

Tidal Deformability of Neutron Stars and Gravitational Waves

Chang-Hwan Lee / Pusan National University

in collaboration with
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Yeunhwan Lim (Texas A&M), Chang Ho Hyun (Daegu)

Master in Science

Journal of the Korean Physical Society, Vol. 24, No. 2, April 1991, pp. 184~186

SHORT NOTE

Dibaryon from 't Hooft Instanton

Dong Pil MIN and Chang Hwan LEE

Department of Physics, Seoul National University, Seoul 151-742

(Received 11 January 1991)

Recently, Manton suggested that a Skyrmion field in R^3 may be generated from an $SU(2)$ instanton. Following the suggestion of Manton, we construct a $B=2$ Skyrmion from a 't Hooft instanton. We discuss the physical implication of such quantities as the baryon number distribution, the Skyrmion mass, and the interaction energy between two nucleons. The above quantities are treated as functions of the separation distance and a scale factor.

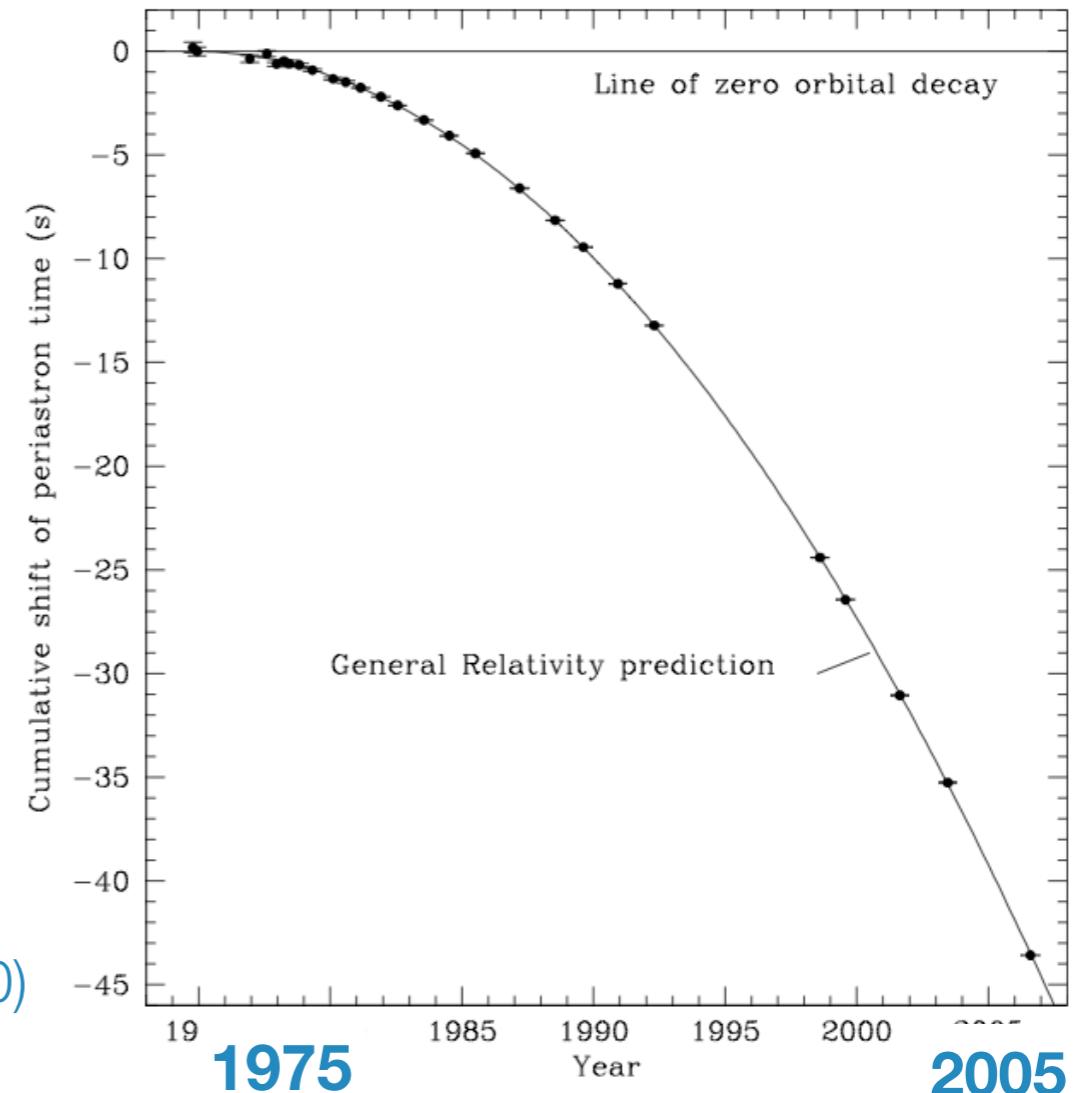
HK Lee's talk on Sep. 14th



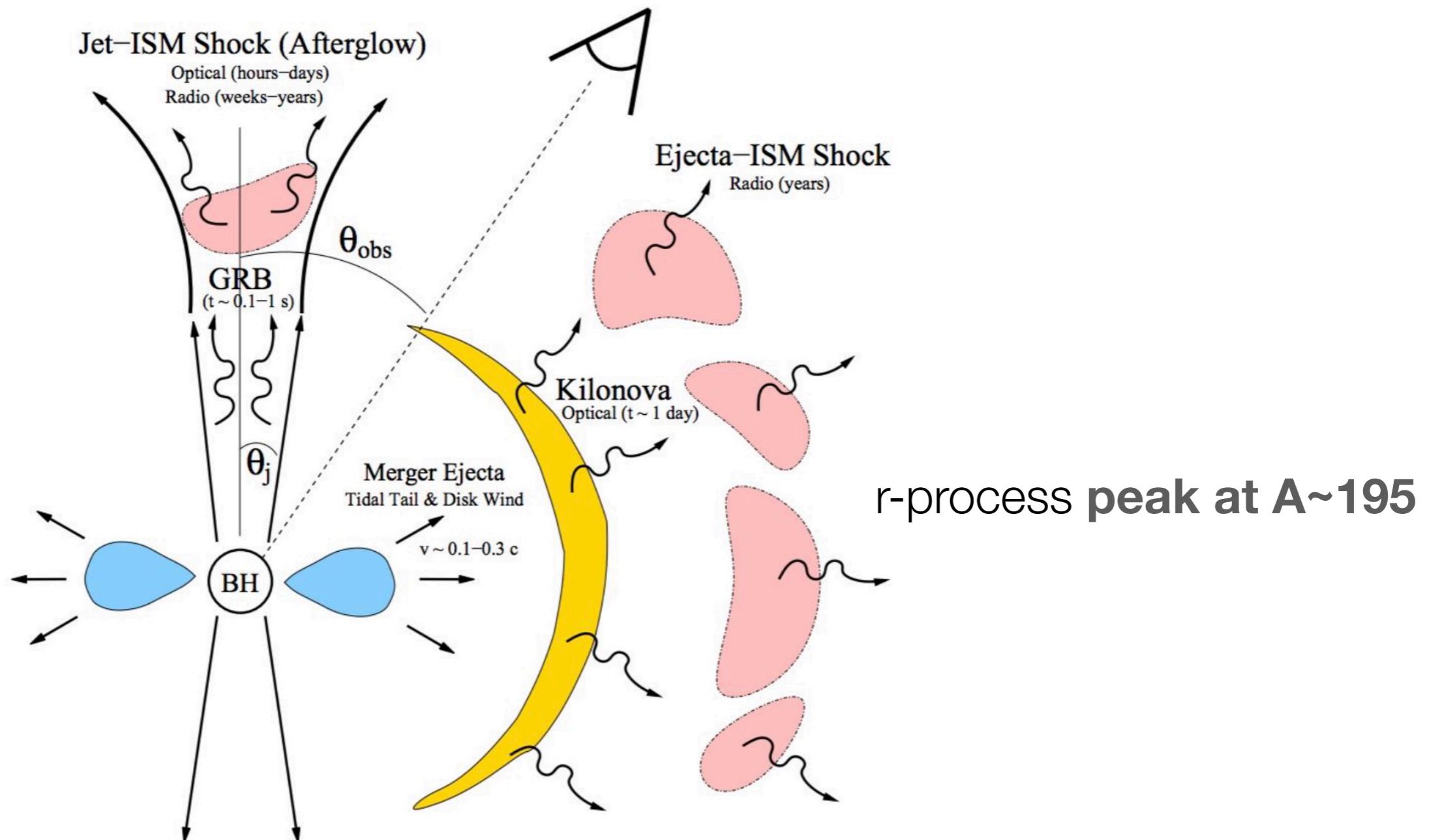
Gravitational waves from neutron star binaries

- B1913+16 / Hulse & Taylor (1975)
- change in the orbital period due to GW radiation
- 1993 Nobel Prize
- LIGO is based on NS binary mergers
- GW expected in **2019**
 $d = O(100 \text{ Mpc})$

Weisberg, Nice, Taylor, ApJ (2010)

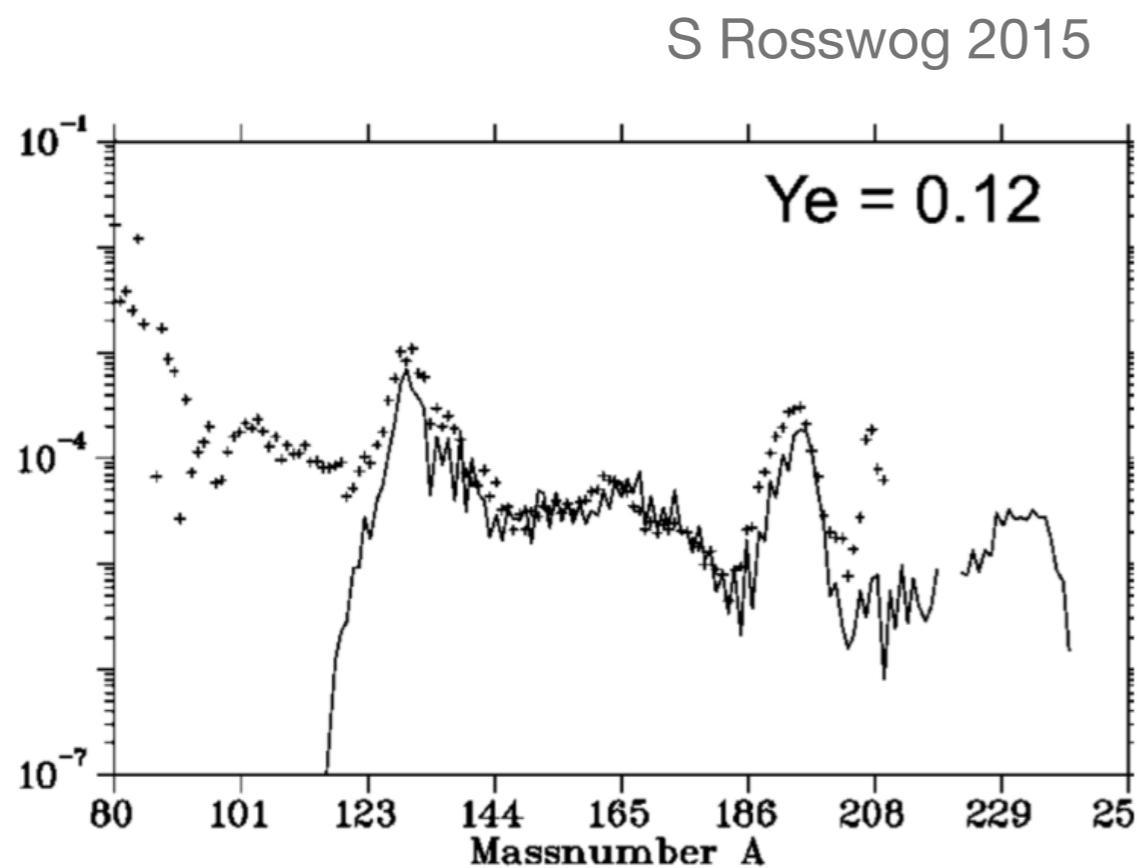


GRB and Kilonova from NS binaries



Heavy Elements from NS mergers

Sources of Heavy Elements



solar pattern vs NS-merger

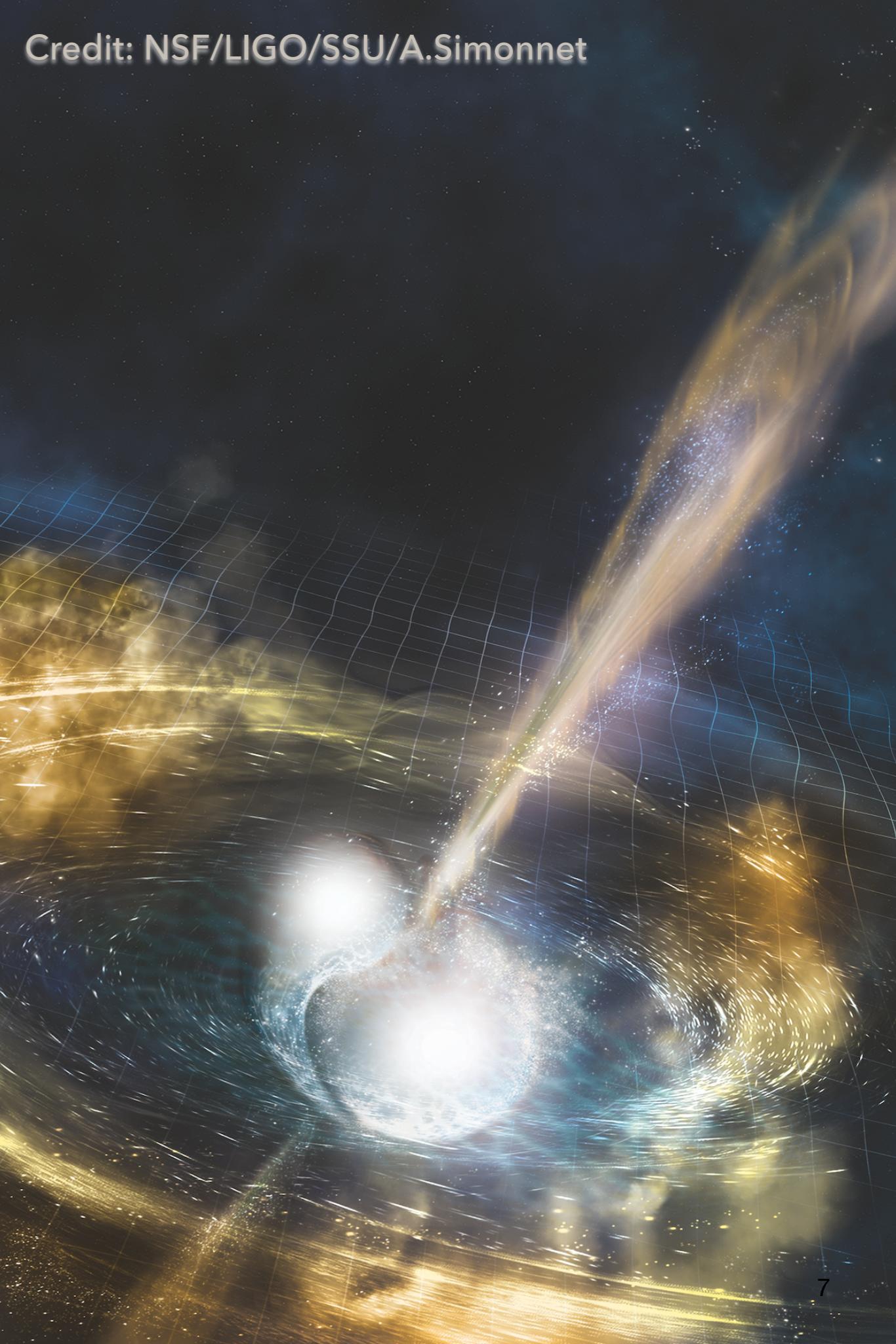
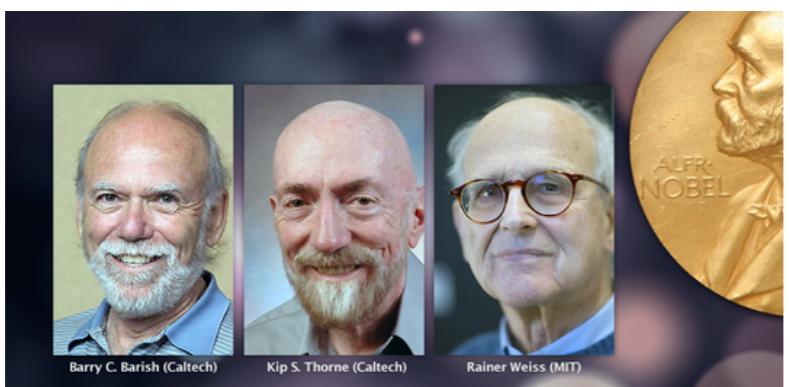
- **Supernovae:**
neutrino-driven wind
r-process **peak at $A \sim 130$**
- **NS mergers:**
r-process **peak at $A \sim 195$**

Press Release Oct 16, 2017

GW from Binary NS Mergers

GW 170817 ($d=40 \text{ Mpc}$)
GRB 170817A by Fermi-GBM
Kilonova/X-ray/Optical Afterglows

*soon after the announcement of
2017 Nobel Prize*





GW170817



LIGO/University of Oregon/Ben Farr

GW170817

Binary Neutron Star Mergers
Oct 16, 2017



GW170817



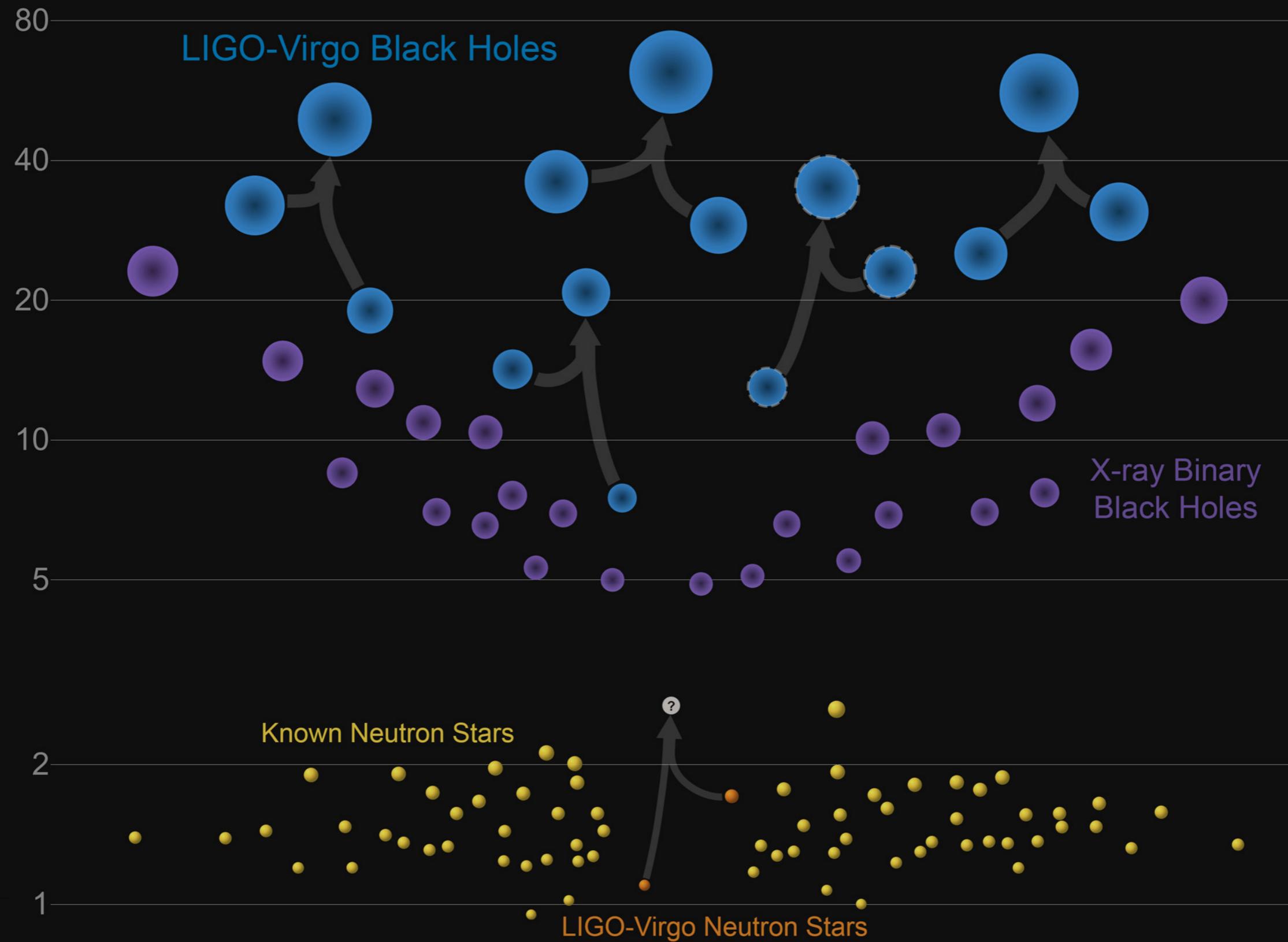
LIGO/University of Oregon/Ben Farr

GW170817

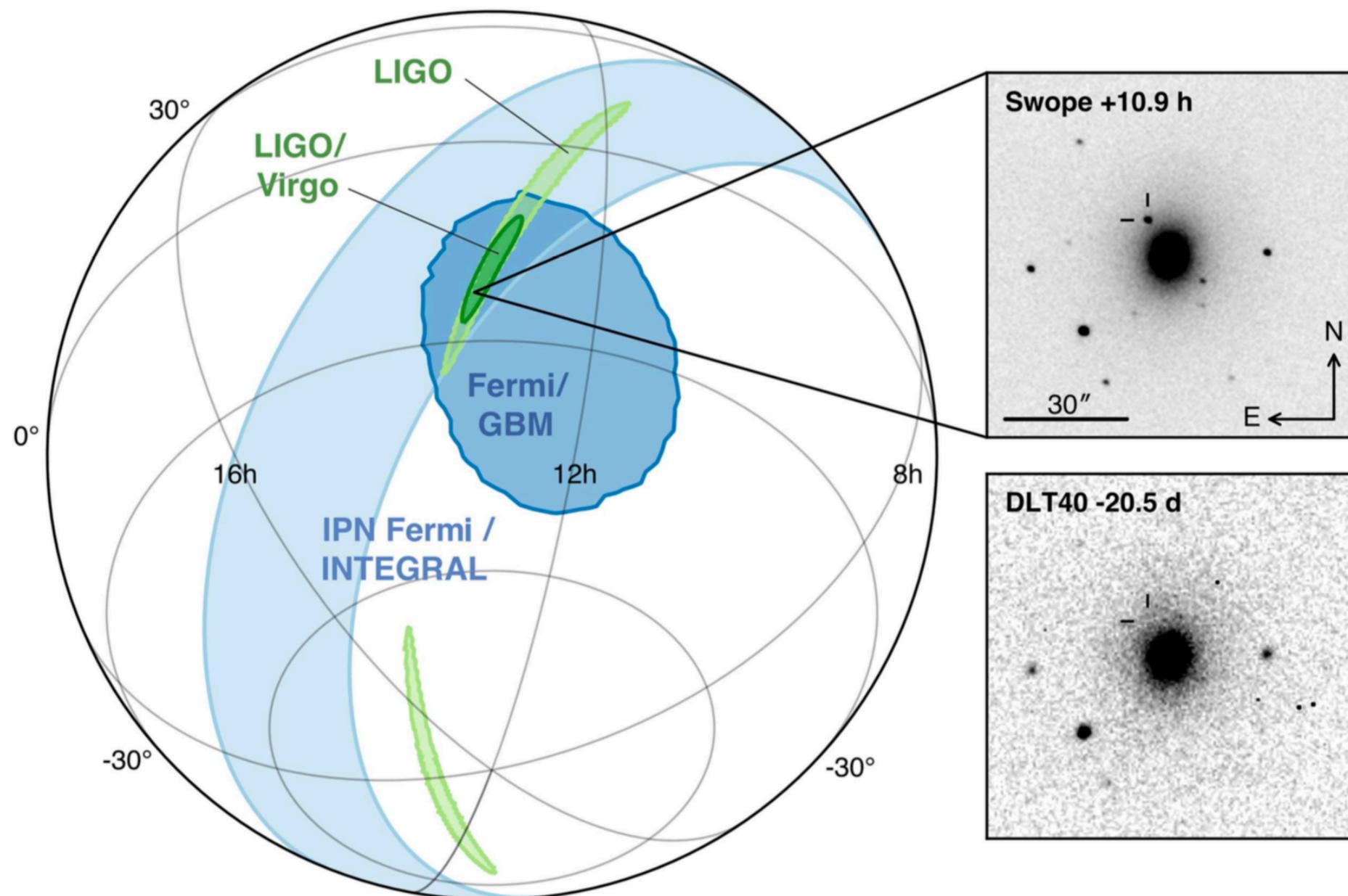
Binary Neutron Star Mergers
Oct 16, 2017

Masses in the Stellar Graveyard

in Solar Masses

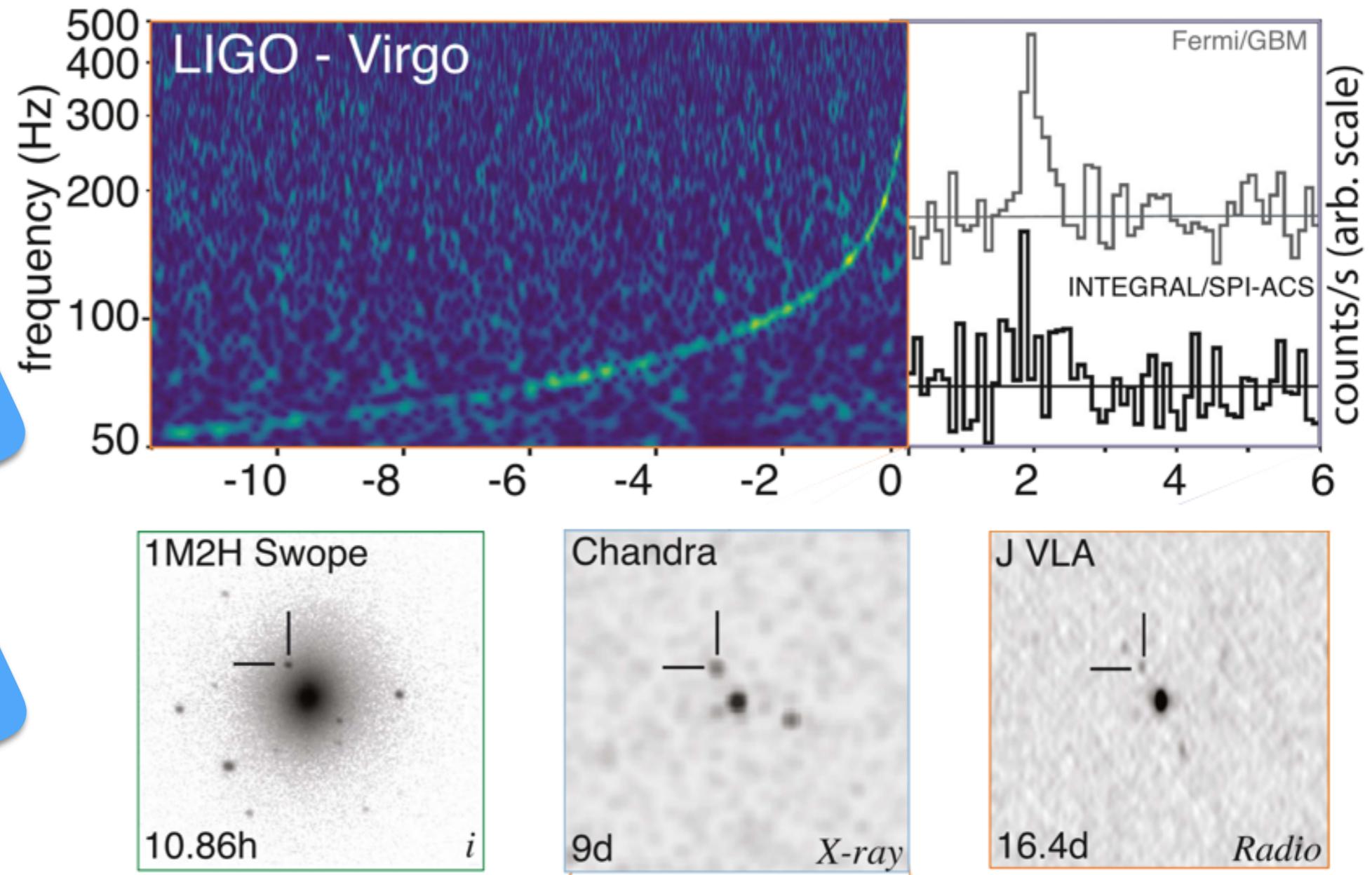


GW170817 / GRB170817A



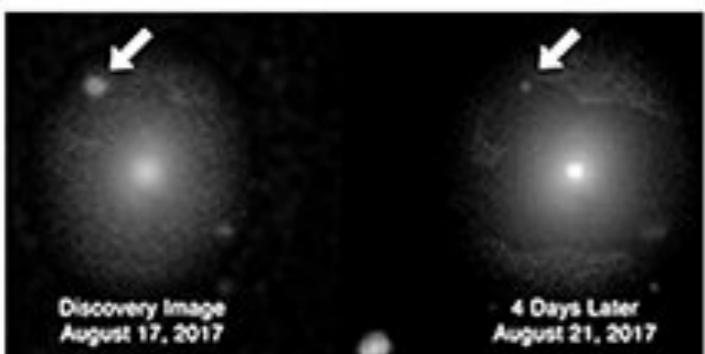
First event of Multi-messenger Astronomy

GW170817
GRB170817A
SSS17al
AT2017gfo



TIMELINE

중성자별 충돌에서 발생한 중력파, 감마선, 가시광선, 엑스선 및 전파 관측



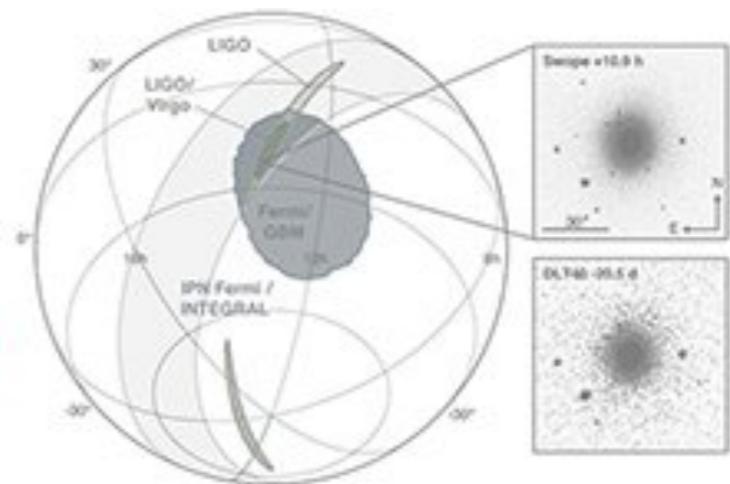
Telescopes in Chile

2017.08.17.
12:41:04 UTC

라이고 및 비르고
중력파 신호
포착

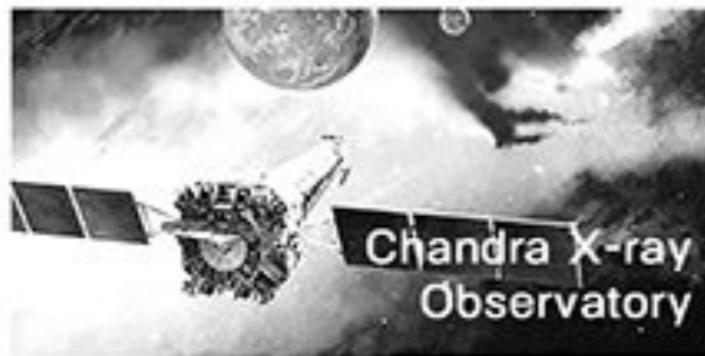
+2
seconds

페르미 및 인티그랄
감마선 신호
포착



Fermi/Integral
gamma-ray

<http://horizon.kias.re.kr>



Chandra X-ray



Korean Telescopes

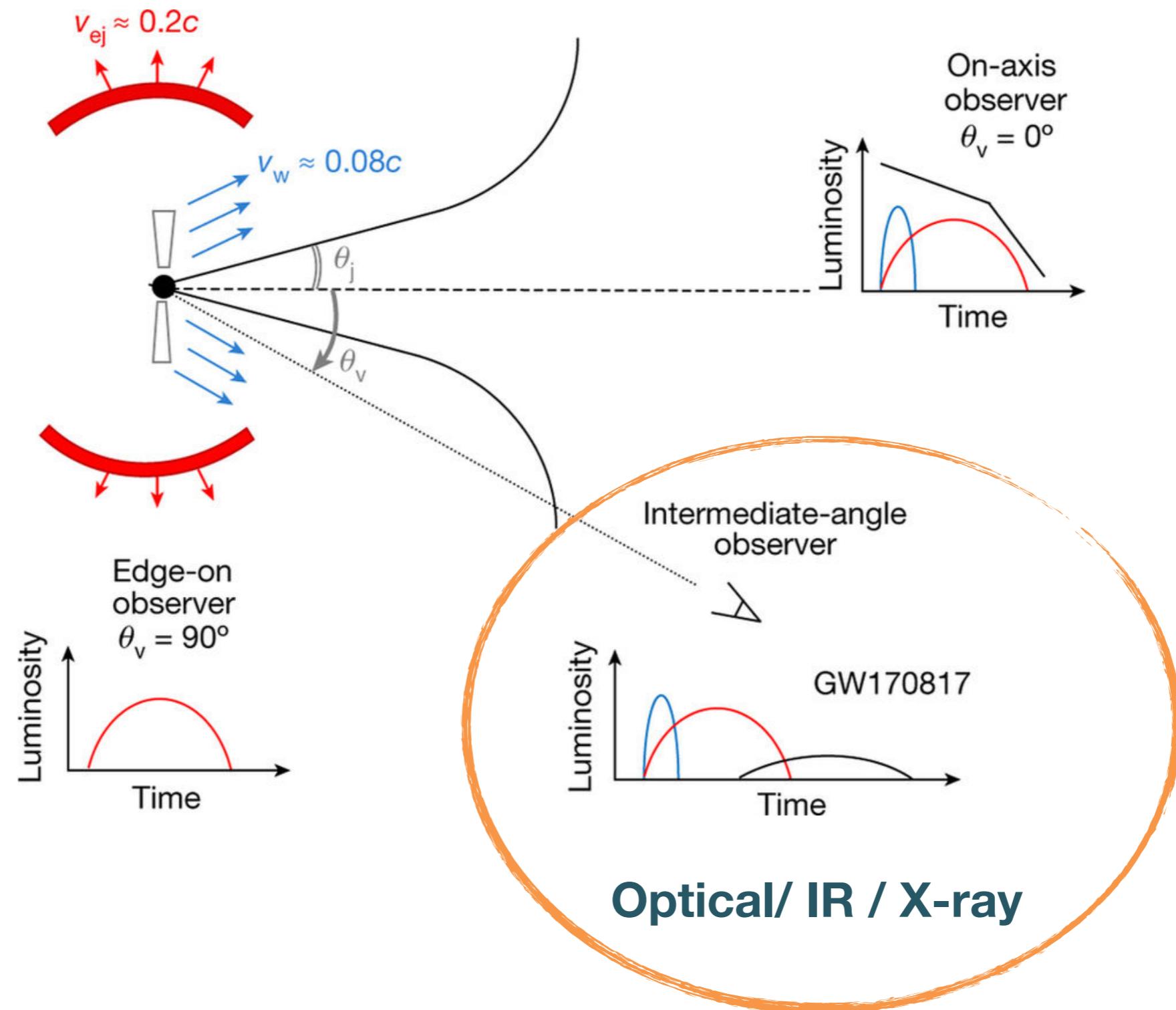
Nature 551, 71 (2017)



VLA radio

Kilonova / Geometry of GW170817

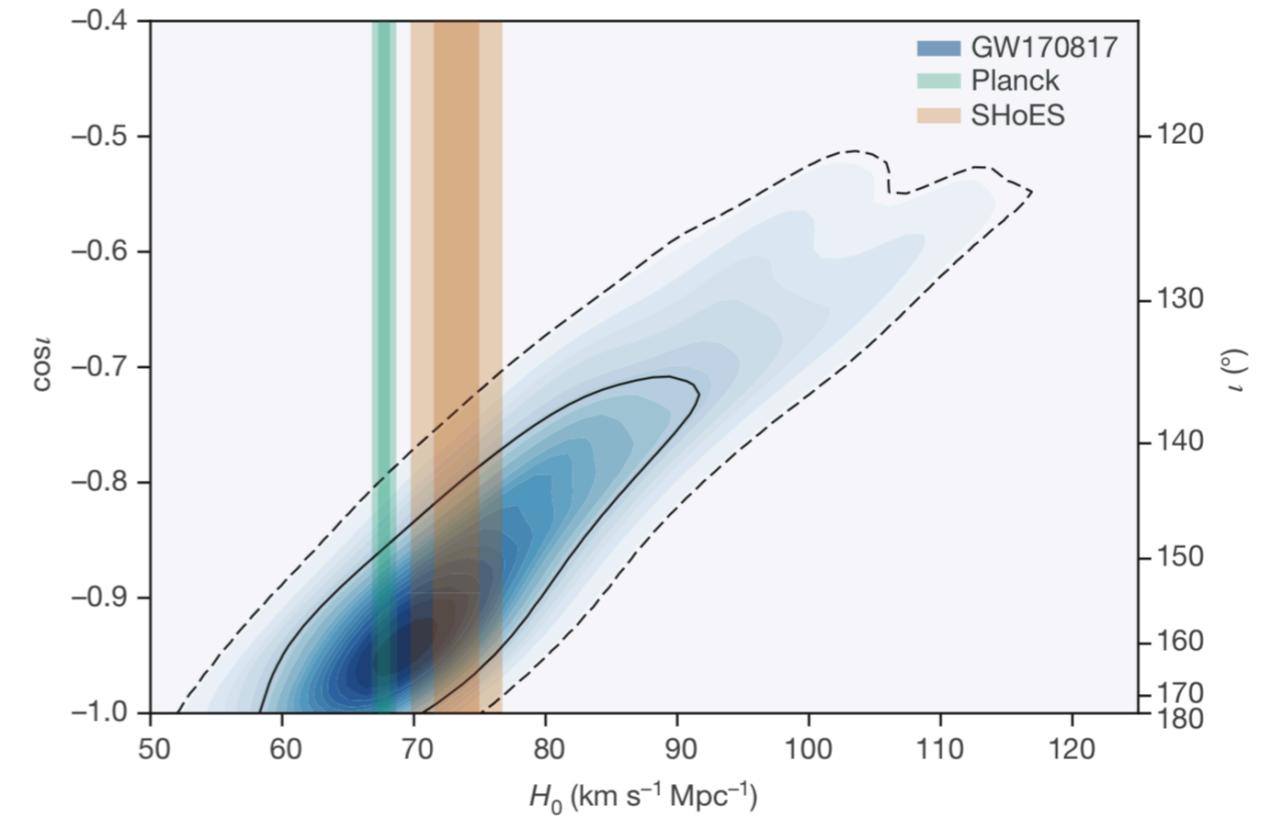
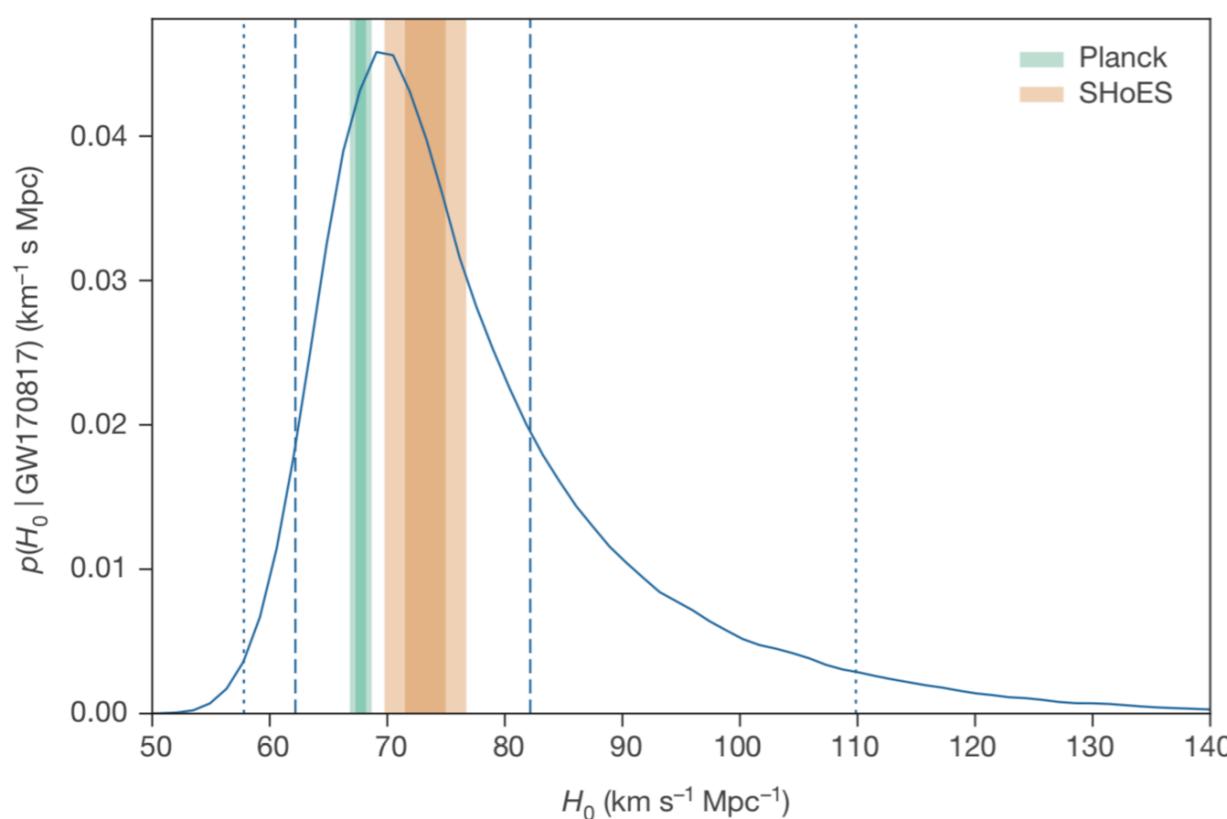
Nature 551, 71 (2017)



A gravitational-wave standard siren measurement of the Hubble constant

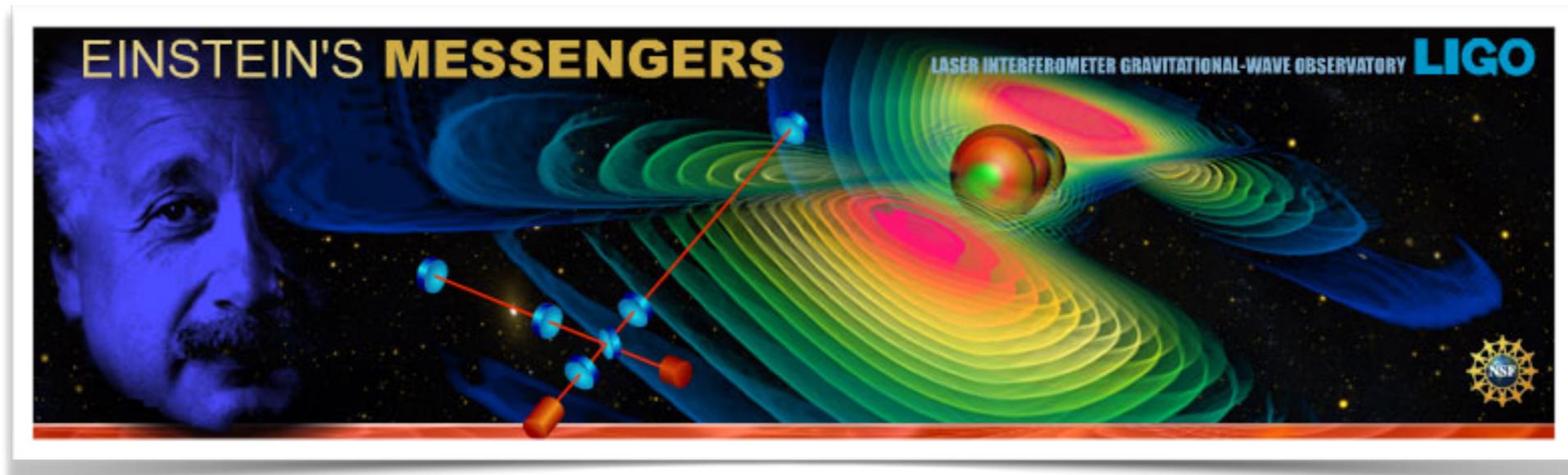
The LIGO Scientific Collaboration and The Virgo Collaboration*, The 1M2H Collaboration*, The Dark Energy Camera GW-EM Collaboration and the DES Collaboration*, The DLT40 Collaboration*, The Las Cumbres Observatory Collaboration*, The VINROUGE Collaboration* & The MASTER Collaboration*

$$H_0 = 70.0^{+12.0}_{-8.0} \text{ km s}^{-1} \text{Mpc}^{-1}$$



Gravitational-Wave & Multi-Messenger Astronomy

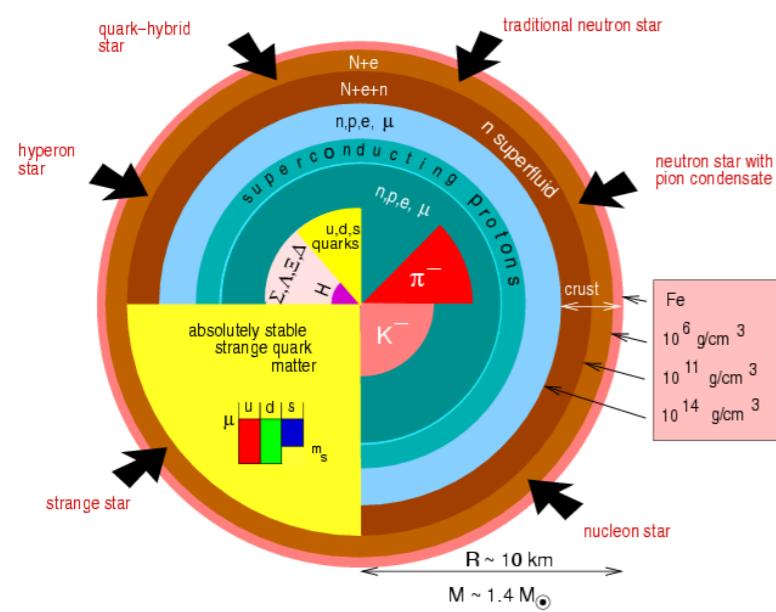
- First direct detection of GW in 2015
- First detection of BHs with masses $30 \sim 60$ solar mass
- **GW, Gamma-ray, Optical, X-ray, Radio from NS mergers**
- New era for GW Astronomy & **Multi-Messenger Astronomy**



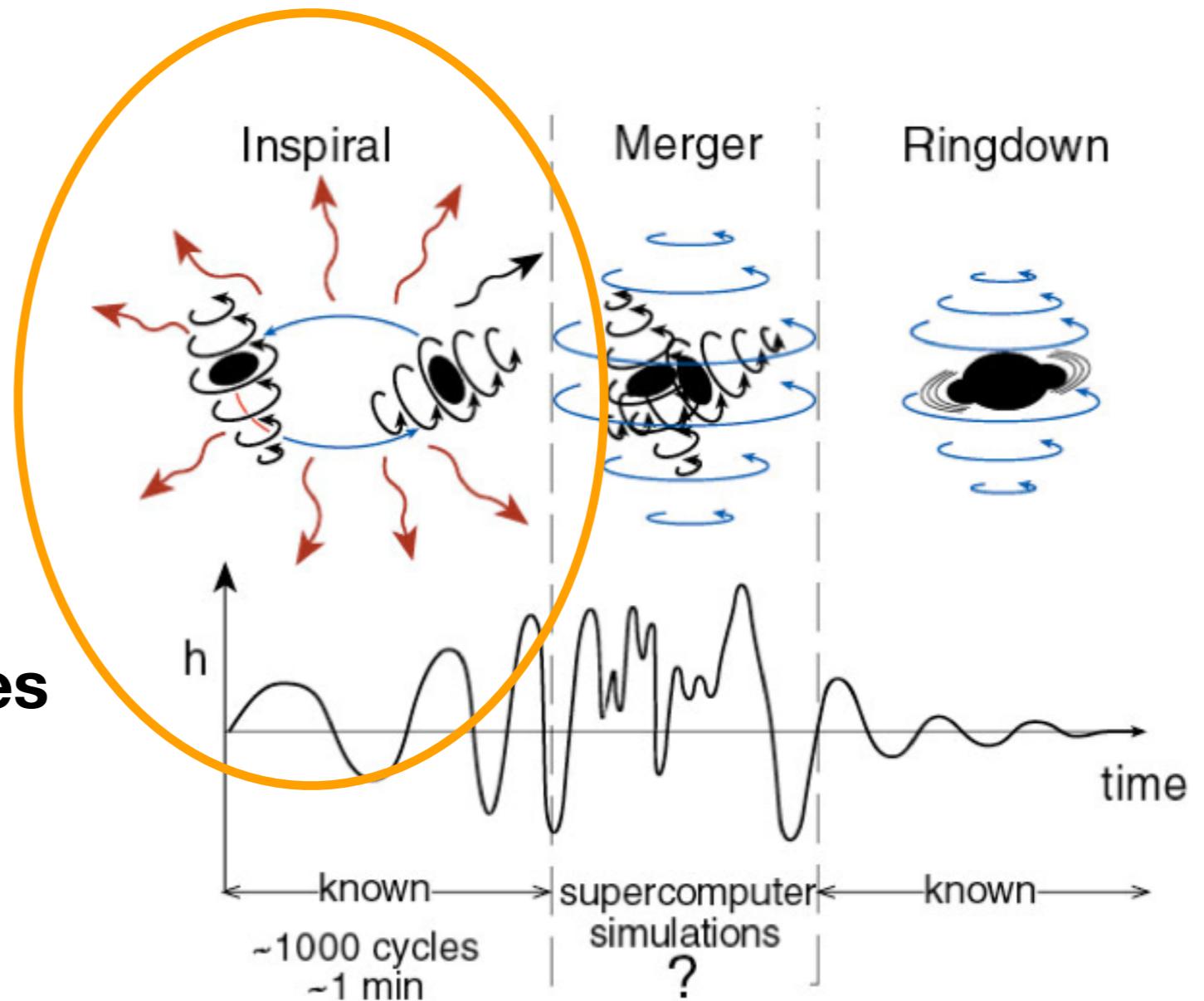
NS in new era of GW & multi-messenger astronomy

Tidal Love number & Deformability

Response of NS to GW during Inspiral



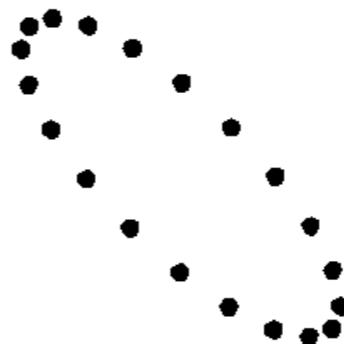
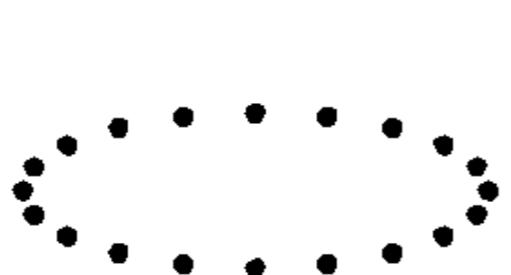
perturbative approaches



Tidal deformability & Love number

Selected references

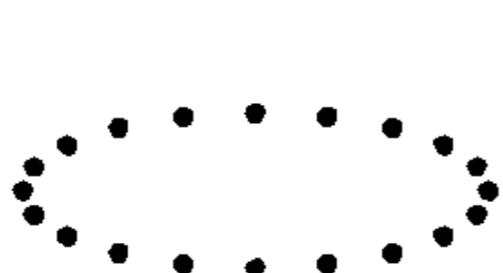
- **A.E.H. Love** (1909) - The Yielding of the Earth to Disturbing Forces
- **K.S. Thorne** & A. Campolattaro (1967) - non-radial pulsation of NS
- J.B. Hartle & **K.S. Thorne** (1969) - stability of rotating NS
-
- **K.S. Thorne** (1998) - Tidal stabilization of rigid rotating, fully relativistic neutron star
-



Tidal deformability & Love number

Selected references

- **A.E.H. Love** (1909) - The Yielding of the Earth to Disturbing Forces
- **K.S. Thorne** & A. Campolattaro (1967) - non-radial pulsation of NS
- J.B. Hartle & **K.S. Thorne** (1969) - stability of rotating NS
-
- **K.S. Thorne** (1998) - Tidal stabilization of rigid rotating, fully relativistic neutron star
-



Tidal deformability & Love number

$$-\frac{(1+g_{tt})}{2} = -\frac{m}{r} - \frac{3Q_{ij}}{2r^3} \left(n^i n^j - \frac{1}{3} \delta^{ij} \right) + \mathcal{O}\left(\frac{1}{r^3}\right) + \frac{\mathcal{E}_{ij}}{2} r^2 n^i n^j + \mathcal{O}(r^3)$$

\mathcal{E}_{ij} : external quadrupole tidal field

Q_{ij} : quadrupole moment of NS

λ : Tidal deformability

$$Q_{ij} = -\lambda \mathcal{E}_{ij}$$

$$Q_{ij} = \int d^3x \delta\rho(x) \left(x_i x_j - \frac{1}{3} r^2 \delta_{ij} \right)$$

$$n^i = \frac{x^i}{r}$$

dimensionless parameter

k_2 : $l=2$ Tidal Love number

$$k_2 = \frac{3}{2} G \lambda R^{-5}$$

Hinderer et al. PRD 81 (2010)

Systematic Parameter Errors in Inspiring Neutron Star Binaries

Marc Favata*

$$\tilde{h}_T(f) = \mathcal{A}f^{-7/6}e^{i\Psi_T}(f)$$

$$\begin{aligned}\Psi_T(f) = & \varphi_c + 2\pi f t_c + \frac{3}{128\eta v^5} (\Delta\Psi_{3.5\text{PN}}^{\text{pp}} \\ & + \Delta\Psi_{3\text{PN}}^{\text{spin}} + \Delta\Psi_{2\text{PN}}^{\text{ecc.}} + \Delta\Psi_{6\text{PN}}^{\text{tidal}} + \Delta\Psi_{6\text{PN}}^{\text{tm}})\end{aligned}$$

$$v = (\pi f M)^{1/3}$$

$$v/c = (GM\pi f/c^3)^{1/3}$$

$$\Delta\Psi_{6\text{PN}}^{\text{tidal}} = -\frac{39}{2}\tilde{\Lambda}v^{10} + v^{12}\left(\frac{6595}{364}\delta\tilde{\Lambda} - \frac{3115}{64}\tilde{\Lambda}\right)$$

$$\begin{aligned}\tilde{\Lambda} \equiv & 32\frac{\tilde{\lambda}}{M^5} = \frac{8}{13}[(1+7\eta-31\eta^2)(\hat{\lambda}_1+\hat{\lambda}_2) \\ & - \sqrt{1-4\eta}(1+9\eta-11\eta^2)(\hat{\lambda}_1-\hat{\lambda}_2)].\end{aligned}$$

Systematic Parameter Errors in Inspiring Neutron Star Binaries

Marc Favata*

phase shift vs deformability

$$\left. \frac{d\Phi}{dx} \right|_T = -\frac{195}{8} \frac{x^{3/2}}{\eta} \frac{\tilde{\lambda}}{M^5} \propto \frac{\tilde{\lambda}}{M^5}$$

$$x = (\omega M)^{2/3} \Rightarrow \left(\omega \frac{GM}{c^3} \right)^{2/3}$$

$$\eta = m_1 m_2 / M^2$$

dimensionless

$$\Lambda = \frac{\lambda}{m^5} \Rightarrow G\lambda \left(\frac{c^2}{Gm} \right)^5 \approx 950.5 \left(\frac{m_\odot}{m} \right)^5 \left(\frac{\lambda}{10^{36} \text{ g cm}^2 \text{ s}^2} \right)$$

$$\Lambda = G \left(\frac{c^2}{Gm} \right)^5 \times \frac{2}{3} \frac{R^5}{G} k_2 = \frac{2}{3} \left(\frac{R c^2}{Gm} \right)^5 k_2 \approx 9495 \left(\frac{R_{10\text{km}}}{m_{M_\odot}} \right)^5 k_2$$

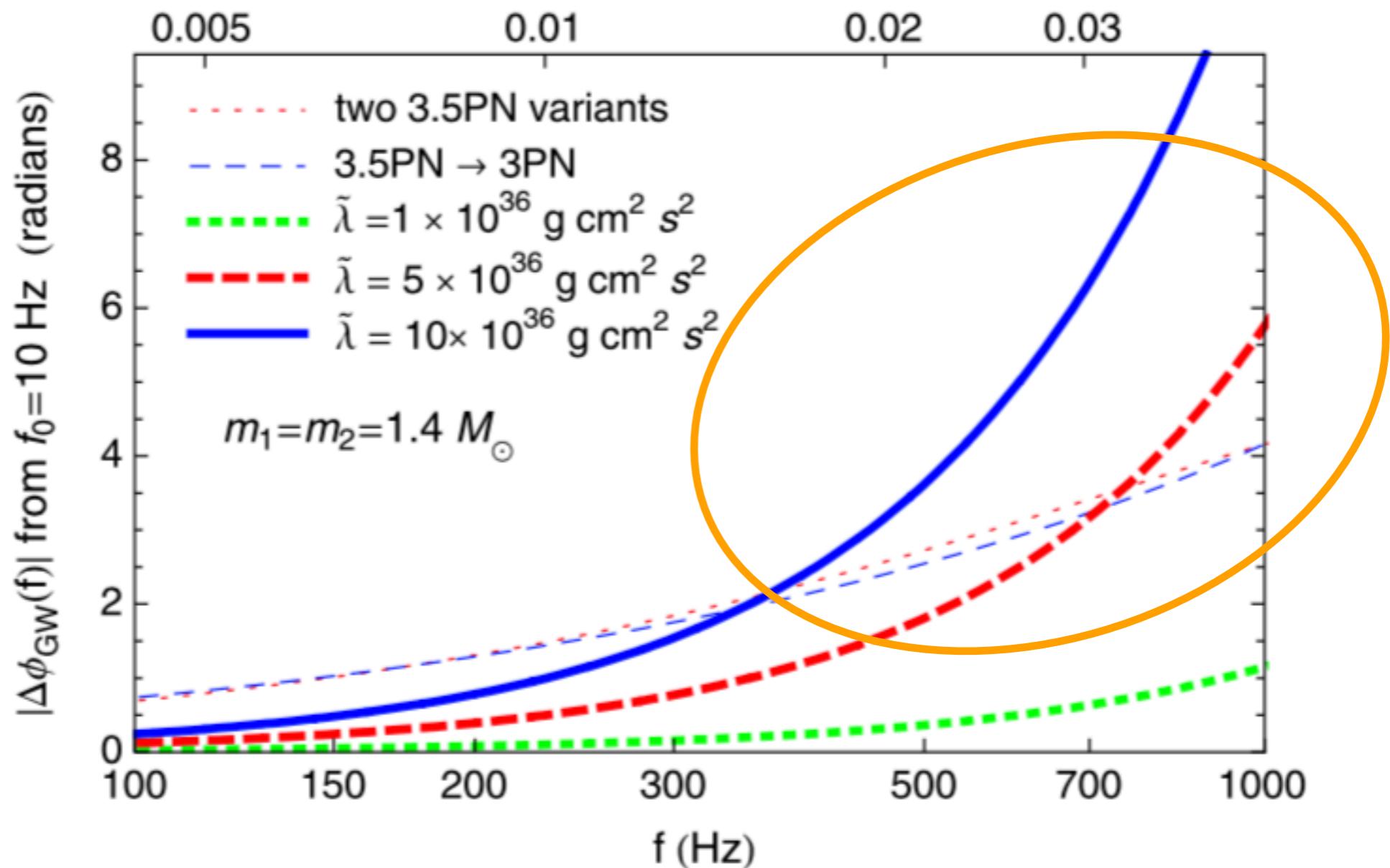
accumulated GW phase

PHYSICAL REVIEW D 81, 123016 (2010)

Tidal deformability of neutron stars with realistic equations of state and their gravitational wave signatures in binary inspiral

Tanja Hinderer,¹ Benjamin D. Lackey,² Ryan N. Lang,^{3,4} and Jocelyn S. Read⁵

$$|\Delta\phi_{\text{GW}}(f)| = |\Phi_{3.5,\text{pp}}(f_{\text{GW}}) - \Phi_{3.5,\lambda}(f_{\text{GW}})|$$



Accumulated GW phase

the number of wave cycles in frequency domain

$$\Delta N_{\text{cyc}, \Psi} = \frac{1}{2\pi} \left[\Psi(f_2) - \Psi(f_1) + (f_1 - f_2) \frac{d\Psi}{df_1} \right]$$

$f_1 = 10 \text{ Hz}$,

the low frequency cutoff for Advanced LIGO due to seismic noises

Waveform models:

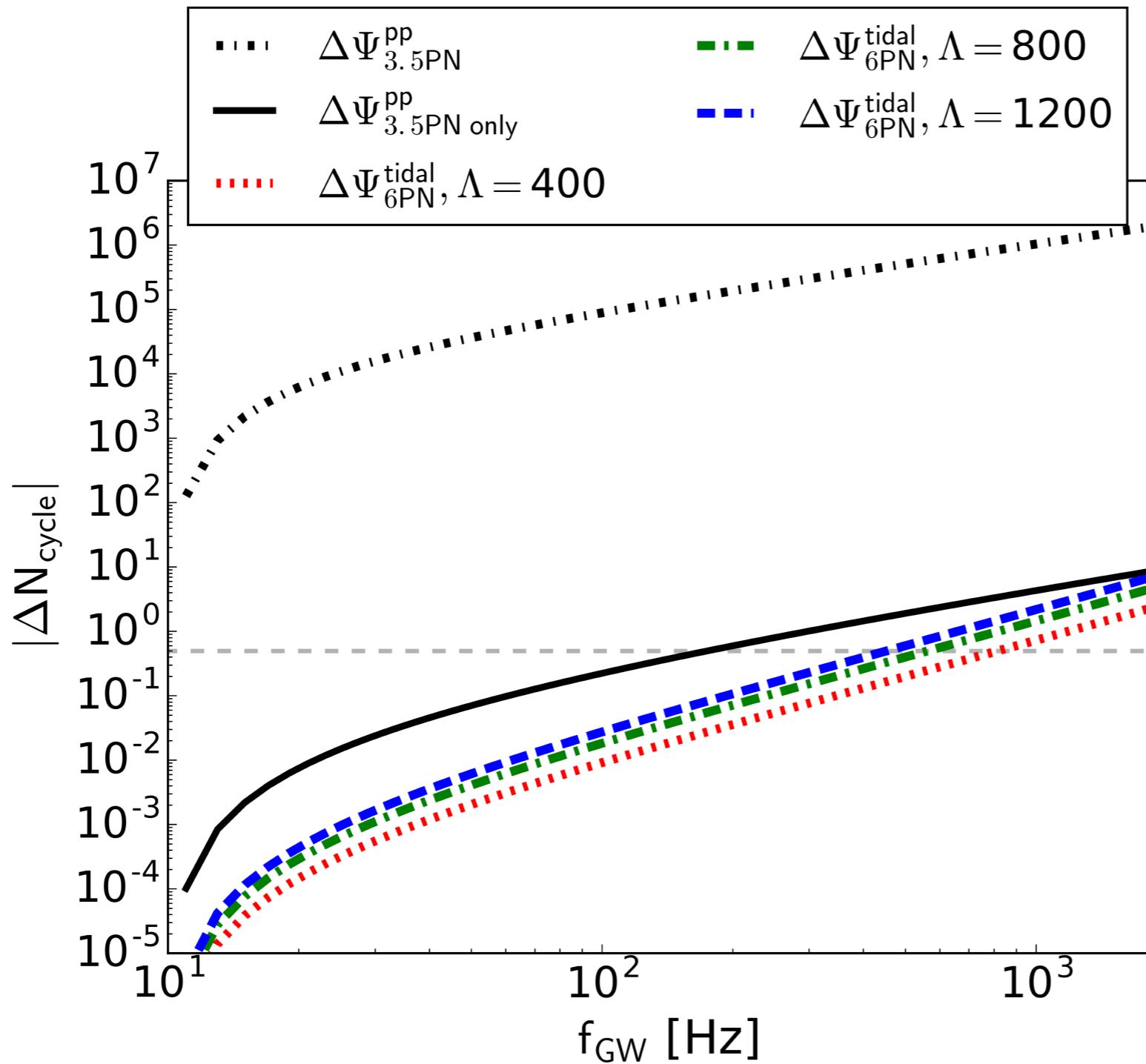
TaylorT2 for ΔN_{cyc}

TaylorF2(SPA) $\Delta N_{\text{cyc}, \Psi}$

Moore et al., PRD.93.124061(2016)

	1.4M _⊙ + 1.4M _⊙ , f ₂ = 1000 Hz		
PN order	ΔN_{cyc}	$\Delta N_{\text{cyc}, \Psi}$	$\Delta N_{\text{useful}}^{\text{norm}}$
0PN(circ)	16 031	986 372	1821
0PN(ecc)	-463	-36 137	-6.37
1PN(circ)	439	21 743	125
1PN(ecc)	-15.8	-1193	-0.332
1.5PN(circ)	-208	-8520	-94.8
1.5PN(ecc)	1.67	103	0.113
2PN(circ)	9.54	294	6.70
2PN(ecc)	-0.215	-15.4	-0.008 17
2.5PN(circ)	-10.6	-218	-10.6
2.5PN(ecc)	0.0443	2.61	0.004 73
3PN(circ)	2.02	18.2	2.80
3PN(ecc)	0.002 00	0.119	-0.000 238
3.5PN(circ)	-0.662	-4.39	-0.977
Total	15 785	962 445	1843

accumulated GW phase

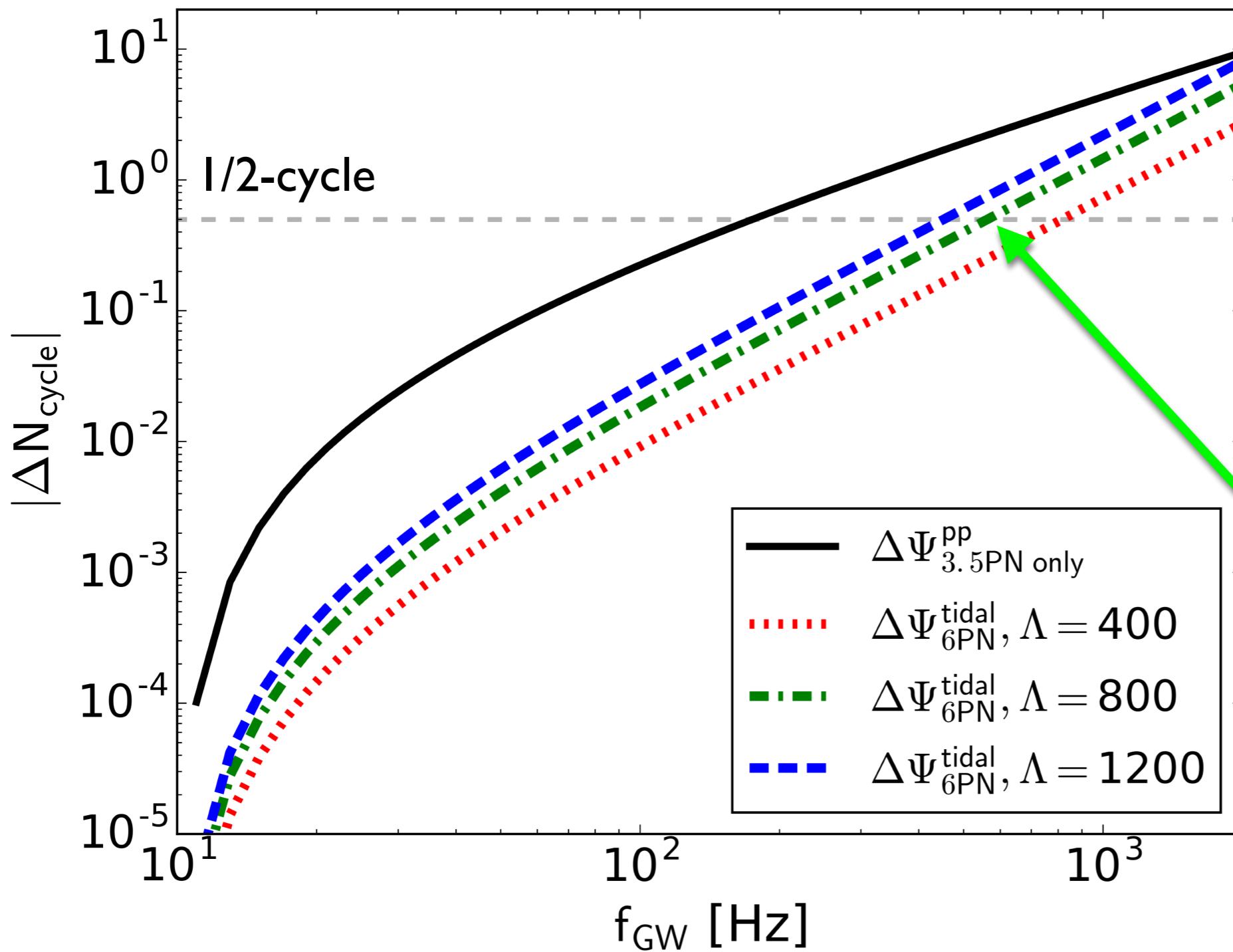


waveform model:
TaylorF2(SPA)

$M_{\text{ch}} = 1.188 M_{\odot}$

$M_1 = M_2 = 1.365 M_{\odot}$

accumulated GW phase



waveform model:
TaylorF2(SPA)

$M_{\text{ch}} = 1.188 M_{\odot}$

$M_1 = M_2 = 1.365 M_{\odot}$

~ 600 Hz

Measurement error vs. source distance

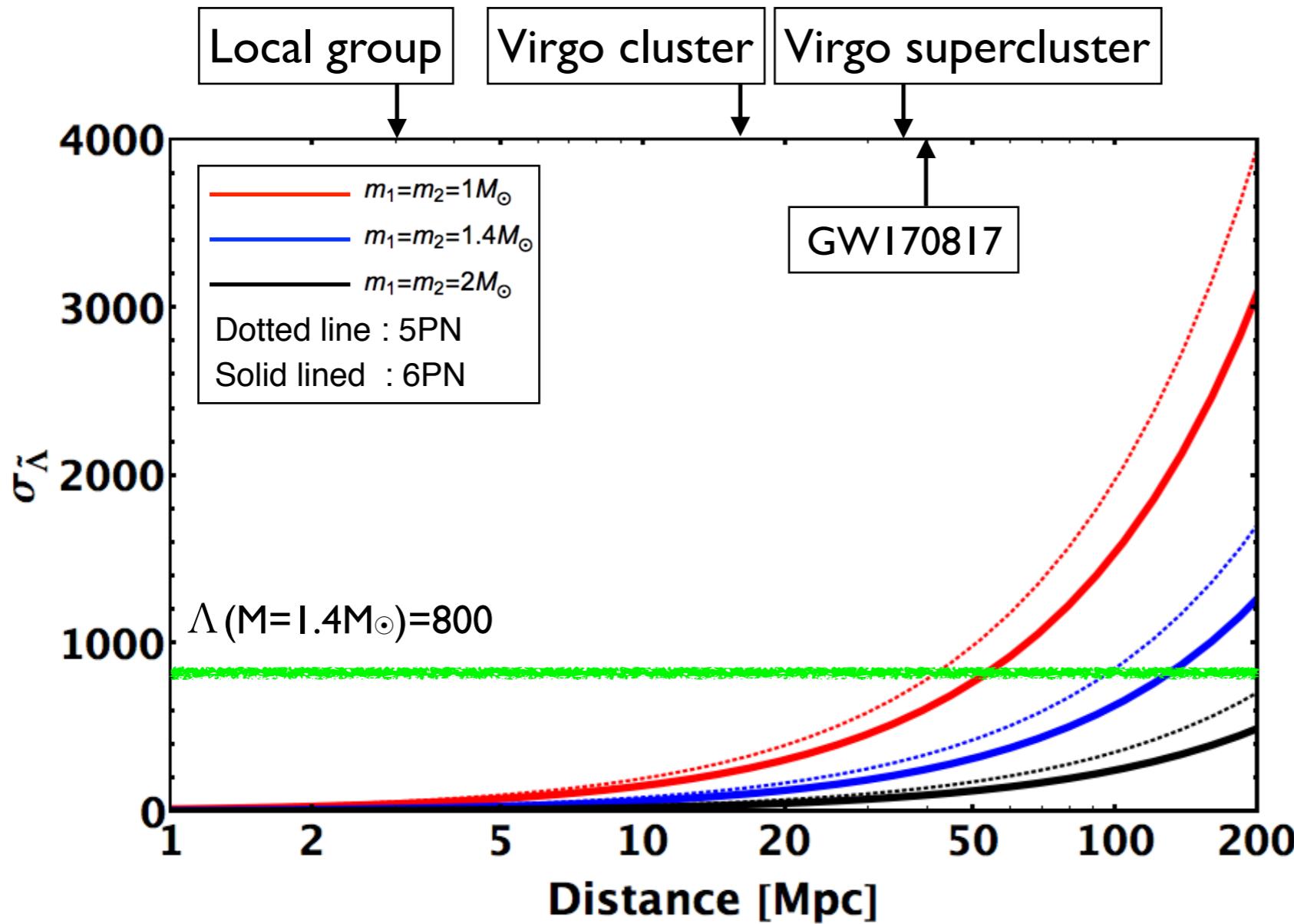


Fig. 1: Tidal deformability measurement error vs distance to the source. distances to galaxy clusters and GW20170817 distance are marked.

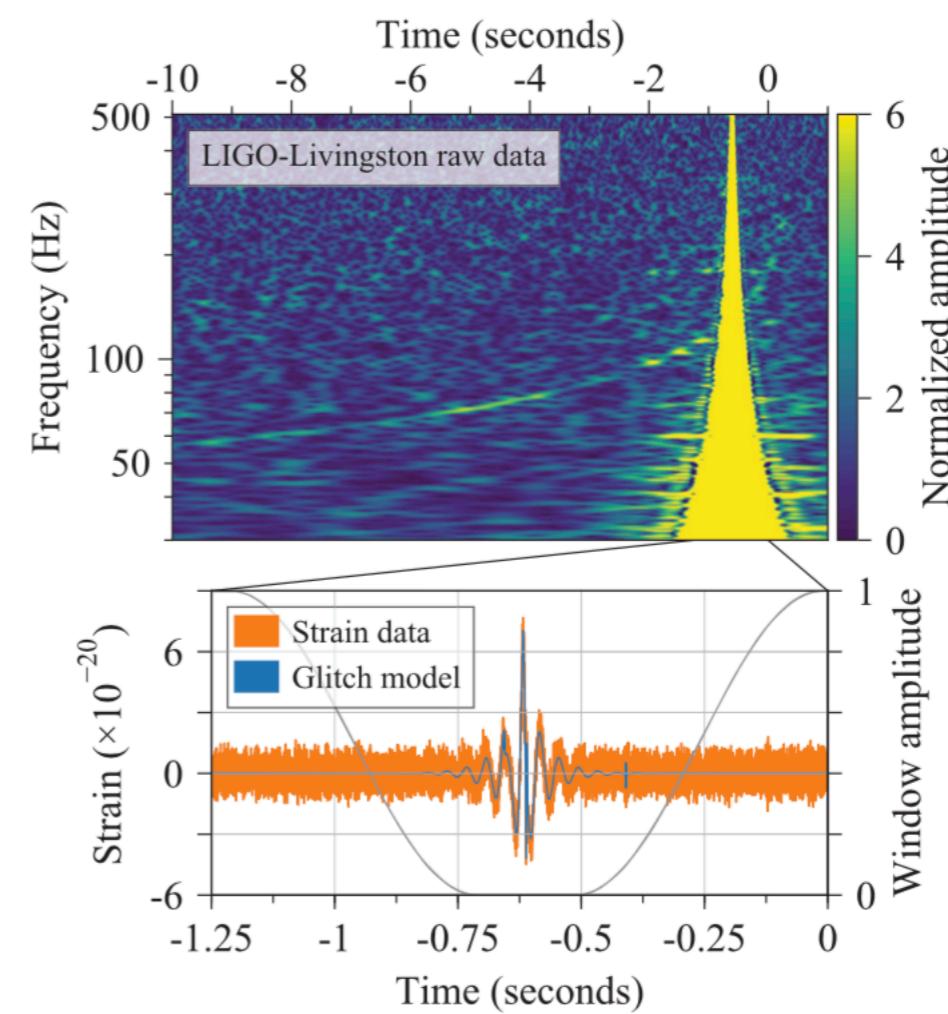
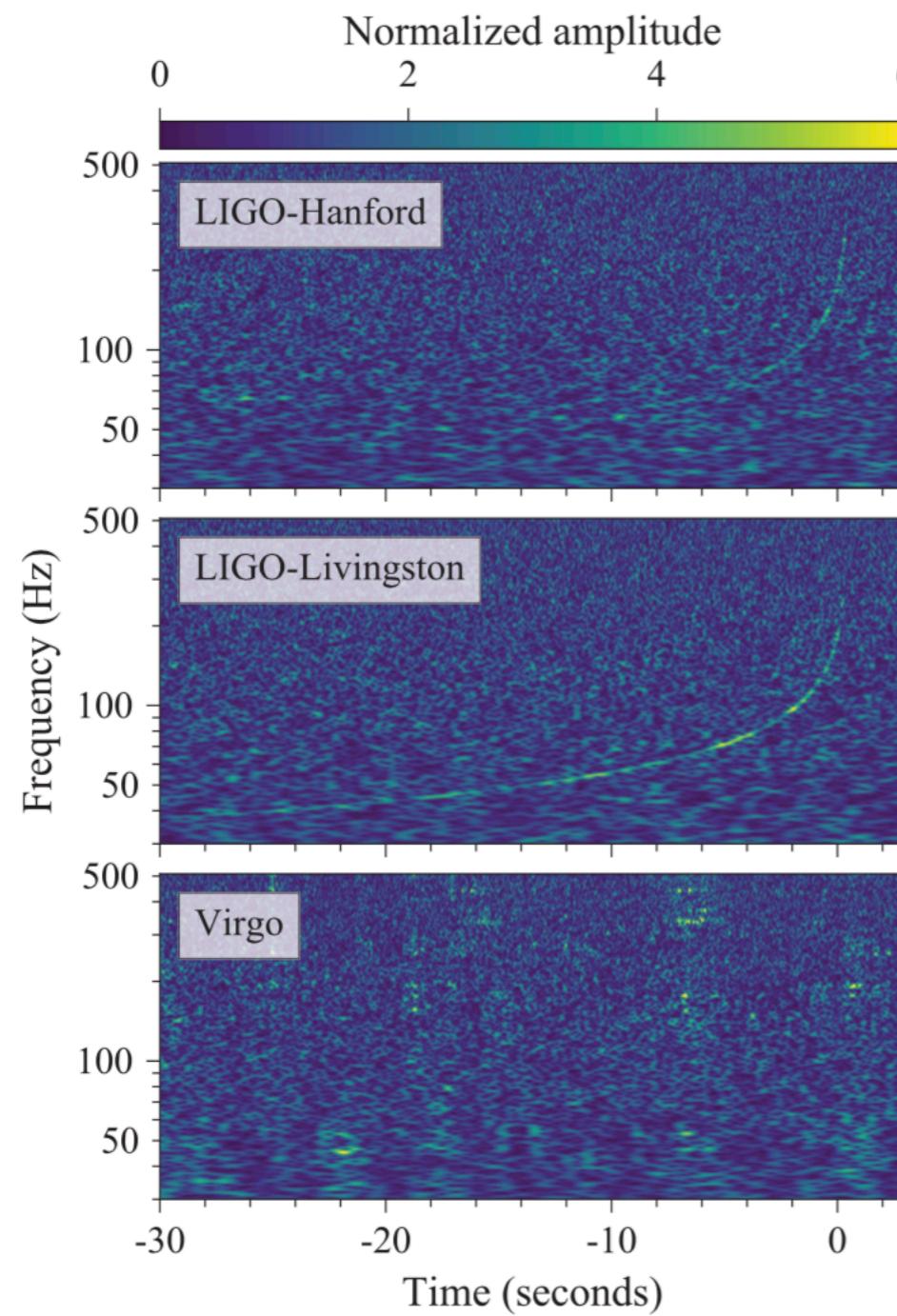


GW170817: Observation of Gravitational Waves from a Binary Neutron Star Inspiral

B. P. Abbott *et al.*^{*}

(LIGO Scientific Collaboration and Virgo Collaboration)

(Received 26 September 2017; revised manuscript received 2 October 2017; published 16 October 2017)





GW170817: Observation of Gravitational Waves from a Binary Neutron Star Inspiral

TABLE I. Source properties for GW170817: we give ranges encompassing the 90% credible intervals for different assumptions of the waveform model to bound systematic uncertainty. The mass values are quoted in the frame of the source, accounting for uncertainty in the source redshift.

	Low-spin priors ($ \chi \leq 0.05$)	High-spin priors ($ \chi \leq 0.89$)
Primary mass m_1	$1.36\text{--}1.60 M_{\odot}$	$1.36\text{--}2.26 M_{\odot}$
Secondary mass m_2	$1.17\text{--}1.36 M_{\odot}$	$0.86\text{--}1.36 M_{\odot}$
Chirp mass \mathcal{M}	$1.188^{+0.004}_{-0.002} M_{\odot}$	$1.188^{+0.004}_{-0.002} M_{\odot}$
Mass ratio m_2/m_1	$0.7\text{--}1.0$	$0.4\text{--}1.0$
Total mass m_{tot}	$2.74^{+0.04}_{-0.01} M_{\odot}$	$2.82^{+0.47}_{-0.09} M_{\odot}$
Radiated energy E_{rad}	$> 0.025 M_{\odot} c^2$	$> 0.025 M_{\odot} c^2$
Luminosity distance D_{L}	$40^{+8}_{-14} \text{ Mpc}$	$40^{+8}_{-14} \text{ Mpc}$
Viewing angle Θ	$\leq 55^\circ$	$\leq 56^\circ$
Using NGC 4993 location	$\leq 28^\circ$	$\leq 28^\circ$
Combined dimensionless tidal deformability $\tilde{\Lambda}$	≤ 800	≤ 700
Dimensionless tidal deformability $\Lambda(1.4M_{\odot})$	≤ 800	≤ 1400

GW170817

**Information of Neutron Star Structure
has been revealed by Gravitational Waves**

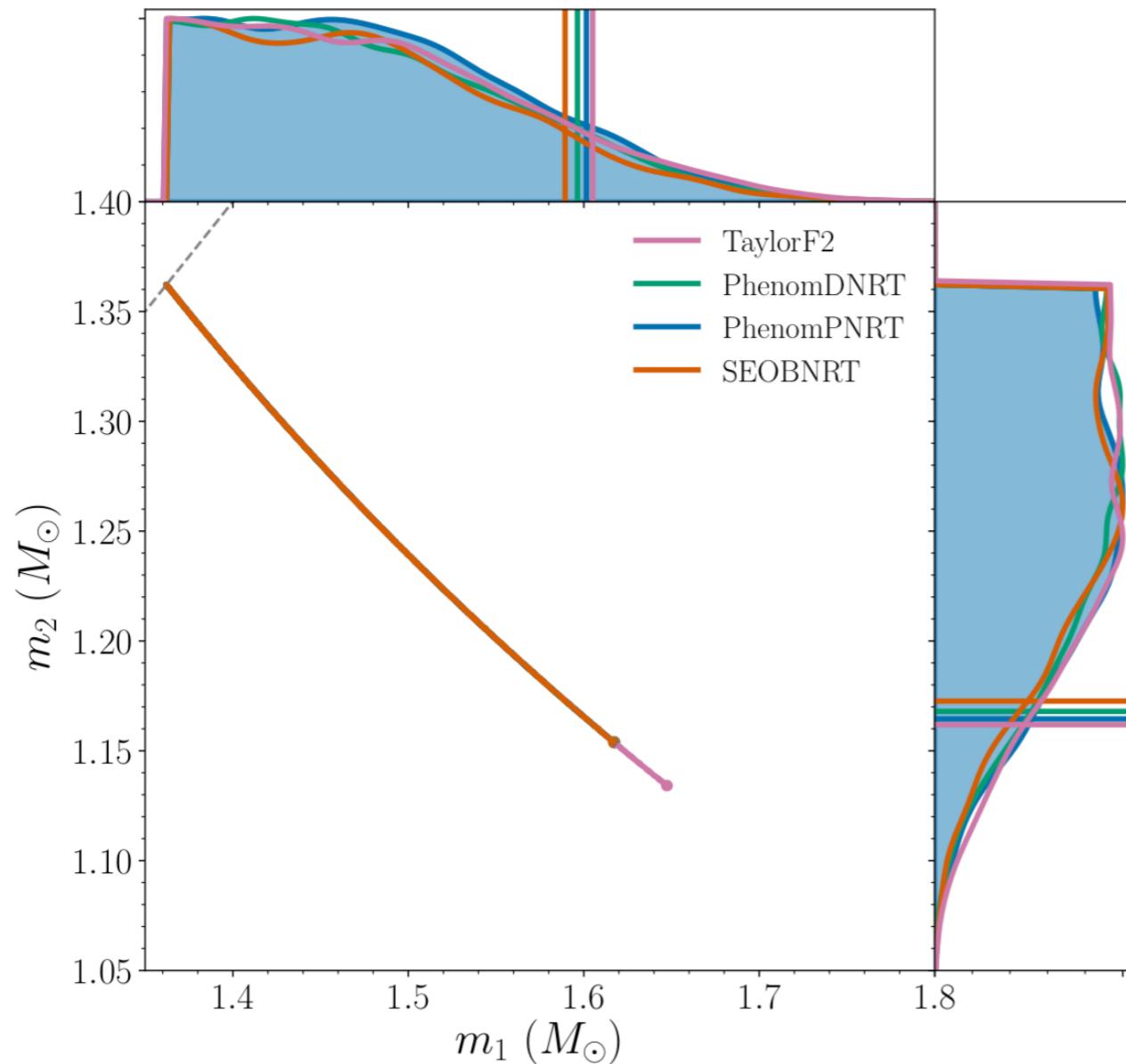
(revised) properties of GW170817

Abbott et al. (LSC and Virgo), arxiv:1805.11579

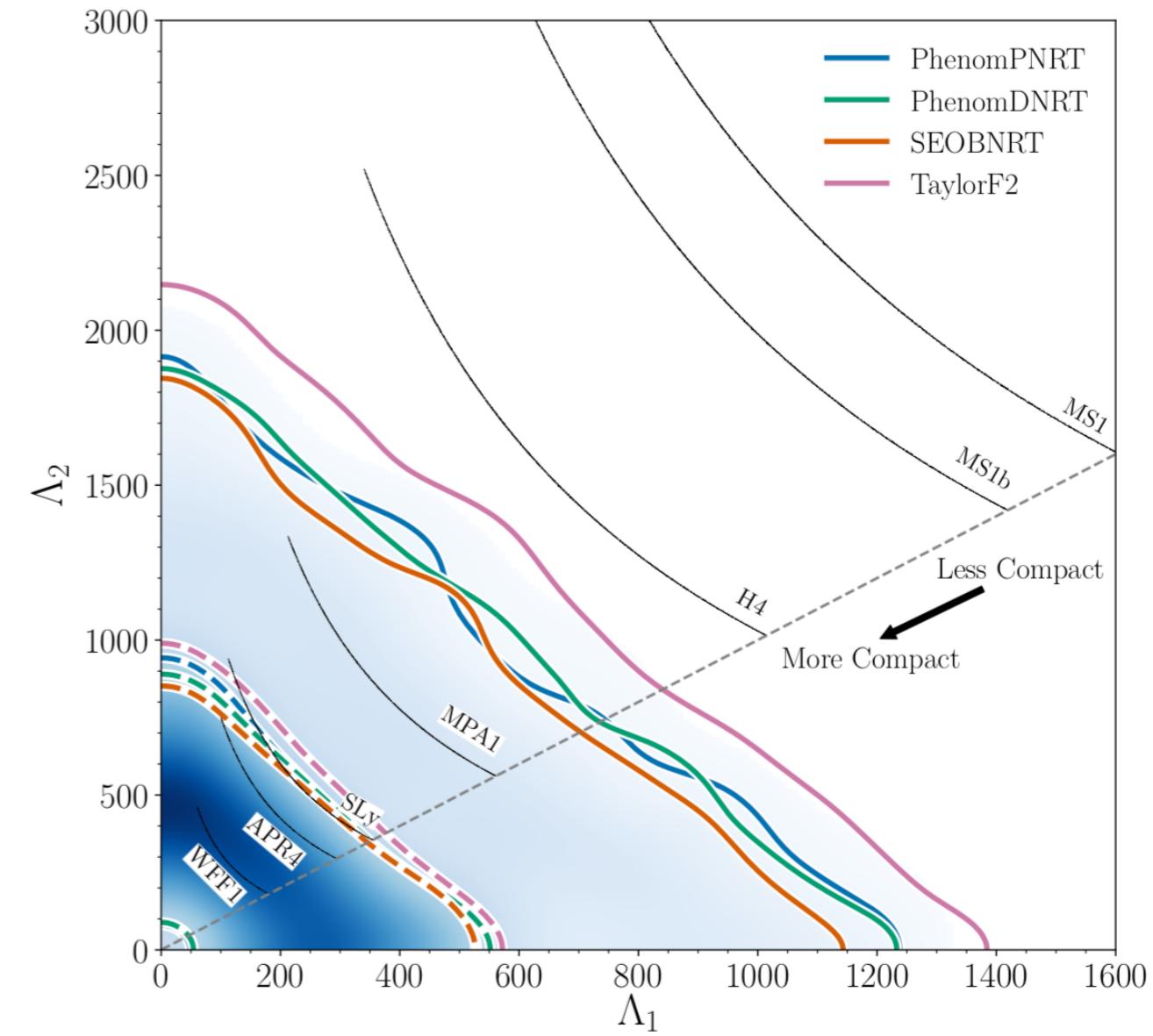
	Low-spin prior ($\chi \leq 0.05$)	High-spin prior ($\chi \leq 0.89$)
Binary inclination θ_{JN}	146^{+25}_{-27} deg	152^{+21}_{-27} deg
Binary inclination θ_{JN} using EM distance constraint [104]	151^{+15}_{-11} deg	153^{+15}_{-11} deg
Detector frame chirp mass \mathcal{M}^{det}	$1.1975^{+0.0001}_{-0.0001} M_{\odot}$	$1.1976^{+0.0004}_{-0.0002} M_{\odot}$
Chirp mass \mathcal{M}	$1.186^{+0.001}_{-0.001} M_{\odot}$	$1.186^{+0.001}_{-0.001} M_{\odot}$
Primary mass m_1	(1.36, 1.60) M_{\odot}	(1.36, 1.89) M_{\odot}
Secondary mass m_2	(1.16, 1.36) M_{\odot}	(1.00, 1.36) M_{\odot}
Total mass m	$2.73^{+0.04}_{-0.01} M_{\odot}$	$2.77^{+0.22}_{-0.05} M_{\odot}$
Mass ratio q	(0.73, 1.00)	(0.53, 1.00)
Effective spin χ_{eff}	$0.00^{+0.02}_{-0.01}$	$0.02^{+0.08}_{-0.02}$
Primary dimensionless spin χ_1	(0.00, 0.04)	(0.00, 0.50)
Secondary dimensionless spin χ_2	(0.00, 0.04)	(0.00, 0.61)
Tidal deformability $\tilde{\Lambda}$ with flat prior	300^{+500}_{-190} (symmetric)/ 300^{+420}_{-230} (HPD)	(0, 630)

300^{+500}_{-190} (symmetric)/ 300^{+420}_{-230} (HPD)	(0, 630)
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A new constraint by GW Observation

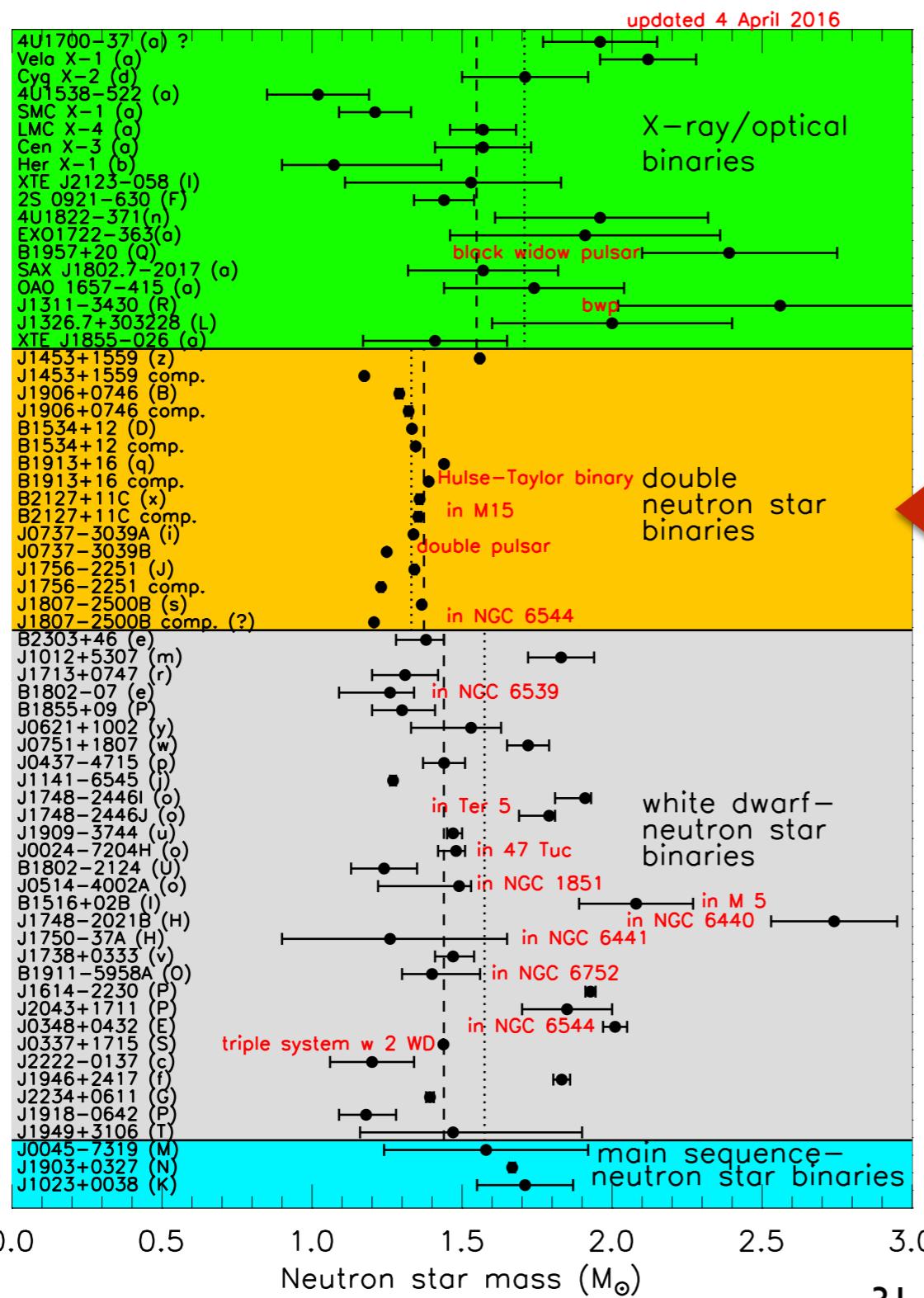


Low-spin prior : $X \leq 0.05$



Abbott et al. (LSC and Virgo), arxiv:1805.11579

Neutron Star of Known Mass



GW170817:
BNS
M1: $1.36 \sim 1.60 M_{\odot}$
($1.36 \sim 2.26$)
M2: $1.17 \sim 1.36 M_{\odot}$
($0.86 \sim 1.36$)

J. Lattimer, Annu.Rev.Nucl.Part.Sci.62,485(2012)
and <https://stellarcollapse.org> by C. Ott

Spectral expansion of adiabatic index [Lindblom et al.]

$$\epsilon(p) = \sum_k \epsilon_k \Phi_k(p).$$

$$\Gamma(p) = \frac{\epsilon + p}{p} \frac{dp}{d\epsilon}$$

$$\frac{d\epsilon(p)}{dp} = \frac{\epsilon(p) + p}{p \Gamma(p)}$$

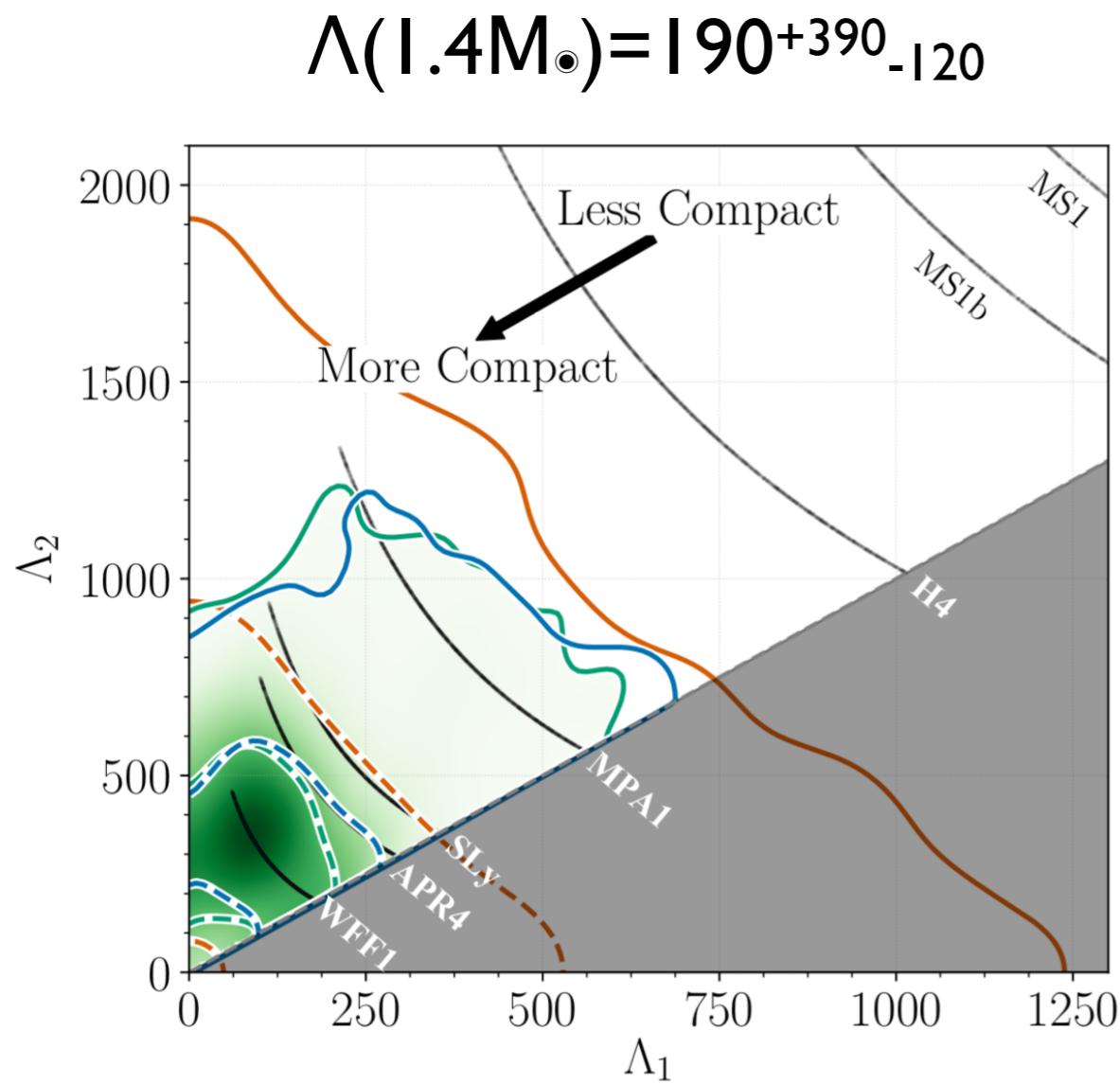
$$\Gamma(p) = \exp \left[\sum_k \gamma_k \Phi_k(p) \right]$$

$$\Gamma(x) = \exp \left(\sum_k \gamma_k x^k \right)$$

piecewise polytropic EoS HK Lee's talk on Sep. 14th

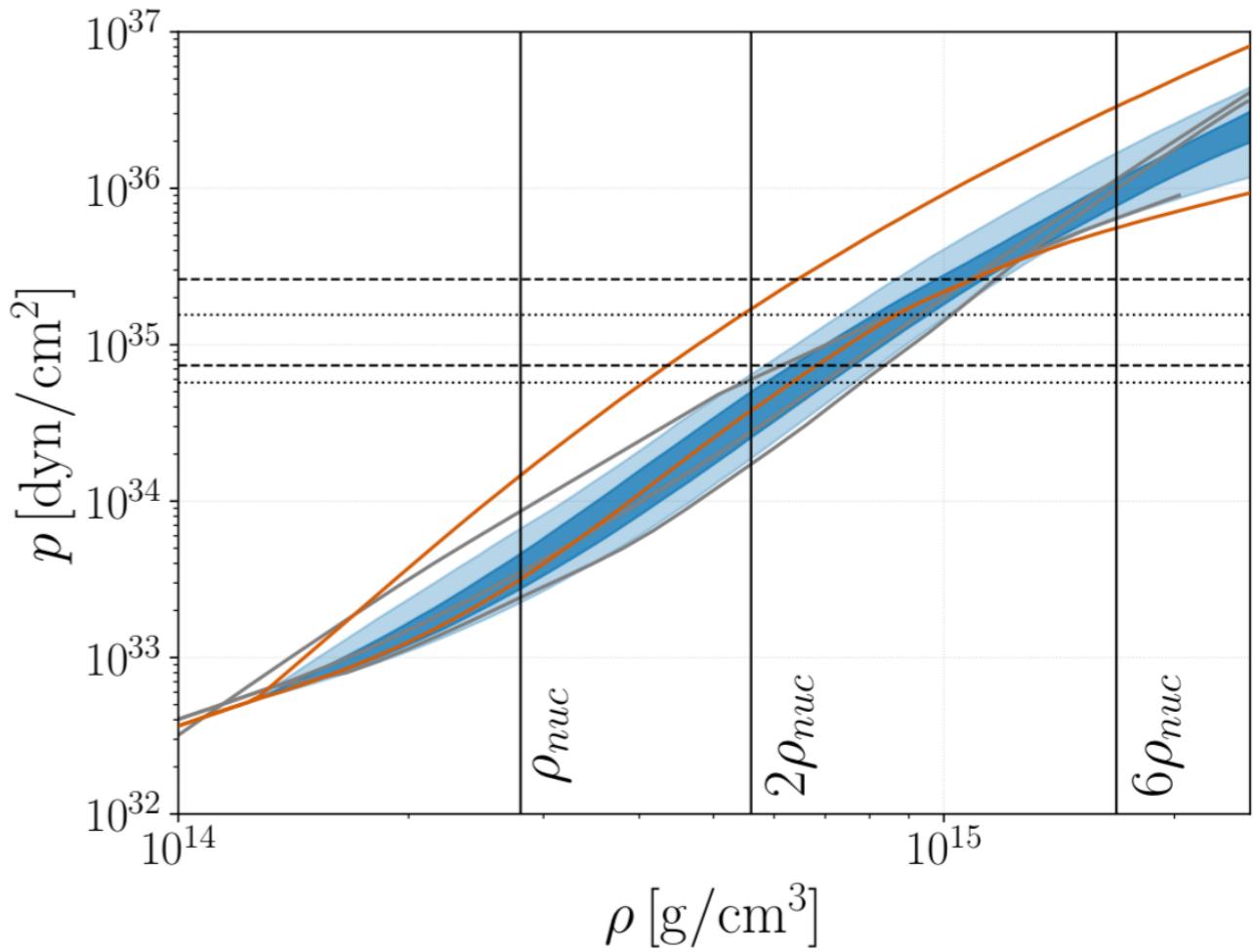
$$p(\rho) = K_i \rho^{\Gamma_i},$$

A new constraint by GW Obs. (I)



$$P(2 \rho_{nuc}) = 3.5^{+2.7}_{-1.7} \times 10^{34} \text{ dyne/cm}^2$$

$$P(6 \rho_{nuc}) = 9.0^{+7.9}_{-2.6} \times 10^{35} \text{ dyne/cm}^2$$



Abbott et al. (LSC and Virgo), arxiv:1805.11581 (PRL accepted)

$$\rho_{nuc} = 2.8 \times 10^{14} \text{ g/cm}^3$$

Universal (Eos-insensitive) relations

Yagi & Yunes, PR 681, 1 (2017)

I-Love-Q relation, ...

- Moment of inertia (I)
- Tidal Love number (Love)
- Quadrupole moment (Q)

Applications

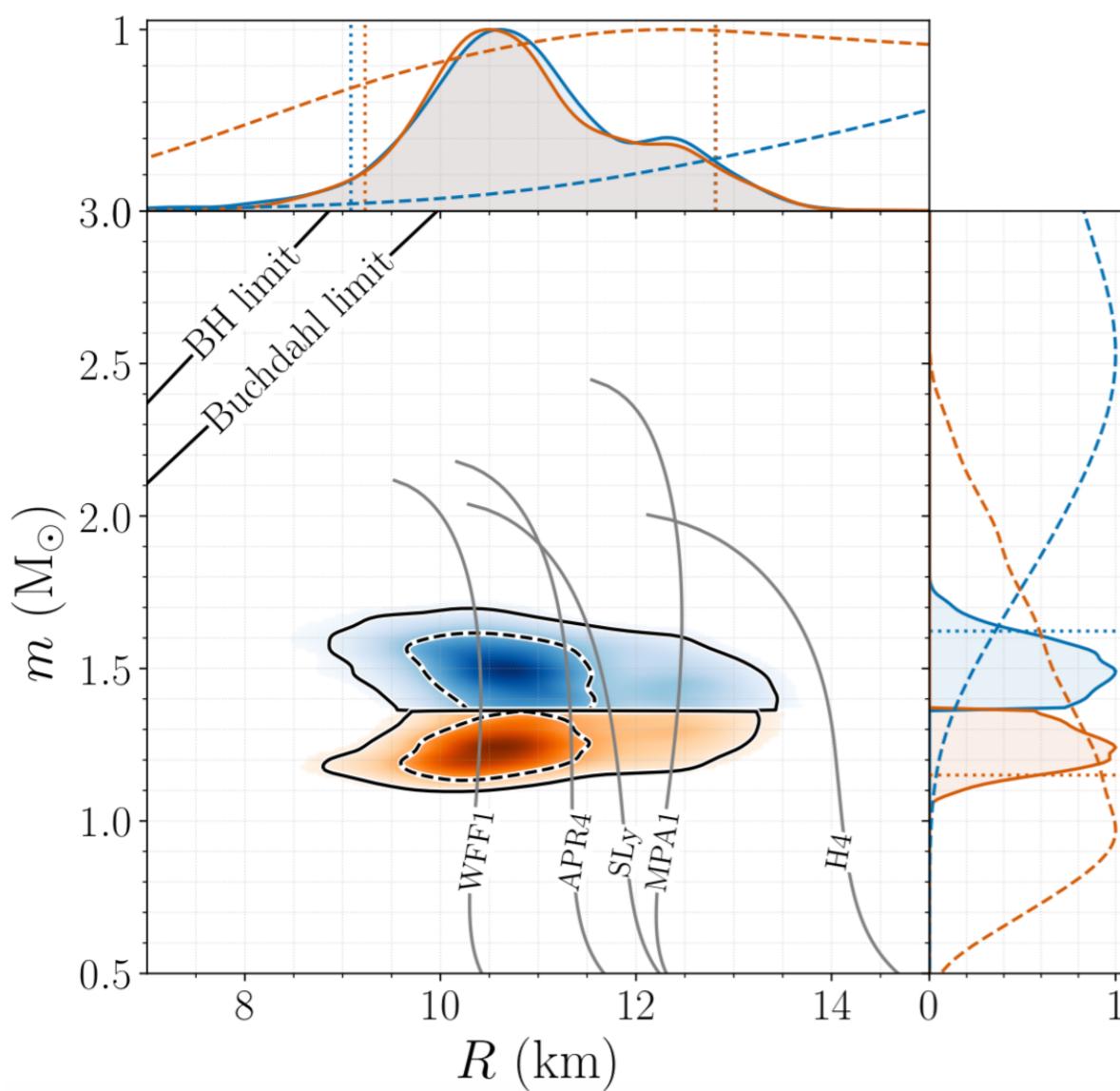
- X-ray observations
- Gravitational-wave measurements
- Gravitational & astrophysical test of GR

A new constraint by GW Obs. (2)

EoS insensitive relations (Yagi&Yunes,PR2017)

$$R_1 = 10.8^{+2.0}_{-1.7} \text{ km}$$

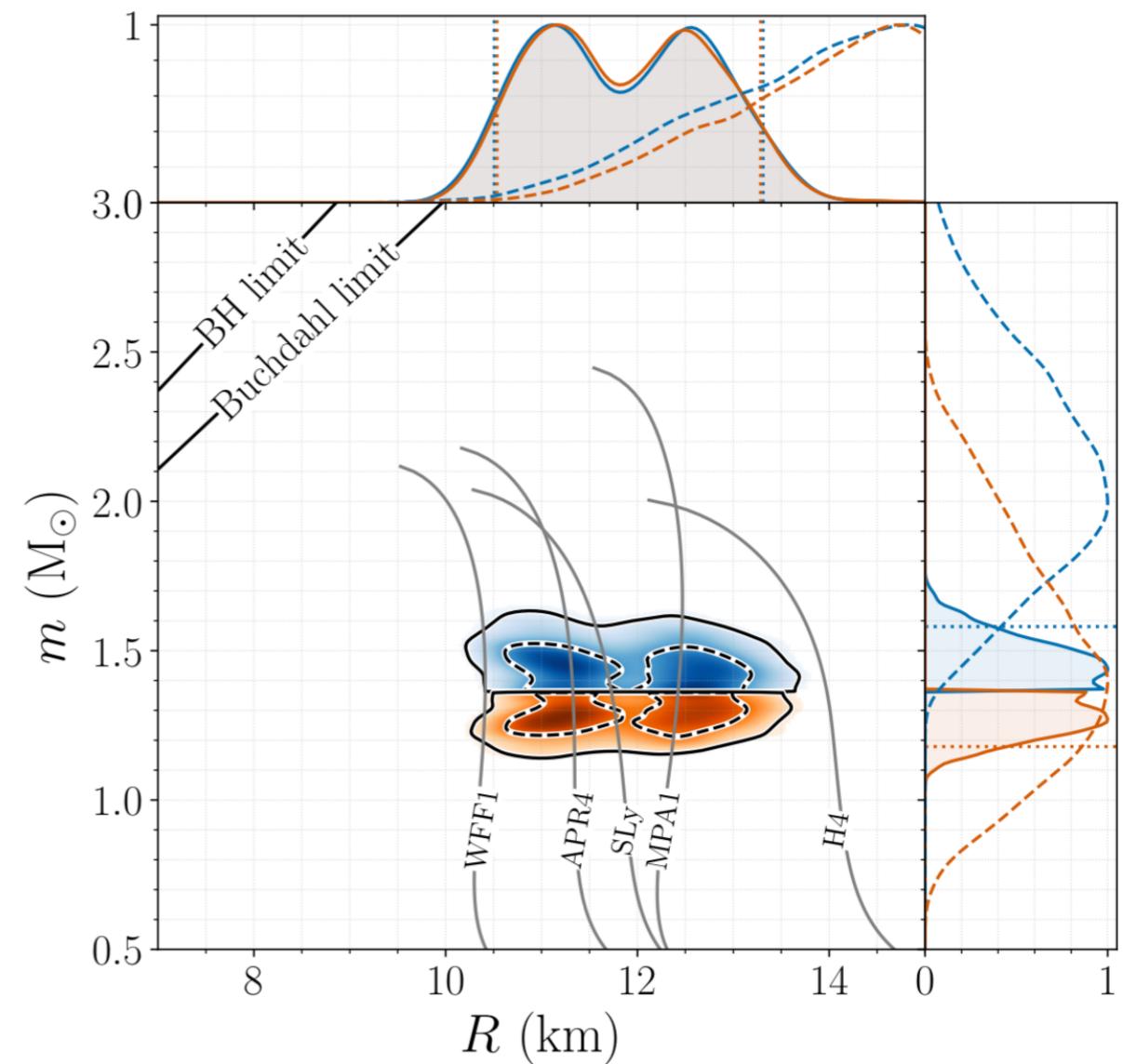
$$R_2 = 10.7^{+2.1}_{-1.5} \text{ km}$$



Parametrized EoS: $M_{\max} \geq 1.97 M_\odot$

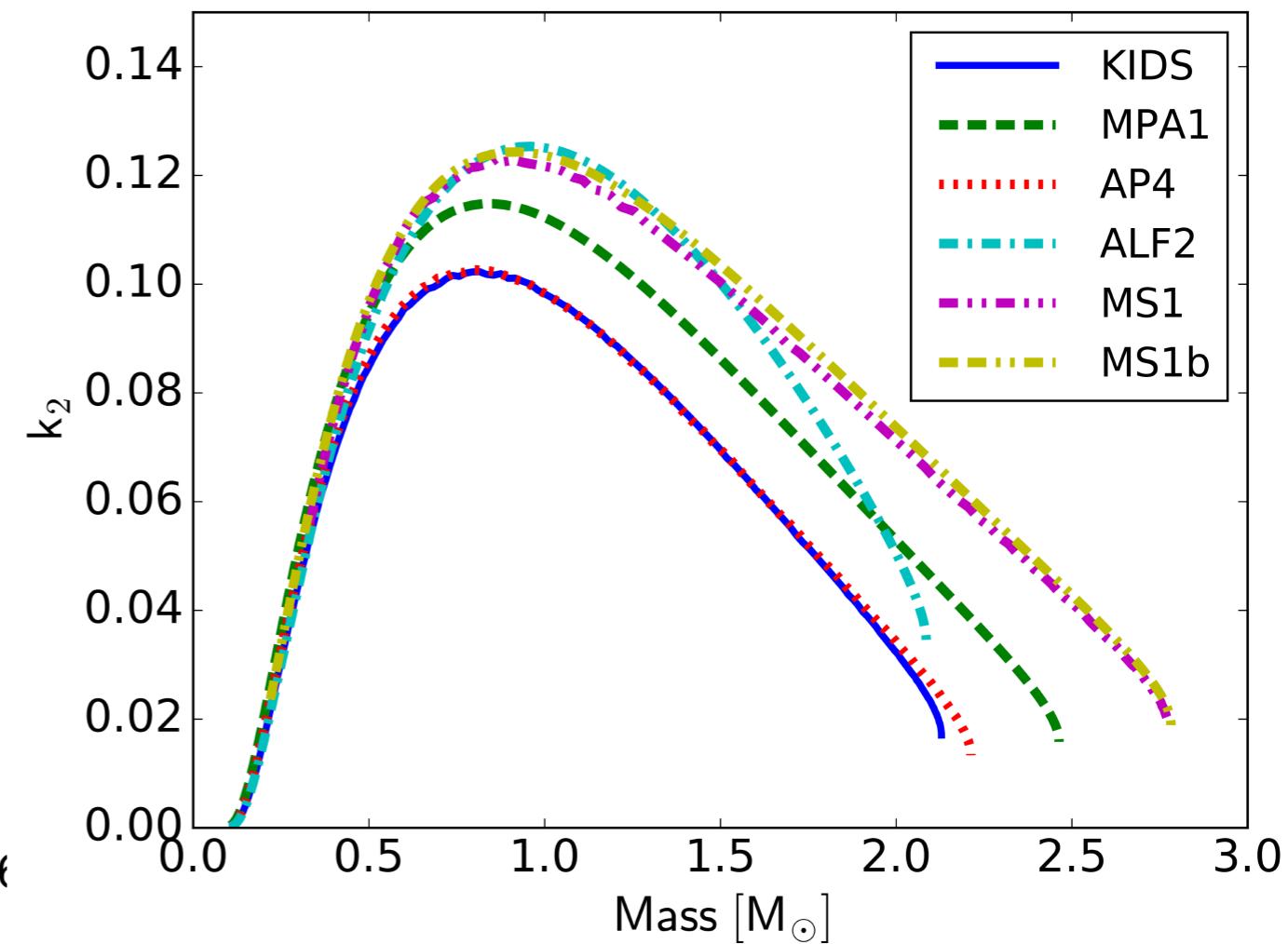
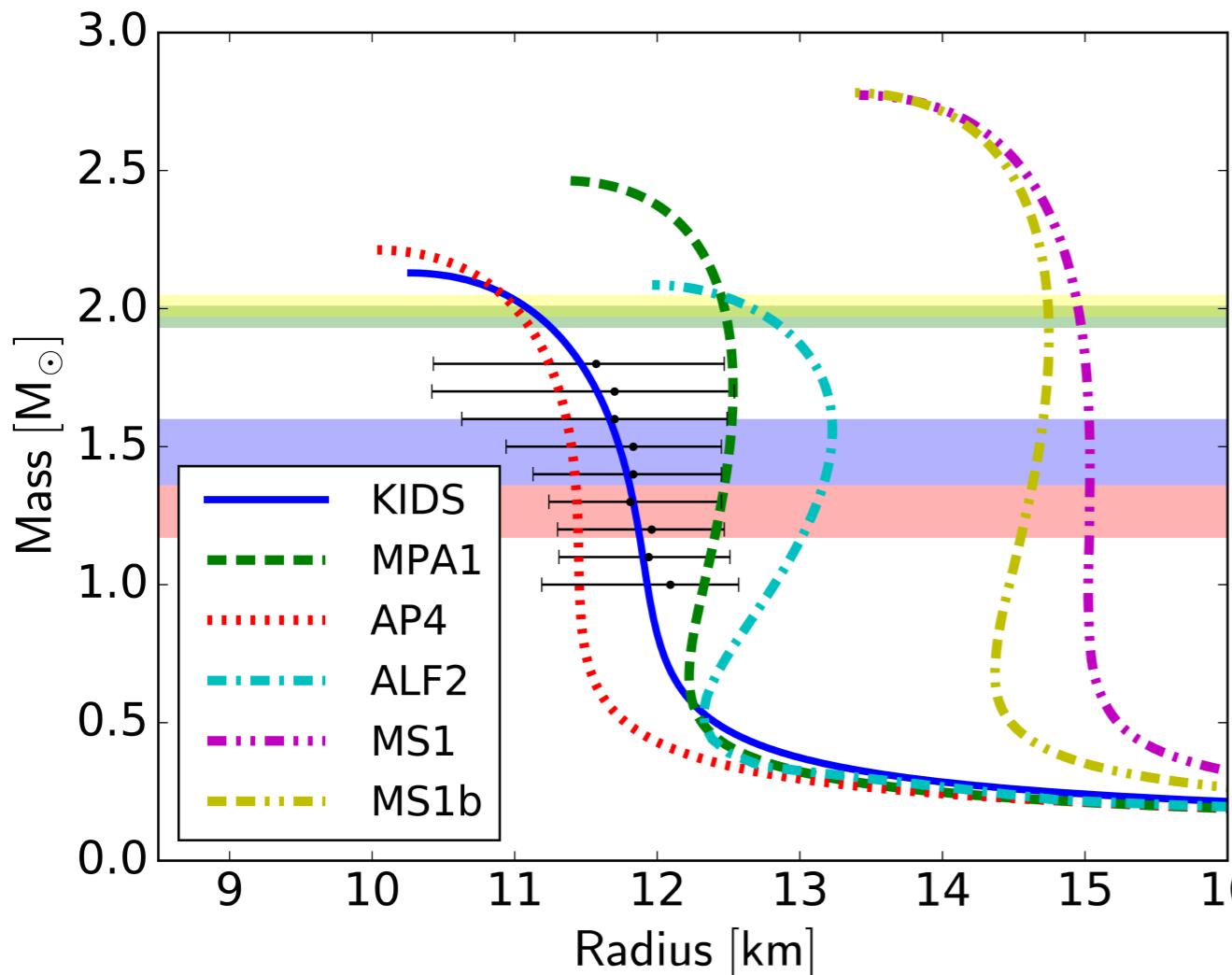
$$R_1 = 11.9^{+1.4}_{-1.4} \text{ km}$$

$$R_2 = 11.9^{+1.4}_{-1.4} \text{ km}$$



What we have done (1)

Kim et al., New Physics: Sae Mulli (2018)

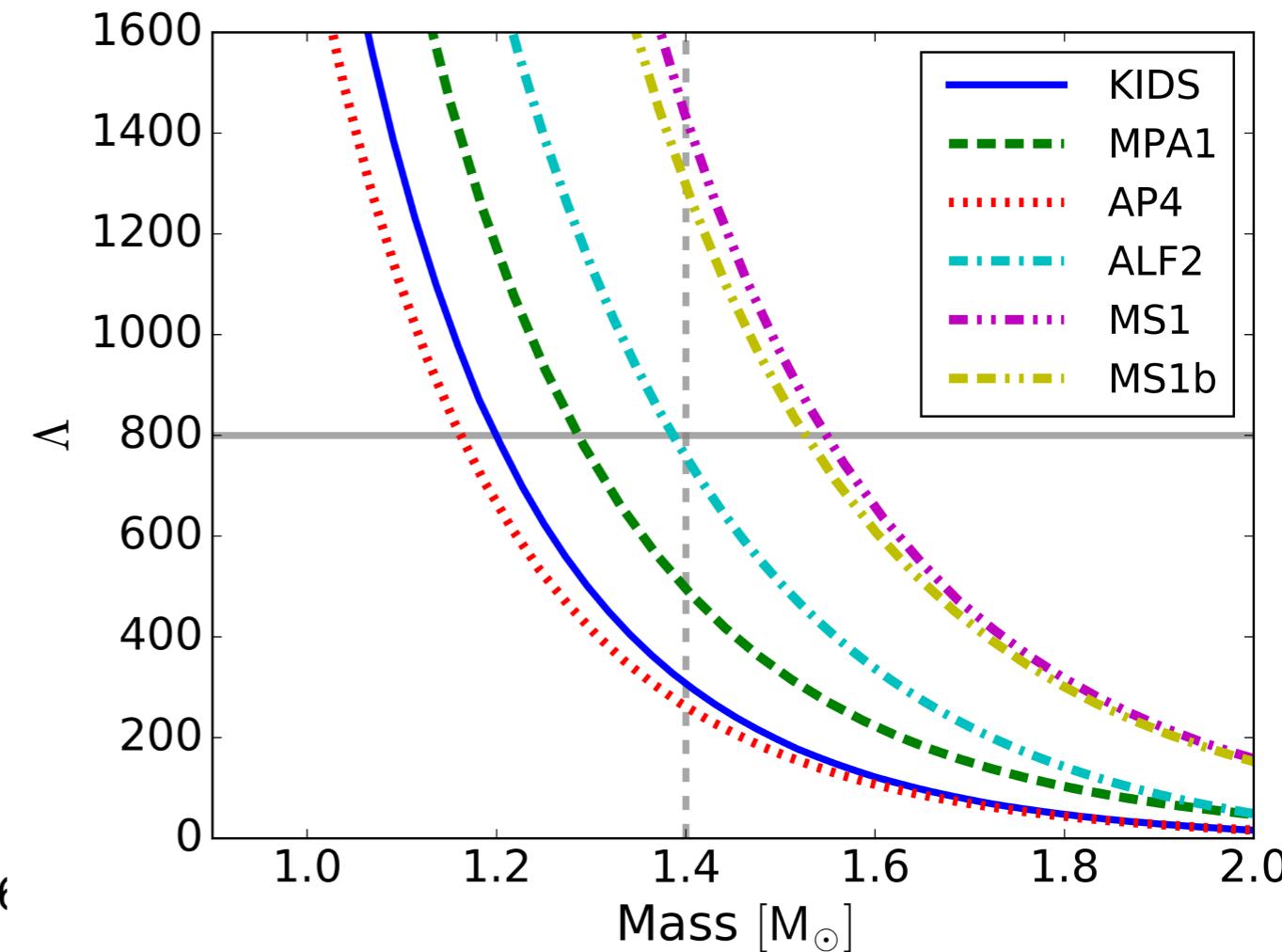
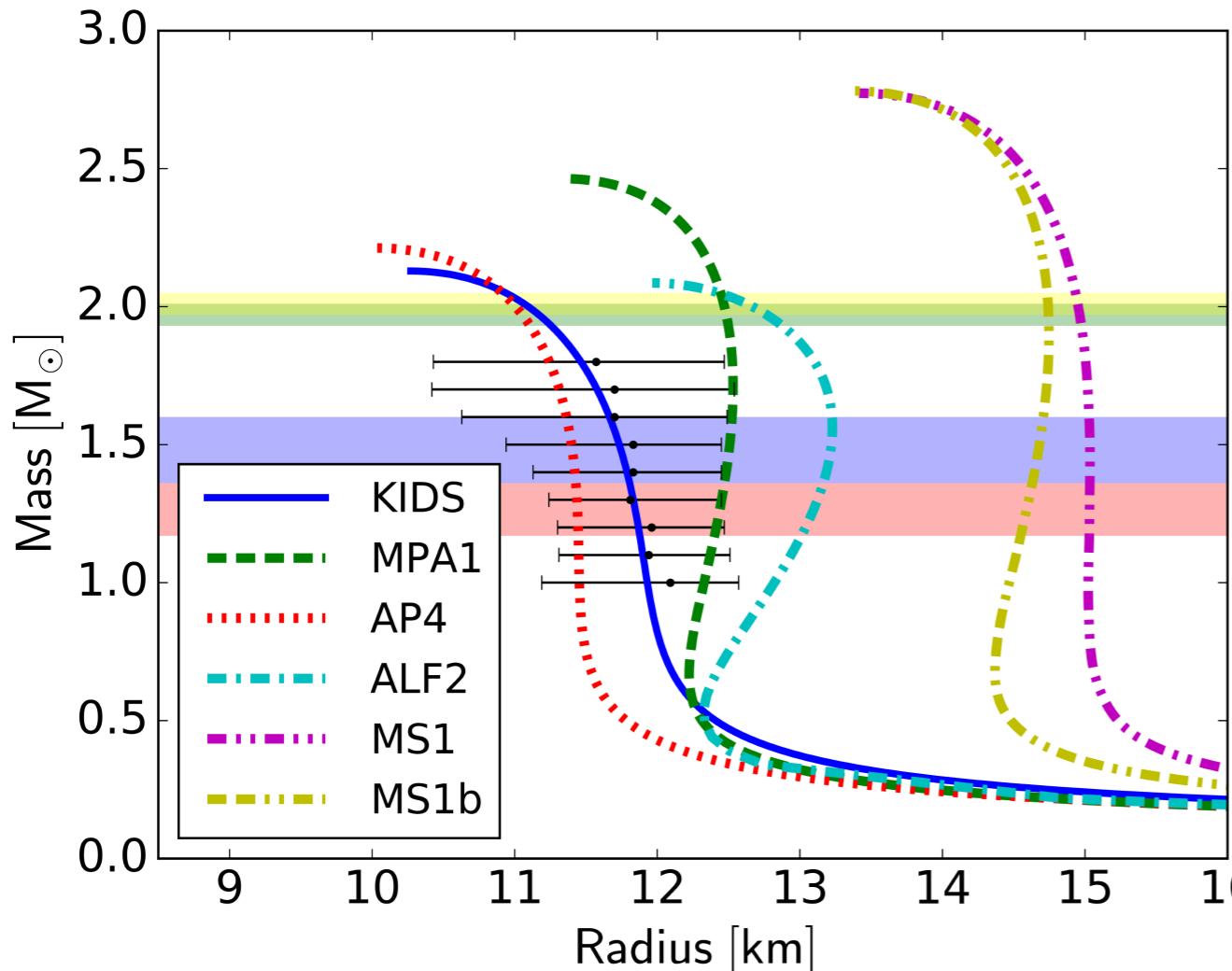


GW170817 - Abbott et al. (LSC and Virgo), arxiv:1805.111579

- $M_{\text{chirp}} = 1.188 M_\odot$
- low spin prior : $\Lambda = 300^{+500}_{-190}$ (symmetric) / 300^{+420}_{-230} (HPD)
- high spin prior : $\Lambda = 0 \sim 630$

What we have done (1)

Kim et al., New Physics: Sae Mulli (2018)



GW170817 - Abbott et al. (LSC and Virgo), arxiv:1805.11579

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Tidal Deformability of Neutron Stars with Realistic Nuclear Energy Density Functionals

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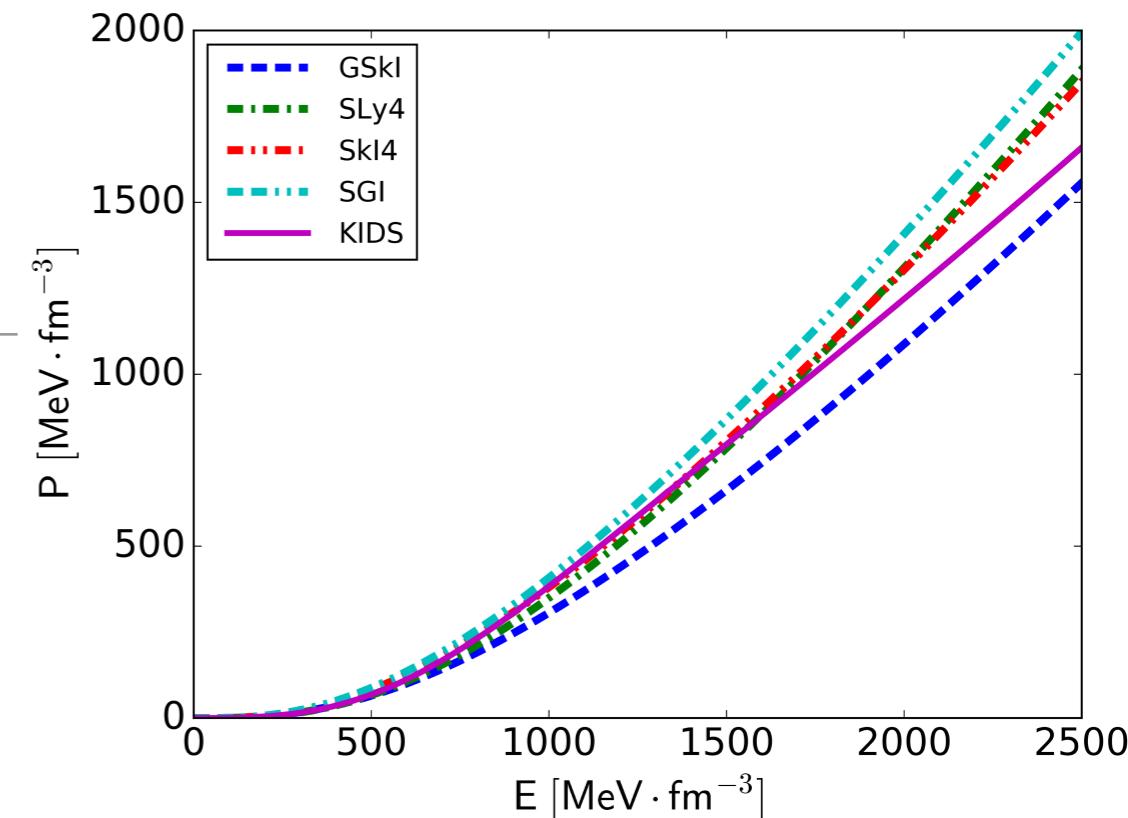
Constraints on Nuclear EoS

- Nuclear data: hundreds of models (Skyrme force, RMF, ...)
- Neutron star maximum mass
 $1.97 \pm 0.04 M_{\odot}$ [Nature 467, 1081 (2010)]
 $2.01 \pm 0.04 M_{\odot}$ [Science 340, 448 (2013)]
- 11 experimental/empirical data for nuclear matter around saturation density [Phys.Rev.C 85, 035201 (2012)]

Constraint	Quantity	Eq.	Density Region	Range of constraint		Ref.
				exp/emp	from CSkP	
SM1	K_o	(7), (15)	ρ_o (fm^{-3})	200 – 260 MeV	202.0 – 240.3 MeV	[64]
SM2	$K' = -Q_o$	(8), (16)	ρ_o (fm^{-3})	200 – 1200 MeV	362.5 – 425.6 MeV	[65]
SM3	$P(\rho)$	(6)	$2 < \frac{\rho}{\rho_o} < 3$	Band Region	see Fig. 1	[78]
SM4	$P(\rho)$	(6)	$1.2 < \frac{\rho}{\rho_o} < 2.2$	Band Region	see Fig. 2	[80]
PNM1	$\frac{E_{PNM}}{E_{PNM}^o}$	(31)	$0.014 < \frac{\rho}{\rho_o} < 0.106$	Band Region	see Fig. 3	[39, 40]
PNM2	$P(\rho)$	(6)	$2 < \frac{\rho}{\rho_o} < 3$	Band Region	see Fig. 5	[78]
MIX1	J	(9)	ρ_o (fm^{-3})	30 – 35 MeV	30.0 – 35.5 MeV	[44]
MIX2	L	(10)	ρ_o (fm^{-3})	40 – 76 MeV	48.6 – 67.1 MeV	[101]
MIX3	$K_{\tau,v}$	(21)	ρ_o (fm^{-3})	-760 – -372 MeV	-407.1 – -360.1 MeV	[107]
MIX4	$\frac{S(\rho_o/2)}{J}$	-	ρ_o (fm^{-3})	0.57 – 0.86	0.61 – 0.67	[110]
MIX5	$\frac{3P_{PNM}}{L\rho_o}$	(41)	ρ_o (fm^{-3})	0.90 – 1.10	1.02 – 1.10	[112]

Selected EoSs

- Skyrme force models
- Basically fitted to properties of well-known nuclei
- Good saturation properties
- M_{max} more than $2M_{\odot}$

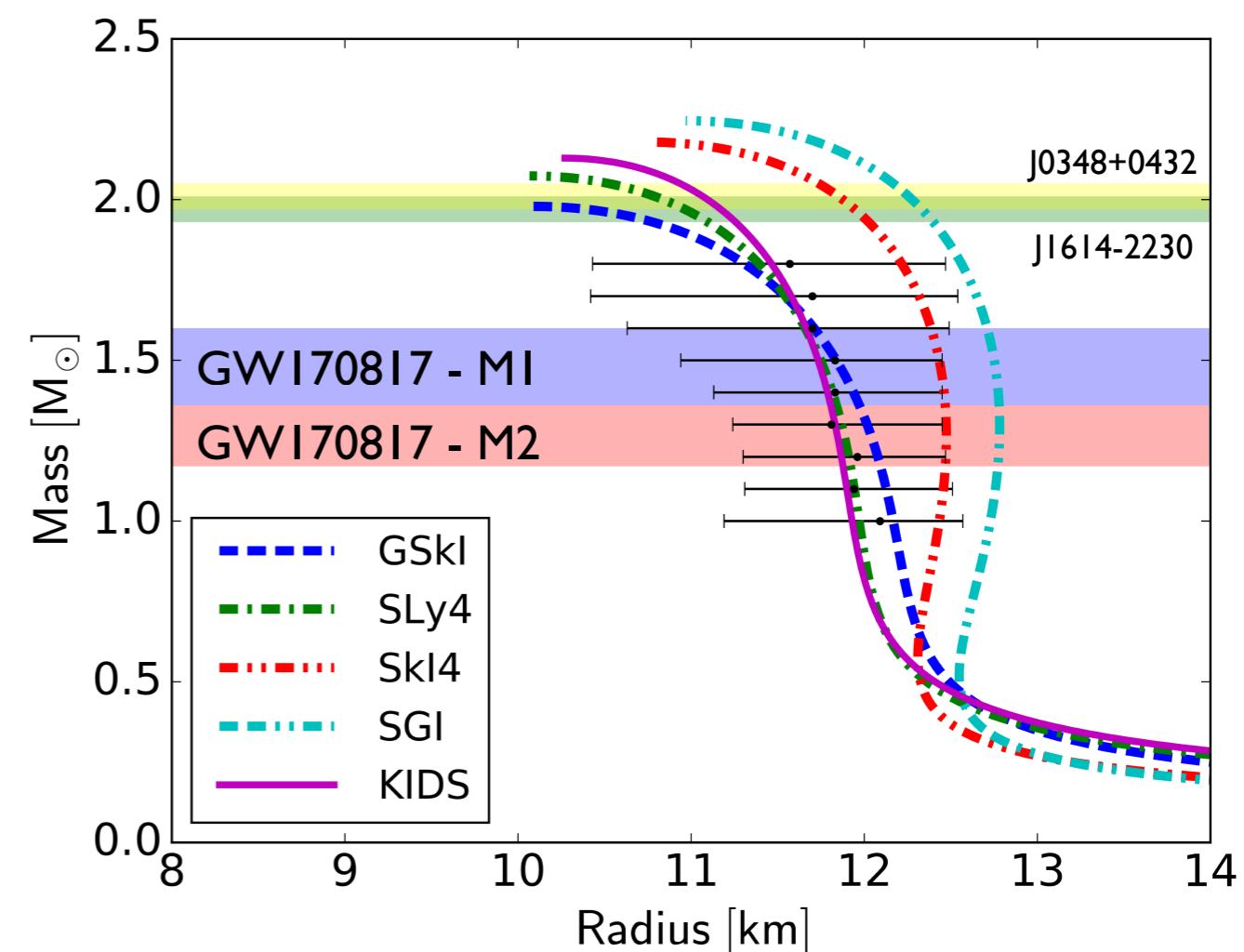
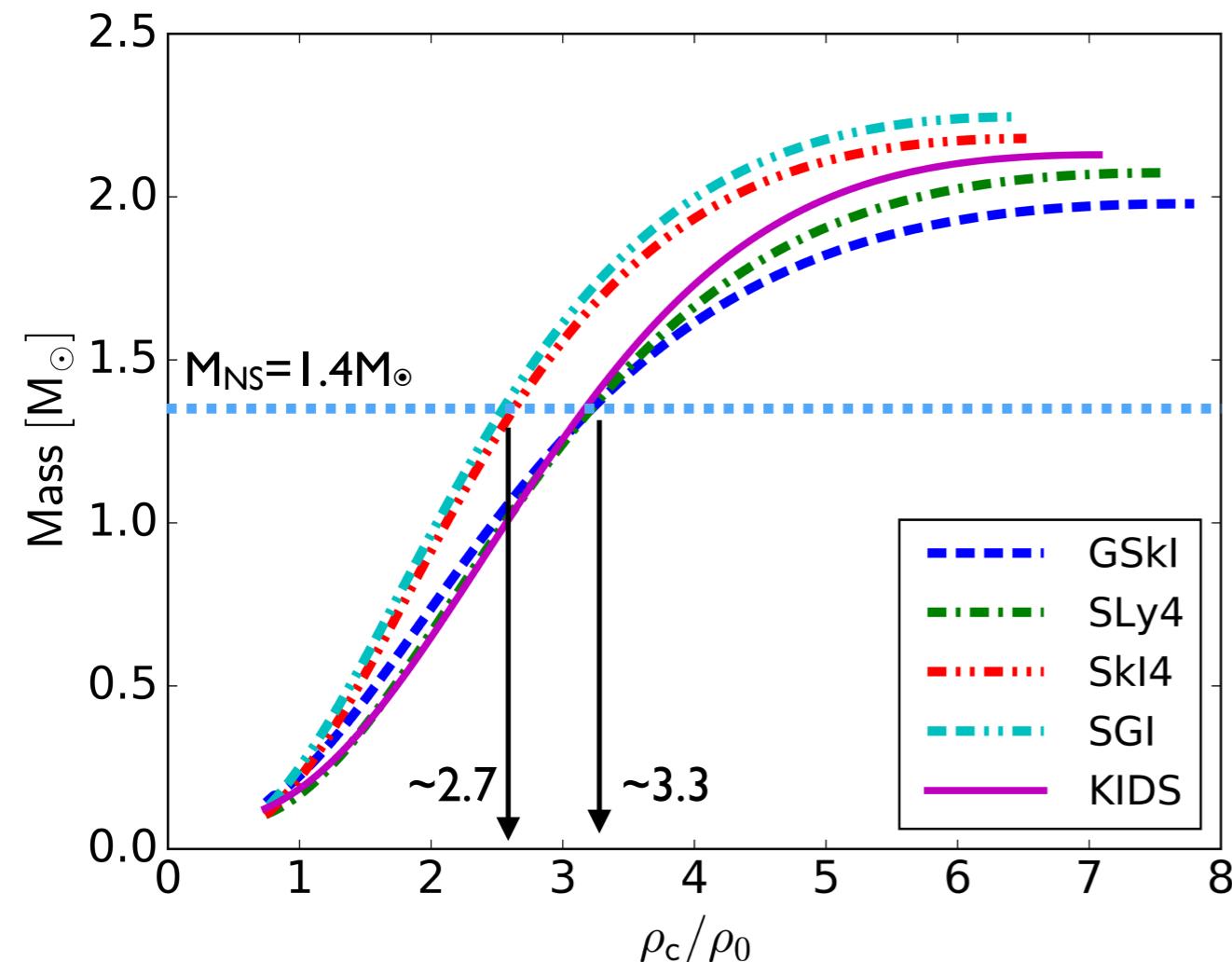


Model	ρ_0	E_0	K_0	$-Q_0$	J	L	$-K_\tau$	M_{max}
Exp/Emp	$\simeq 0.16$	$\simeq 16.0$	$200 \sim 260$	$200 \sim 1200$	$30 \sim 35$	$40 \sim 76$	$372 \sim 760$	$\geq 1.93 \sim 2.05$
CSkP	-	-	$202.0 \sim 240.3$	$362.5 \sim 425.6$	$30.0 \sim 35.5$	$48.6 \sim 67.1$	$360.1 \sim 407.1$	-
GSkI	0.159	16.02	230.2	405.6	32.0	63.5	364.2	1.98
SLy4	0.160	15.97	229.9	363.1	32.0	45.9	322.8	2.07
SkI4	0.160	15.95	248.0	331.2	29.5	60.4	322.2	2.19
SGI	0.154	15.89	261.8	297.9	28.3	63.9	362.5	2.25
KIDS	0.160	16.00	240.0	372.7	32.8	49.1	375.1	2.14

KIDS (Korea: IBS-Daegu-Sungkyunkwan): A new systematic expansion scheme for nuclear EDF
[Phys. Rev. C 97, 014312 (2018)]

Mass-Radius relations

Kim et al., arxiv:1805.00219

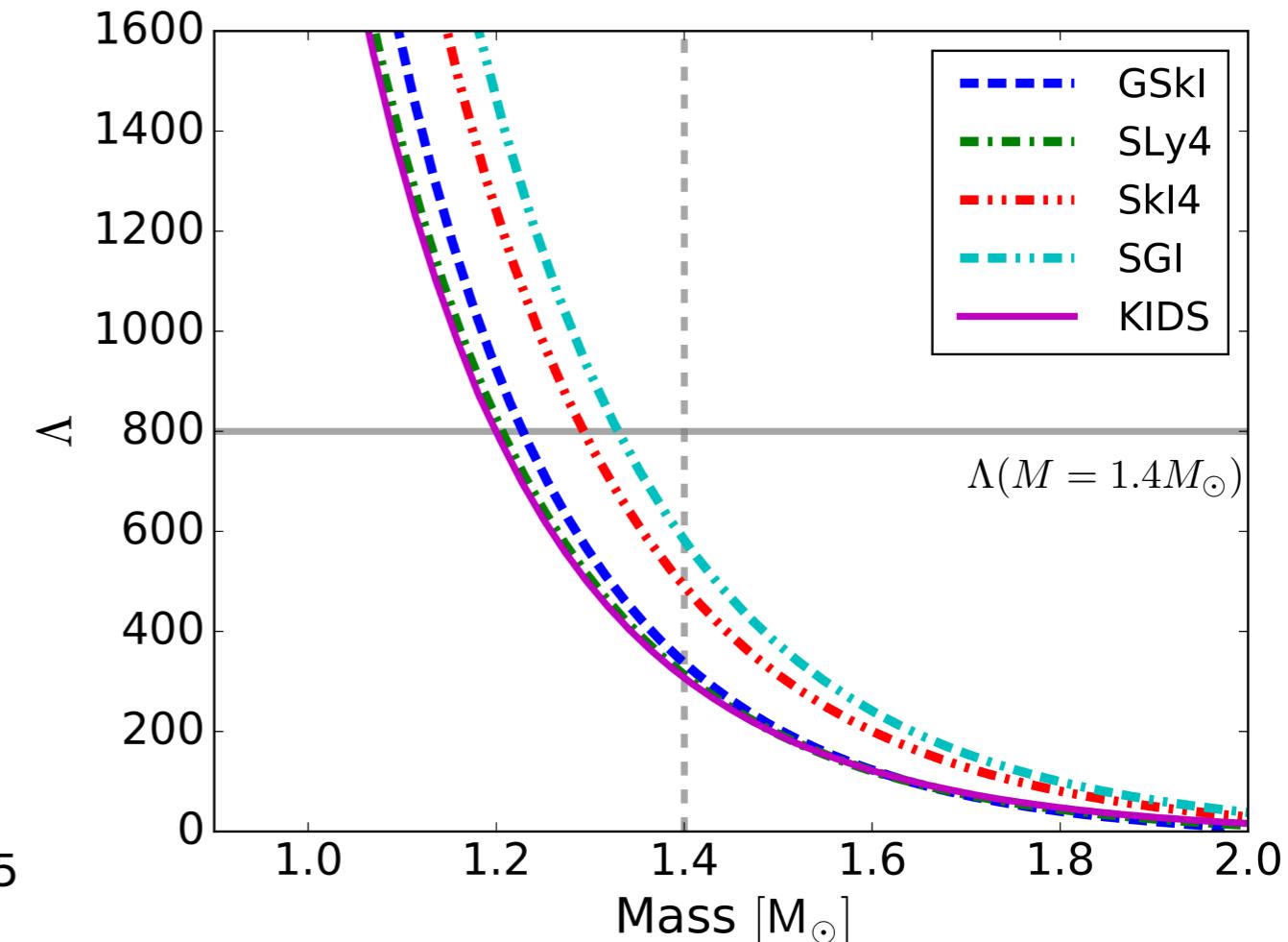
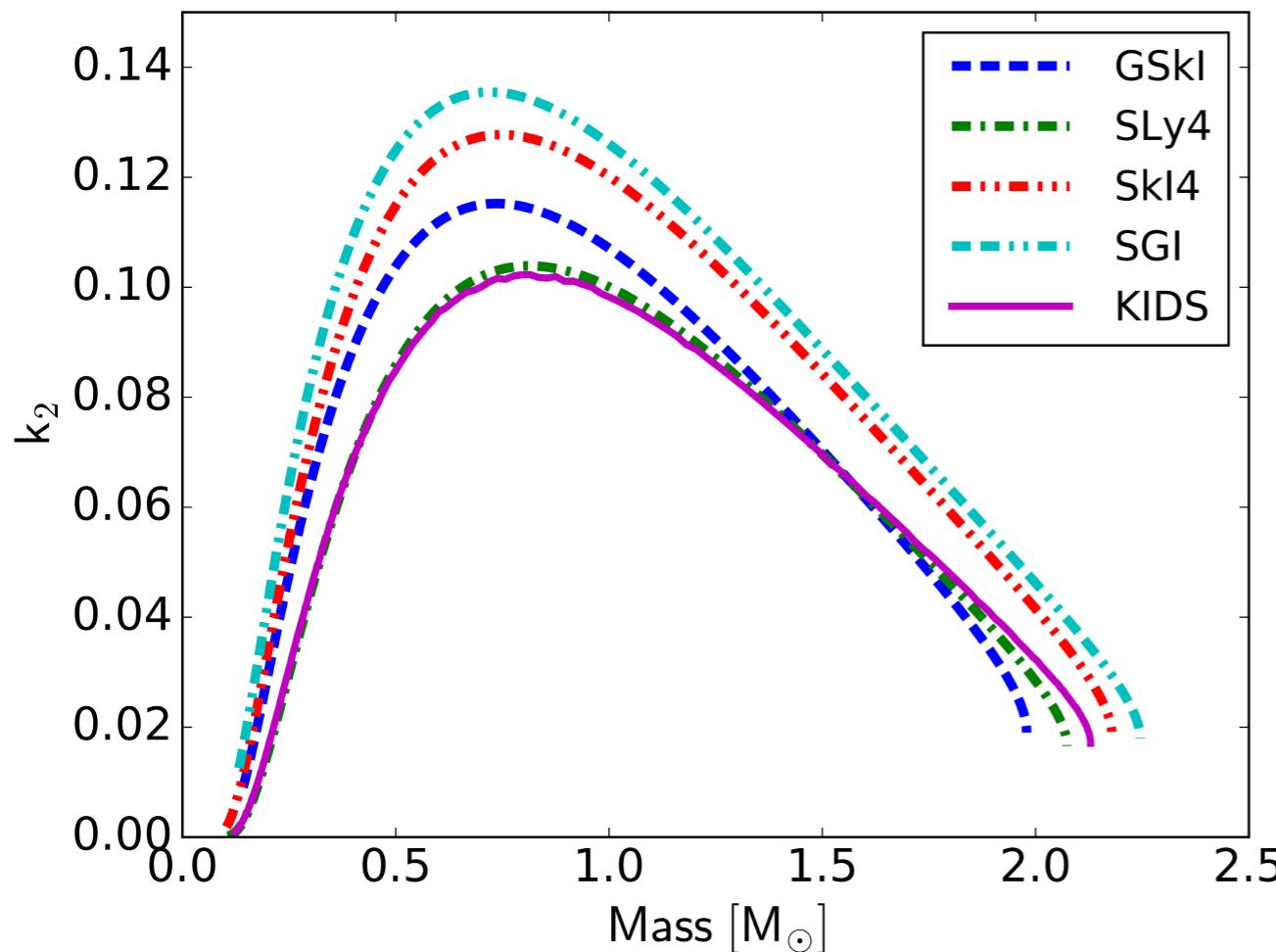


GW170817

- $M_{\text{chirp}} = 1.188 M_{\odot}$
- low spin prior : $M1 = 1.36 \sim 1.60 M_{\odot}$, $M2 = 1.17 \sim 1.36 M_{\odot}$
- high spin prior : $M1 = 1.36 \sim 2.26 M_{\odot}$, $M2 = 0.86 \sim 1.36 M_{\odot}$

Tidal deformability of a NS

Kim et al., arxiv:1805.00219

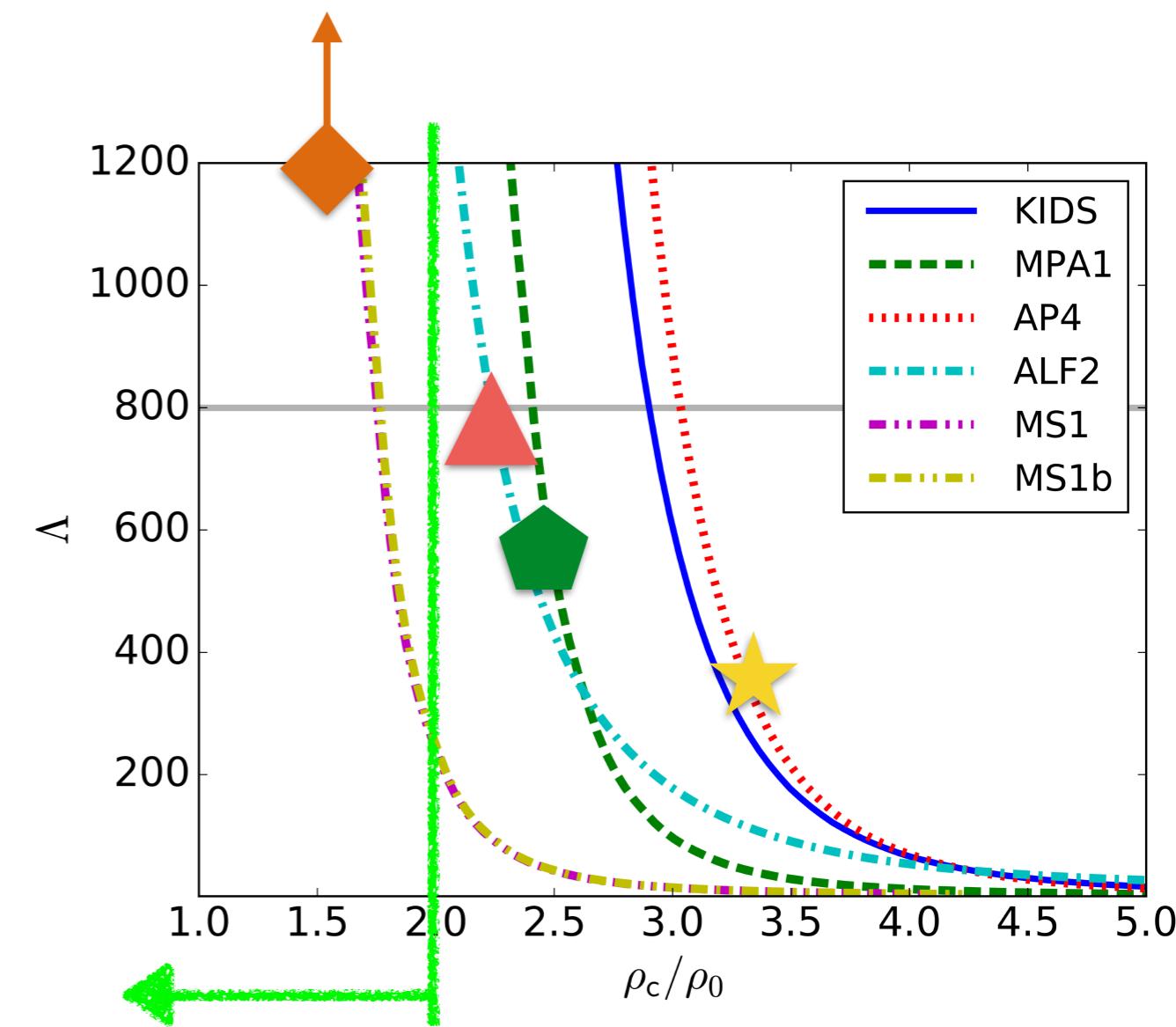
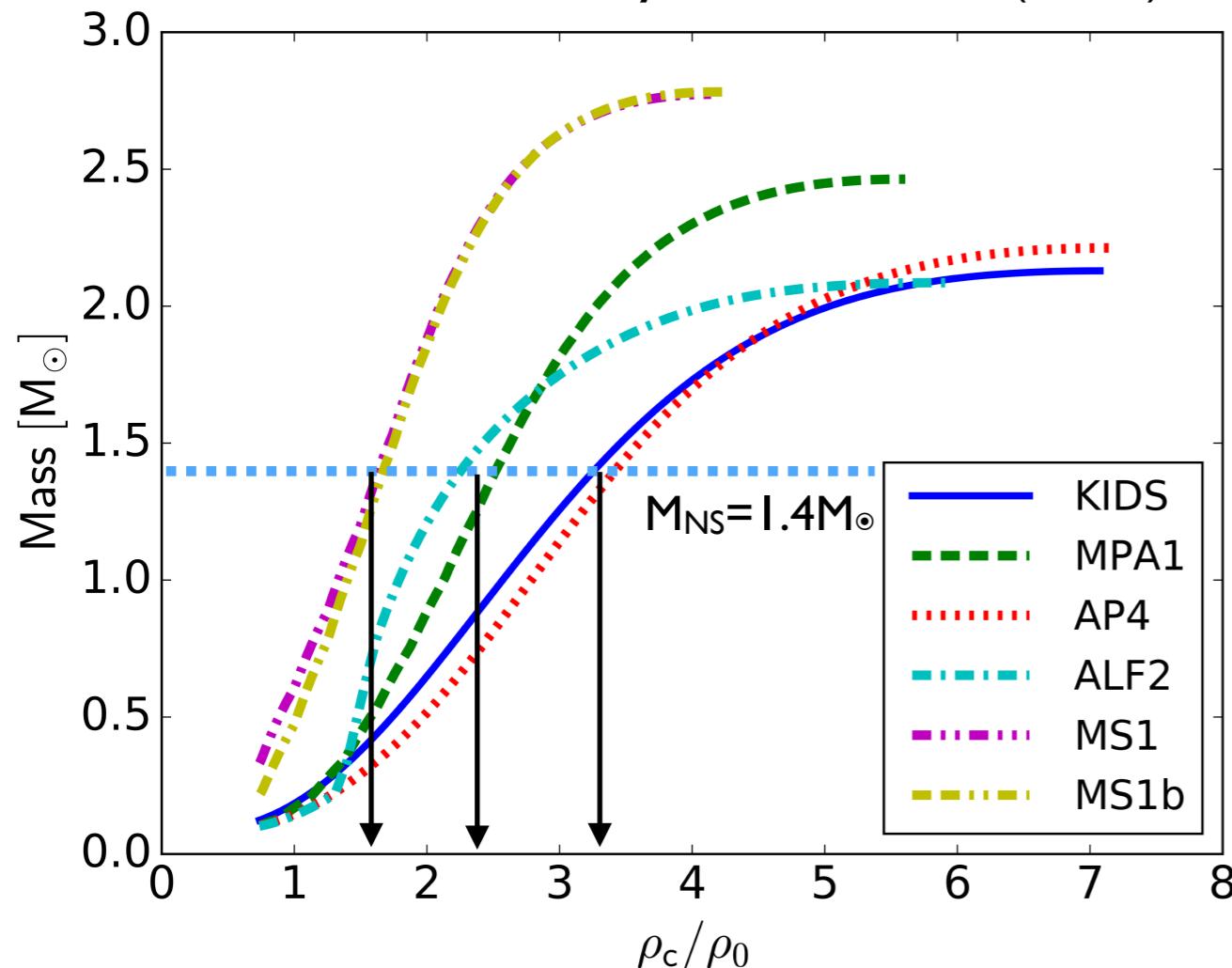


GW170817, $M_{\text{chirp}} = 1.188 M_\odot$

- low spin prior : $\Lambda(1.4 M_\odot) < 800$
- high spin prior : $\Lambda(1.4 M_\odot) < 1400$

Central Density at $M_{\text{NS}}=1.4 M_{\odot}$

Kim et al., New Physics: Sae Mulli (2018)



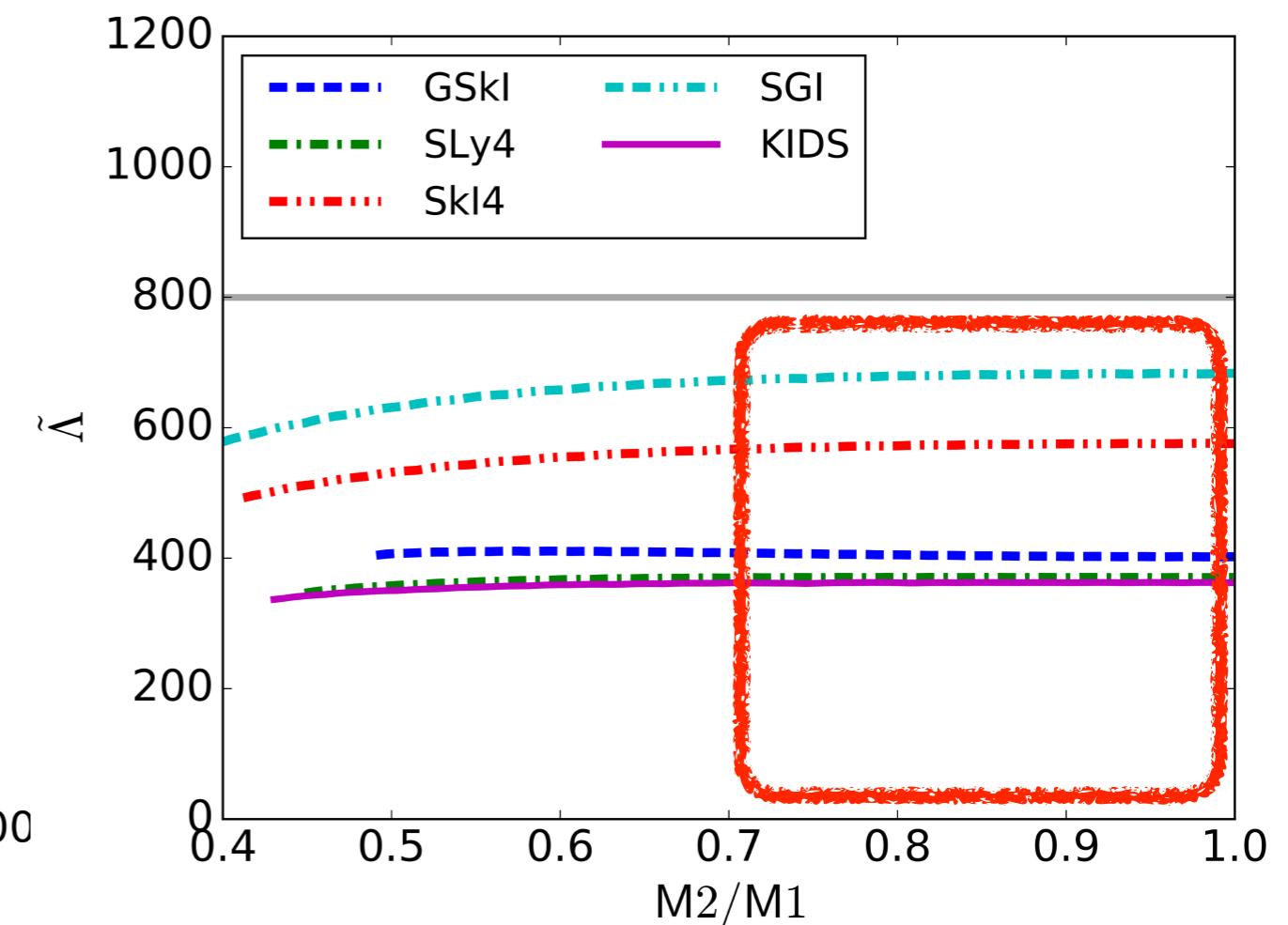
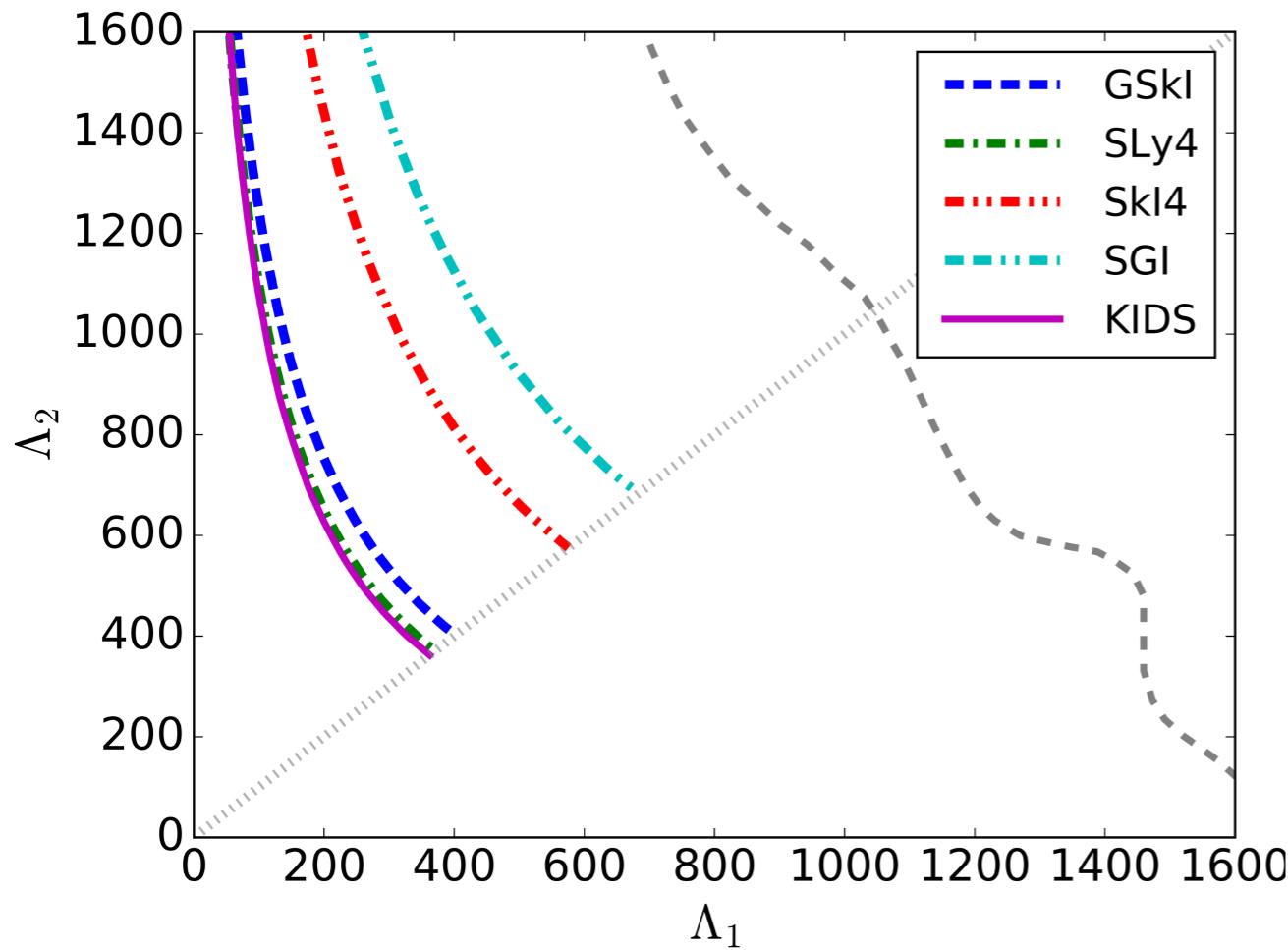
GW170817 - Abbott et al. (LSC and Virgo), arxiv:1805.11579
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ruled out ?

$$\Lambda(1.4 M_{\odot}) = 190^{+390}_{-120}$$

Tidal deformability in BNS

Kim et al., arxiv:1805.00219

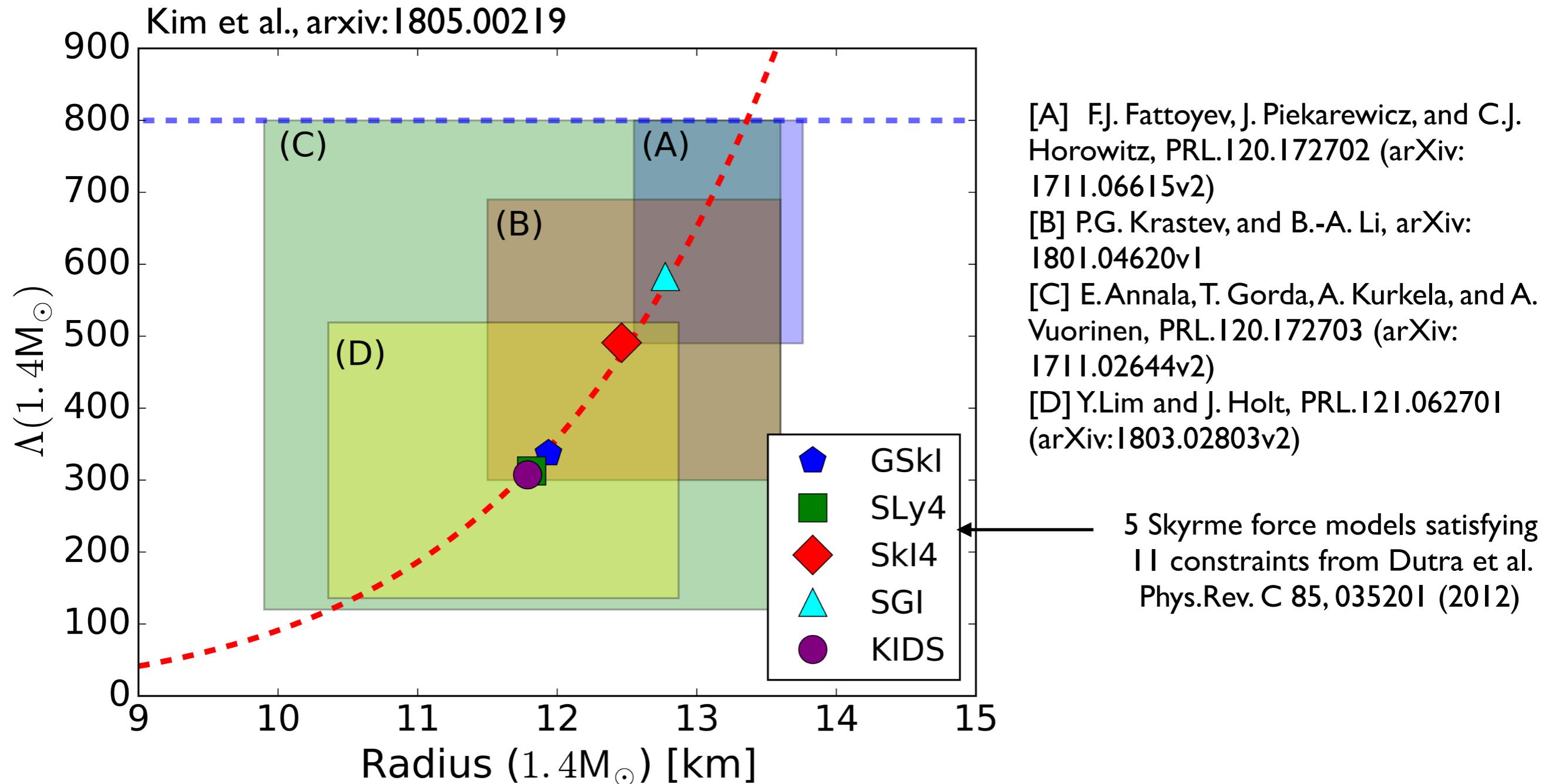


$$\tilde{\Lambda} = \frac{16}{13} \frac{(m_1 + 12m_2)m_1^4\Lambda_1 + (m_2 + 12m_1)m_2^4\Lambda_2}{(m_1 + m_2)^5}$$

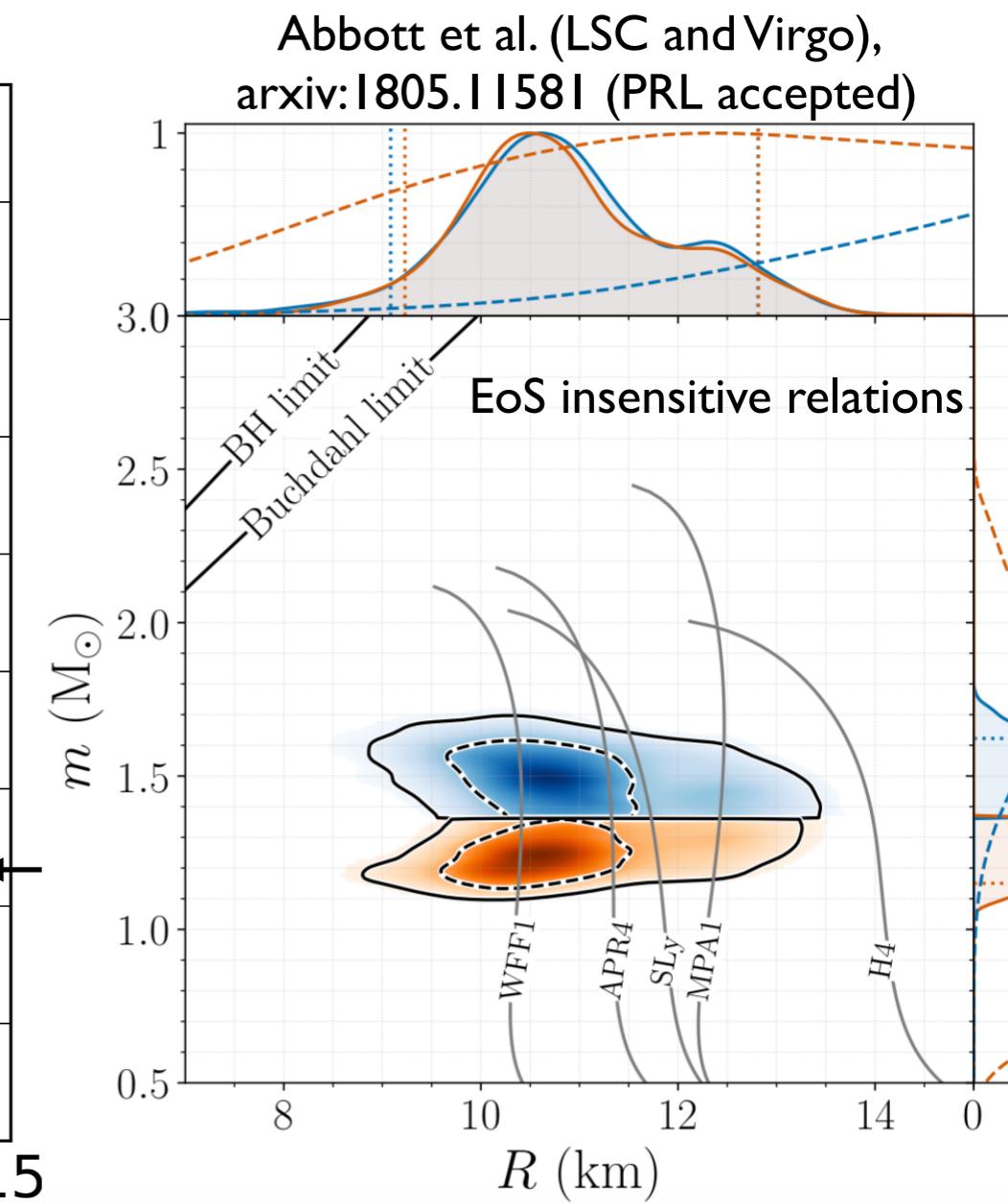
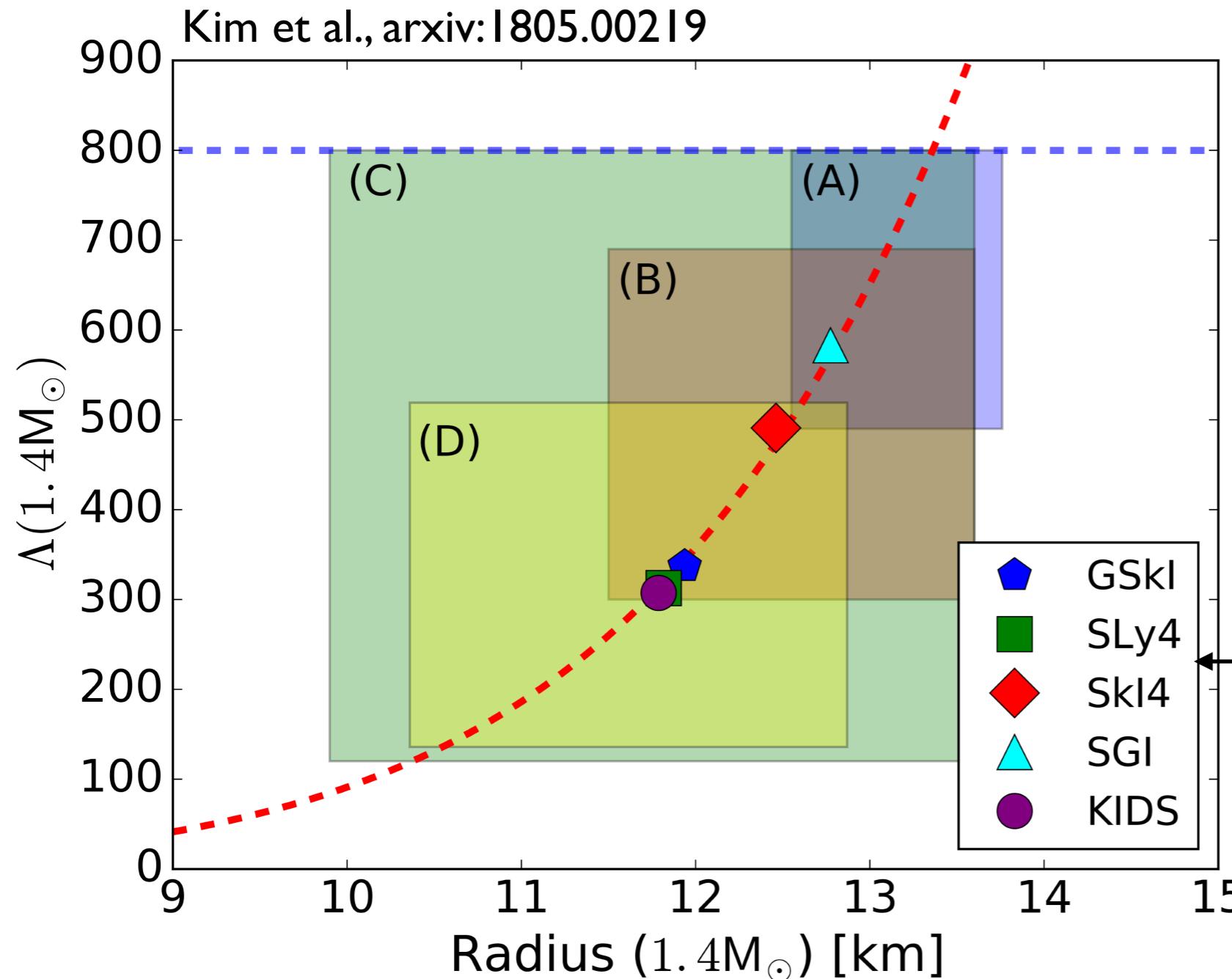
GW170817, $M_{\text{chirp}} = 1.188 M_{\odot}$

- low spin prior : reduced $\Lambda < 800$
- high spin prior : reduced $\Lambda < 700$

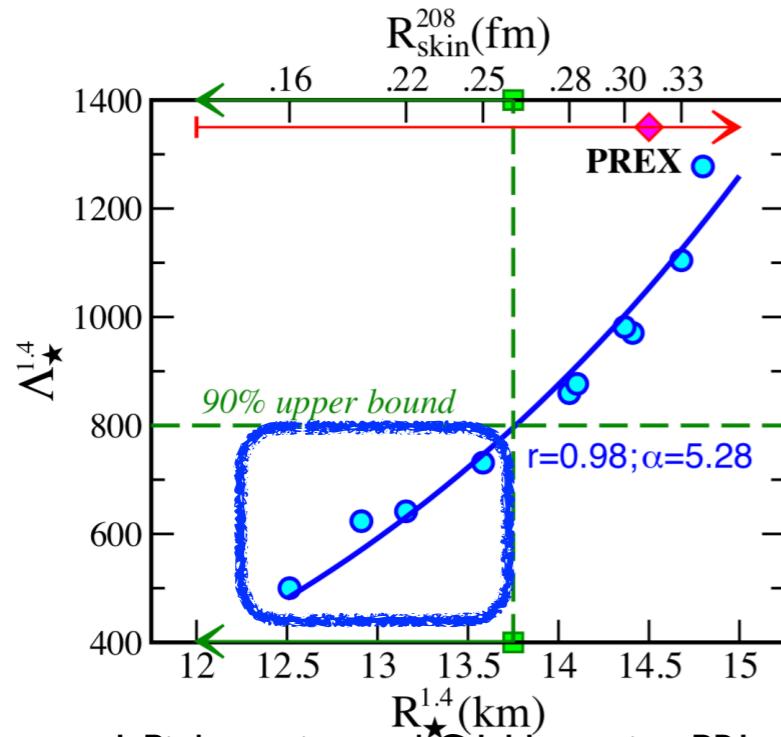
Comparison with recent works



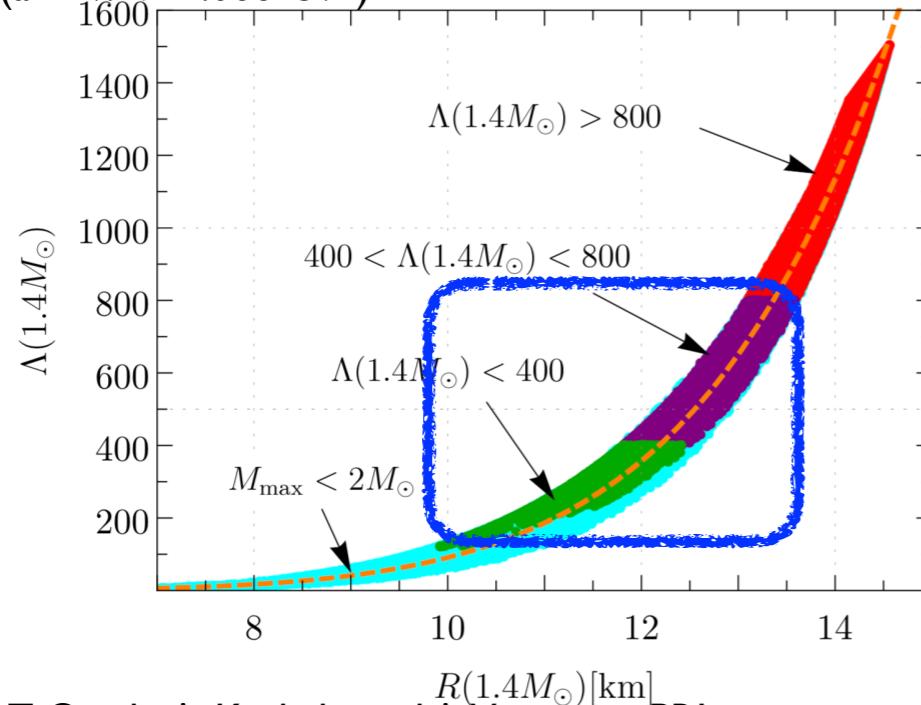
Comparison with recent works



Other Works



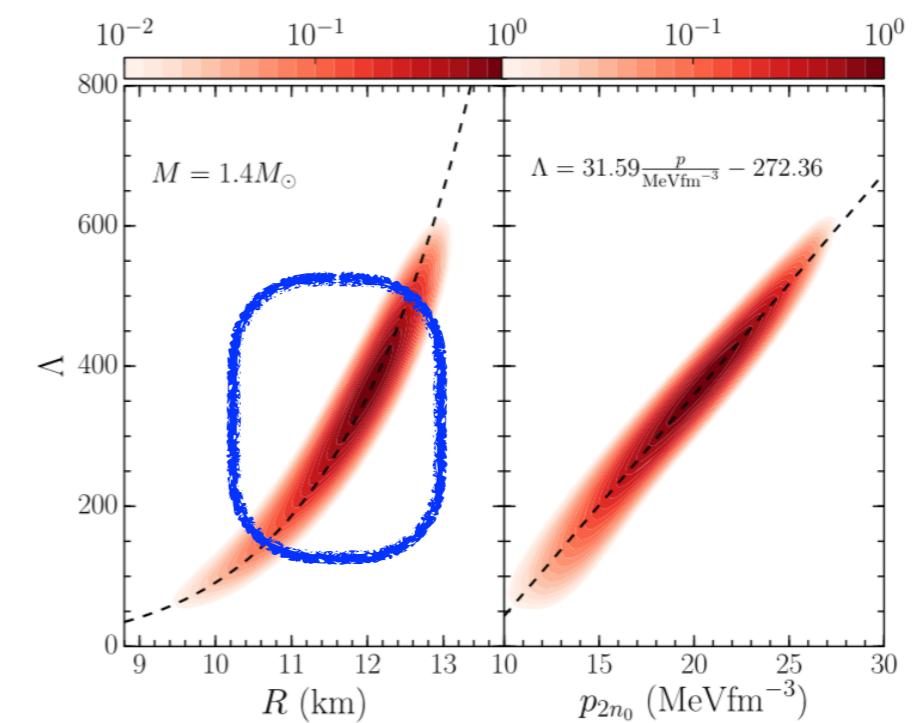
[A] F.J. Fattoyev, J. Piekarewicz, and C.J. Horowitz, PRL. 120.172702 (arXiv:1711.06615v2)



[C] E. Annala, T. Gorda, A. Kurkela, and A. Vuorinen, PRL. 120.172703 (arXiv:1711.02644v2)

EOS	R	β	k_2	λ	L
APR	11.55	0.179	0.0721	1.48	62
MDI ($x = 0$)	11.85	0.174	0.0707	1.65	62
MDI ($x = -1$)	13.59	0.152	0.0831	3.85	107
DBHF+Bonn B	12.64	0.163	0.0946	3.06	69
FPS	10.84	0.191	0.0664	1.00	35
SLY4	11.72	0.176	0.0762	1.68	47

[B] P.G. Krastev, and B.-A. Li, arXiv:1801.04620v1



[D] Y.Lim and J. Holt, PRL. 121.062701 (arXiv:1803.02803v2)

Prospects of the Observing Runs

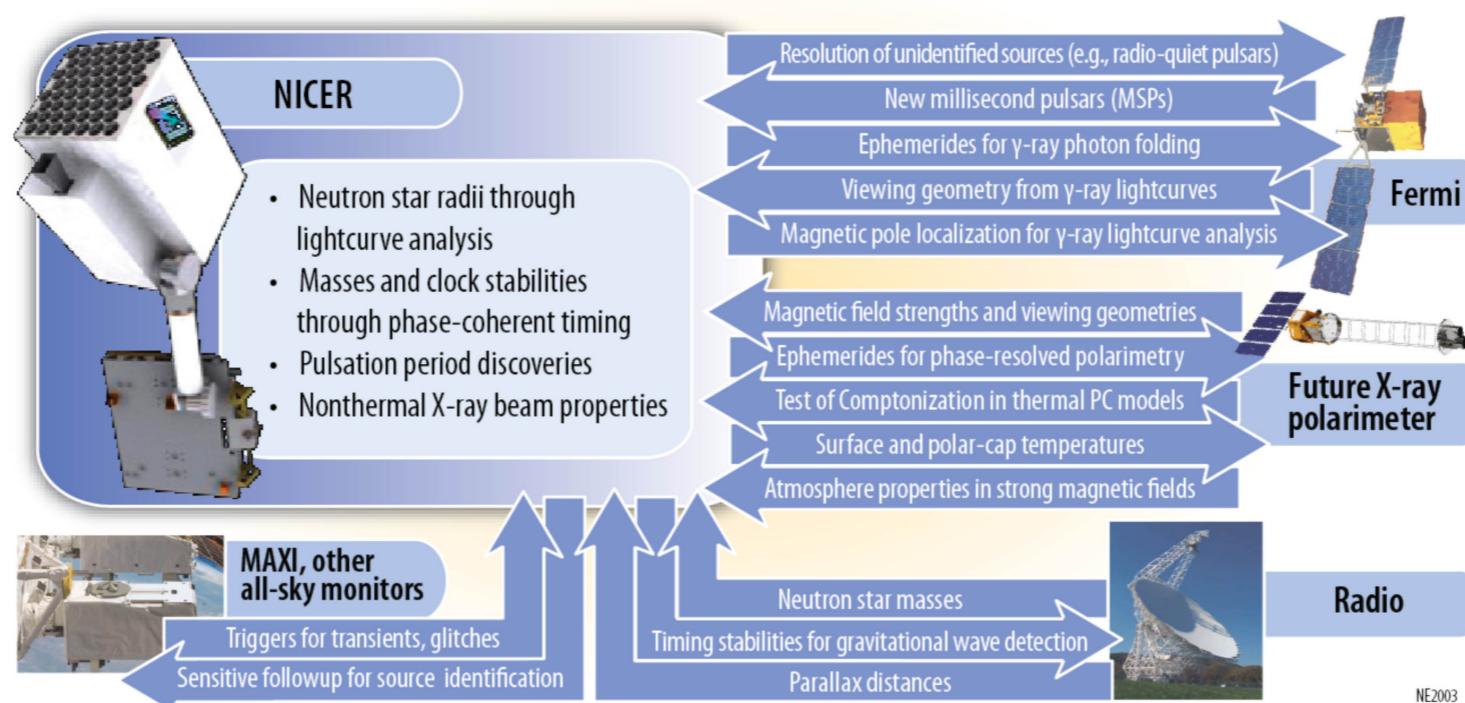
“Prospects for Observing and Localizing Gravitational-Wave Transients with Advanced LIGO, Advanced Virgo and KAGRA”, arXiv:1304.0670v4, LIGO-PI200087-v45, Living Rev. Relativity, 21, 3 (2018)

Epoch	2015–2016	2016–2017	2018–2019	2020+	2024+
Planned run duration	4 months	9 months	12 months	(per year)	(per year)
Expected burst range/Mpc	LIGO	40–60	60–75	75–90	105
	Virgo	—	20–40	40–50	40–70
	KAGRA	—	—	—	100
Expected BNS range/Mpc	LIGO	40–80	80–120	120–170	190
	Virgo	—	20–65	65–85	65–115
	KAGRA	—	—	—	125
Achieved BNS range/Mpc	LIGO	60–80	60–100	—	—
	Virgo	—	25–30	—	—
	KAGRA	—	—	—	—
Estimated BNS detections	0.05–1	0.2–4.5	1–50	4–80	11–180
Actual BNS detections	0	1	—	—	—
90% CR % within median/deg ²	5 deg ²	< 1	1–5	1–4	3–7
	20 deg ²	< 1	7–14	12–21	14–22
	460–530	230–320	120–180	110–180	9–12
Searched area % within	5 deg ²	4–6	15–21	20–26	23–29
	20 deg ²	14–17	33–41	42–50	44–52
					87–90

We expect to observe more BNS and/or NS-BH

NICER Neutron star Interior Composition ExploreR

- **launch:** early 2017, SpaceX
- **platform:** ISS ELC (ExPRESS Logistics Carrier)
- **instrument:** X-ray (0.2-12 keV)
- **objective**
 - **structure:** neutron star radii to 5%, cooling timescales
 - **dynamics:** stability of pulsars as clocks, properties of outbursts, oscillations, and precession
 - **energetics:** intrinsic radiation patterns, spectra, and luminosities



Prospects

- Both **Masses & Tidal Deformability of NS**
can be measured simultaneously
by GW generated from NS mergers
- **GW can give constraints on the radius of NS &
high-density EOS**
- Expecting more GWs from NS binary mergers

*Binary interactions
are always interesting*

Thanks

