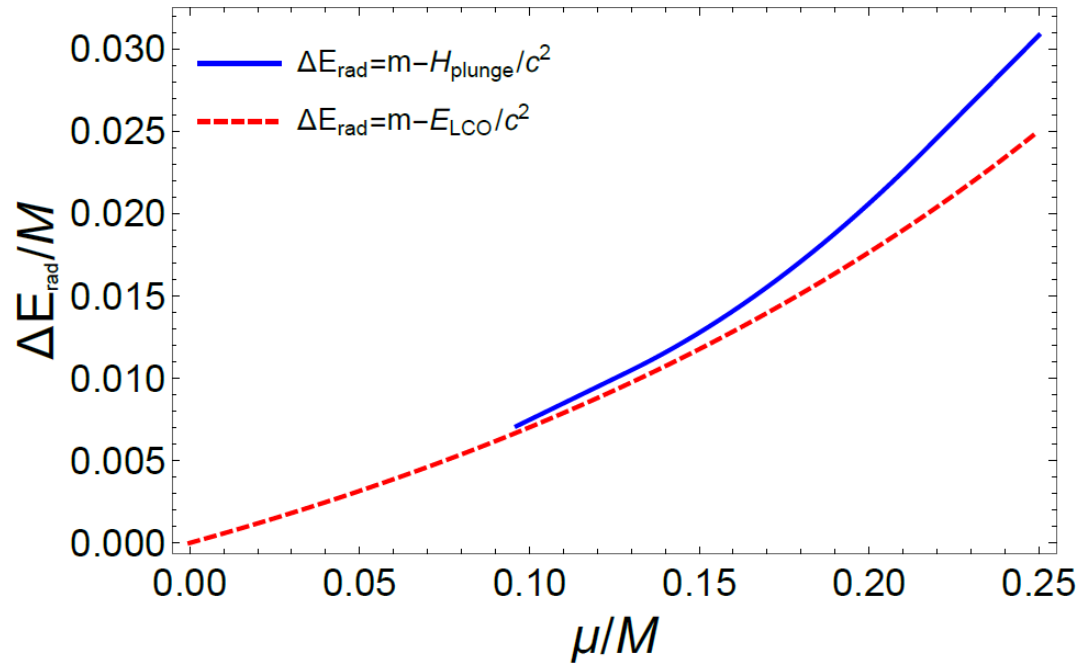
Approximately up to very close the  
last circular orbit (LCO) or  
up to the “contact”

## NS+NS

$$f_{\text{merger}}^{\text{NS-NS}} \approx f_{\text{contact}}^{\text{NS-NS}} = \frac{1}{\pi} \frac{c^3}{GM} \left[ \frac{\mathcal{C}_1 \mathcal{C}_2 (1+q)}{\mathcal{C}_1 + q \mathcal{C}_2} \right]^{3/2}$$

## NS+BH

$$f_{\text{plunge}}^{\text{NS-BH}} \approx \frac{1}{\pi} \left( \frac{GM}{r_{\text{LSO}}^3} \right)^{1/2} = \frac{1}{\pi 6^{3/2}} \left( \frac{c^3}{GM} \right)$$



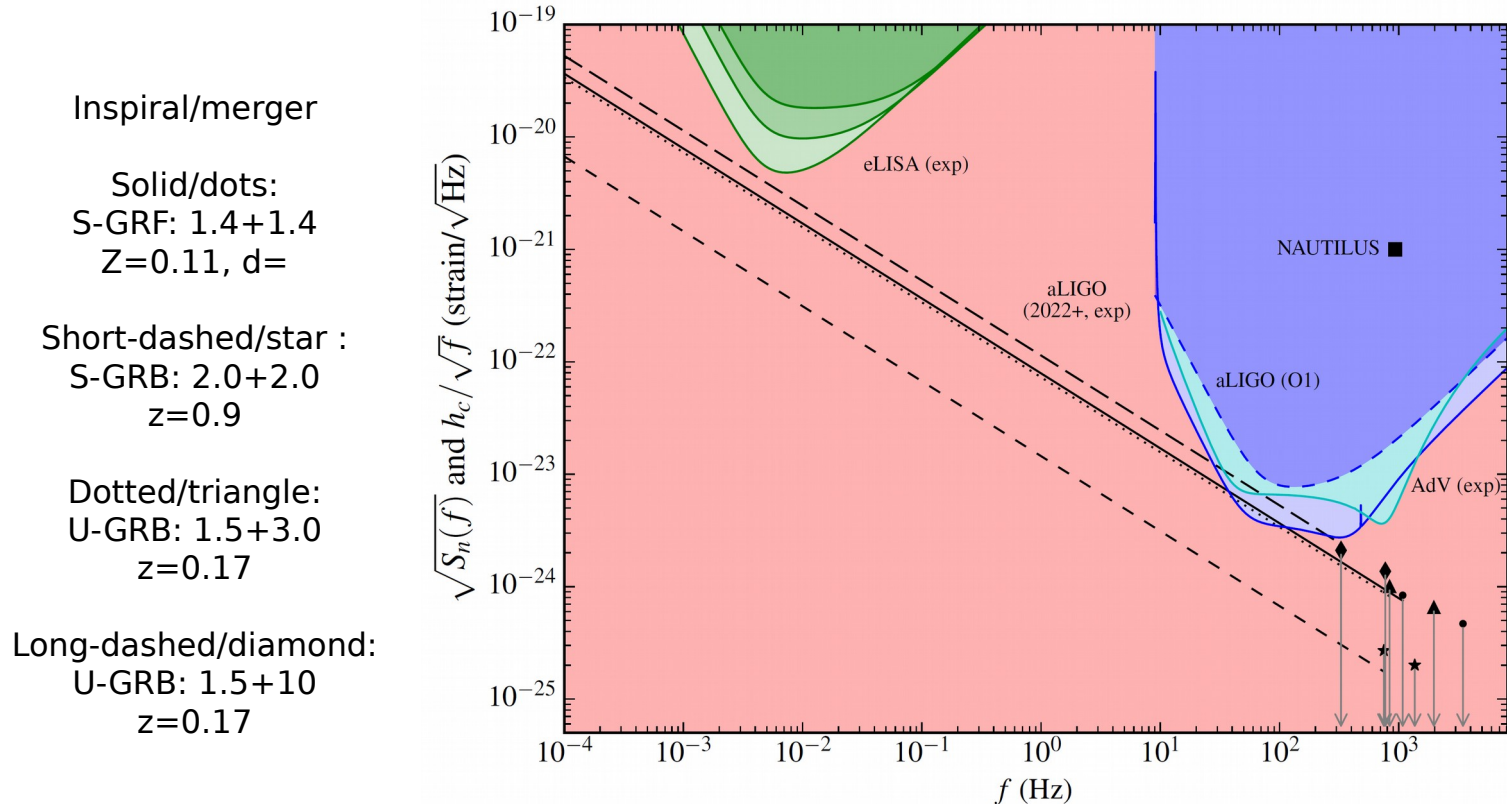
Rodriguez, Rueda, Ruffini, arXiv: 1706.07704  
(last-week post)

Ruffini, Rodriguez,  
Muccino, Rueda et al., arXiv: 1602.03545

# Some properties of the relevant NS-NS and NS-BH mergers

	$\Delta E_{\text{insp}}$ (erg)	$f_{\text{merger}}$ (kHz)	$z_{\text{min}}^{\text{obs}}$	$d_{l_{\text{min}}}$ (Mpc)	$d_{\text{GW}}$ (Mpc)	
					O1	2022+
S-GRF	$7.17 \times 10^{52}$	1.20	0.111	508.70	168.43	475.67
S-GRB	$1.02 \times 10^{53}$	1.43	0.903	5841.80	226.62	640.18
U-GRB	$1.02 \times 10^{53}$	0.98	0.169	804.57	235.62	665.72

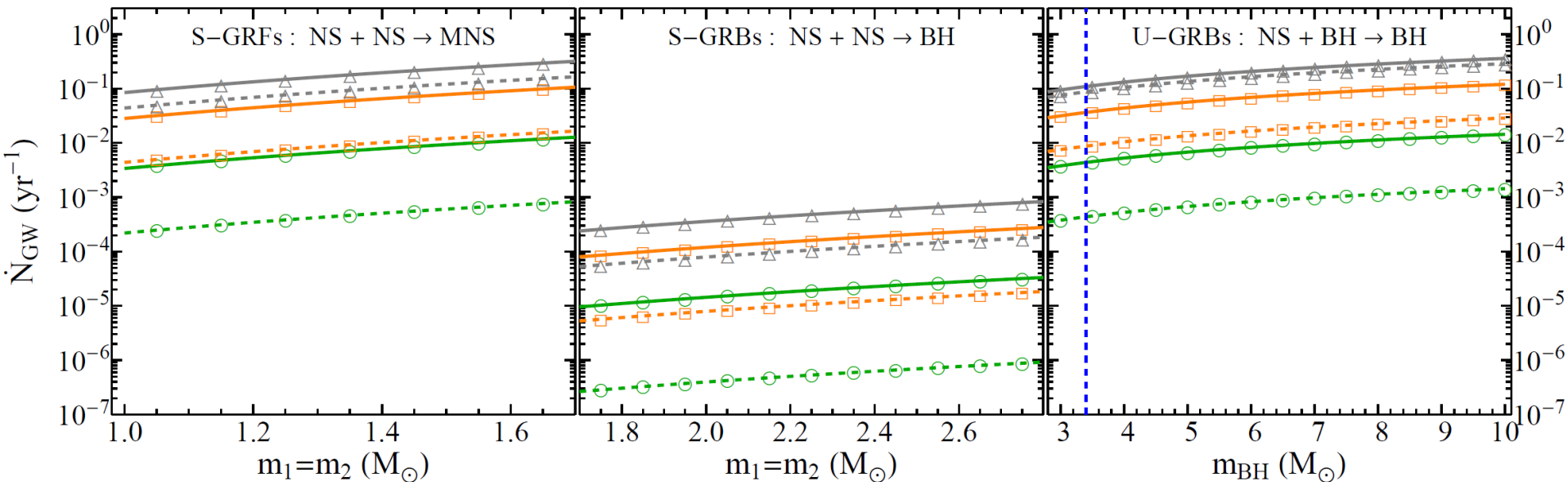
# GW detectability by aLIGO, eLISA and resonant bars



Ruffini, Rodriguez, Muccino, Rueda et al., arXiv: 1602.03545  
aLIGO sensitivity from Abbott et al., Liv. Rev. Rel. 19 (2016)  
ELISA sensitivity from Klein et al. PRD 93, 024003 (2016)  
NAUTILUS sensitivity from Astone et al., CQG 25, 114048 (2008)

# Detectability of GRB GWs by aLIGO

Ruffini, Rodriguez, Muccino, Rueda et al., arXiv: 1602.03545



$$\dot{N}_{\text{GW}} = \rho_{\text{GRB}} V_{\text{max}}^{\text{GW}}$$

$$V_{\text{max}}^{\text{GW}} = (4\pi/3)\mathcal{R}^3$$

$\mathcal{R}$  is the GW “range”; the values for aLIGO from: Abbott et al., Liv. Rev. Rel. 19 (2016)

# IN CONCLUSION:

GRB sub-class	$\dot{N}_{\text{GRB}}$ ( $\text{yr}^{-1}$ )	$\dot{N}_{\text{GRB}}^{\text{obs}}$ ( $\text{yr}^{-1}$ )	$\dot{N}_{\text{GW}}$ ( $\text{yr}^{-1}$ )
XRFs	144–733	1 (1997–2014)	undetectable
BdHNe	662–1120	14 (1997–2014)	undetectable
BH-SN	$\lesssim$ 662–1120	$\lesssim$ 14 (1997–2014)	undetectable
S-GRFs	58–248	3 (2005–2014)	O1: $(0.4\text{--}8)\times 10^{-3}$ O3: 0.011–0.065 2022+: 0.1–0.2
S-GRBs	2–8	1 (2006–2014)	O1: $(0.4\text{--}8)\times 10^{-6}$ O3: $(0.08\text{--}1.2)\times 10^{-4}$ 2022+: $(0.8\text{--}3.6)\times 10^{-4}$
U-GRBs	662–1120	–	O1: $(0.36\text{--}3.6)\times 10^{-3}$ O3: 0.008–0.032 2022+: 0.076–0.095

For more details see: Ruffini, Rodriguez, Muccino, Rueda et al.; arXiv: 1602.03545