

# A new mechanism to bind hadronic molecules 

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## Contents

$\square$ Where all these started-the pentaquark states
$\square$ A two-channel study of the $P_{c}(4450)$
> An Efimov like effect
> A new (long range ) binding mechanism
$\square$ Two recent extensions
$>$ Near-threshold Coulomb-like Baryonia: $\boldsymbol{\Lambda}_{\boldsymbol{c}}(\mathbf{2 5 9 5}) \boldsymbol{\Sigma}_{\boldsymbol{c}}\left(\overline{\Sigma_{c}}\right)$
$>$ Exotic doubly charmed $D_{s 0}^{*}(2317) D$ and $D_{s 1}(2460) D^{*}$ molecules
$\square$ Summary and outlook

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$\square$ A two-channel study of the $P_{c}(4450)$
> An Efimov like effect
> A new (long range ) binding mechanism
$\square$ Two recent extensions
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## The pentaquark states

Two Breit-Wigner states


$$
\begin{gathered}
\mathrm{Pc}(4380): M=4380 \pm 8 \pm 29 \mathrm{MeV} ; \\
\Gamma=205 \pm 18 \pm 86 \mathrm{MeV} \\
\mathrm{Pc}(4450): M=4449.8 \pm 1.7 \pm 2.5 \mathrm{MeV} ; \\
\Gamma=39 \pm 5 \pm 19 \mathrm{MeV}
\end{gathered}
$$

The preferred JP assignments are of opposite parity, with one state having spin $3 / 2$ and the other 5/2: $\left(3 / 2^{-}, 5 / 2^{+}\right),\left(3 / 2^{+}, 5 / 2^{-}\right),\left(5 / 2^{+}, 3 / 2^{-}\right)$



## The pentaquark states

Two Breit-Wigner states

$\mathrm{Pc}(4380): M=4380 \pm 8 \pm 29 \mathrm{MeV}$; $\Gamma=205 \pm 18 \pm 86 \mathrm{MeV}$
Pc(44450): $M=4449.8 \pm 1.7 \pm 2.5 \mathrm{MeV}$;
$\Gamma=39 \pm 5 \pm 19 \mathrm{MeV}$


Phys.Rev.Lett. 115 (2015) 072001

## The pentaquark states

Even before the experimental discovery
$\square$ Heavy-light diquarks.
> L. Maiani et al., Phys. Rev. D 71, 014028 (2005).

- Diquark-diquark-antiquark
> R. Jaffe and F. Wilczek, Phys. Rev. Lett. 91, 232003 (2003).
> A. Chandra et al., Mod. Phys. Lett. A 27, 1250006 (2012).
- Diquark- triquark
> M. Karliner and H. J. Lipkin, Phys. Lett. B 575, 249 (2003).
$\square$ Coupled channel
$>$ J.-J. Wu et al., Phys. Rev. Lett. 105, 232001 (2010).
- Weakly bound "molecules" of a baryon plus a meson
> M. B. Voloshin and L. B. Okun, JETP Lett. 23, 333 (1976)
> A. De Rujula et al., Phys. Rev. Lett. 38, 317 (1977)
> N. A. Törnqvist, Phys. Rev. Lett. 67, 556 (1991); N.A. Törnqvist, Z. Phys. C 61, 525 (1994)
$>$ Z.-C. Yang et al., Chin. Phys. C 36, 6 (2012)
$>$ W. L. Wang et al., Phys. Rev. C 84, 015203 (2011)
> M. Karliner and J. L. Rosner, Phys.Rev.Lett. 115, 122001 (2015)

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## Nature of the pentaquark states

$\square$ Tightly bound multiquark states
$\square$ Loosely bound multiquark sates-molecules
$\square$ Kinematical effects—triangle singularities

DOne pion exchange or one boson exchange
$\square$ Unitary chiral coupled channels and their extensions
$\square$ Contact interactions formulated in an EFT language

Not easy to discriminate different scenarios, see, e.g., the debate on X(3872)

## The pentaquark states

## T.J. Burns

Eur. Phys. J. A (2015) 51: 152

|  |  | $P_{c}(4380)^{+}$ | $P_{c}(4450)^{+}$ |
| :---: | :---: | :---: | :---: |
|  | Mass | $4380 \pm 8 \pm 29$ | $4449.8 \pm 1.7 \pm 2.5$ |
|  | Width | $205 \pm 18 \pm 86$ | $35 \pm 5 \pm 19$ |
|  | Assignment 1 | $3 / 2^{-}$ | $5 / 2^{+}$ |
|  | Assignment 2 | $3 / 2^{+}$ | $5 / 2^{-}$ |
|  | Assignment 3 | $5 / 2^{+}$ | $3 / 2^{-}$ |
|  |  |  | 2 |
|  | $\Sigma_{c}^{*+} \bar{D}^{0}$ | $4382.3 \pm 2.4$ |  |
|  | $\chi_{c 1} p$ |  | $4448.93 \pm 0.07$ |
|  | $\Lambda_{c}^{*+} D^{0}$ |  | $4457.09 \pm 0.35$ |
|  | $\Sigma_{c}^{+} \bar{D}^{* 0}$ |  | $4459.9 \pm 0.5$ |
|  | $\Sigma_{c}^{+} \bar{D}^{0} \pi^{0}$ |  | $4452.7 \pm 0.5$ |
| Analogy | X(3872) |  | Pc(4450) |
|  | $\bar{D}^{*}+D^{*} i$ |  | $\Sigma_{c} \bar{D}^{*}-\Lambda_{c 1} \bar{D}$ |

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$\square$ Two recent applications
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## A two channel study of the $P_{c}(4450)$



## A two channel study of the $P_{c}(4450)$

-There is standard one-pion exchange in the $\Sigma_{c} \bar{D}^{*}$ channel but no one-pion exchange in the $\Lambda_{c 1} D$ channel-not our concern here
-In the off diagonal channel


$$
\begin{gathered}
\left\langle\Lambda_{c 1} \bar{D}\right| V_{\mathrm{OPE}}(\vec{r})\left|\Sigma_{c} \bar{D}^{*}\right\rangle=\omega_{\pi} \tau \vec{\epsilon} \cdot \hat{r} W_{E}(r) \\
\tau=\sqrt{3} \text { for } \mathrm{I}=1 / 2 ; \tau=0 \text { for } \mathrm{I}=3 / 2
\end{gathered}
$$

$$
W_{E}(r)=\frac{g_{1} h_{2} \mu_{\pi}^{2}}{4 \pi \sqrt{2} f_{\pi}^{2}} \frac{e^{-\mu_{\pi} r}}{\mu_{\pi} r}\left(1+\frac{1}{\mu_{\pi} r}\right)
$$

$$
\begin{array}{r}
\omega_{\pi}=m\left(\Lambda_{c 1}\right)-m\left(\Sigma_{c}\right) \\
\mu_{\pi}=\sqrt{\left|m_{\pi}^{2}-\omega_{\pi}^{2}\right|}
\end{array}
$$

## A two channel study of the $P_{c}(4450)$

-There are standard one-pion exchange in the $\Sigma_{c} \bar{D}^{*}$ channel but no one-pion exchange in the $\Lambda_{c 1} D$ channel-not our concern here

■In the off diagonal channel


$$
\left|\mu_{\pi}\right|=\sqrt{\left|\omega_{\pi}^{2}-m_{\pi}^{2}\right|}=5 \sim 35 \mathrm{MeV} \ll m_{\pi}
$$

$\square$ In the $\mu_{\pi}=0$ limit, for $I=1 / 2$, one has the following potential

$$
\left\langle\Lambda_{c 1} \bar{D}\right| V_{\mathrm{OPE}}(\vec{r})\left|\Sigma_{c} \bar{D}^{*}\right\rangle=\frac{g_{1} h_{2} \omega_{\pi}}{4 \pi f_{\pi}^{2}} \sqrt{\frac{3}{2}} \frac{\vec{\epsilon} \cdot \hat{r}}{r^{2}}+\mathcal{O}\left(\mu_{\pi}^{2} r^{2}\right)
$$

## A $1 / \mathbf{r}^{2}$ potential and Efimov effect

$\square$ At zero energy the reduced Schroedinger equation for the s-wave

$$
-u^{\prime \prime}(r)+\frac{g}{r^{2}} u(r)=0
$$

For a finite energy analysis, see M. Bawin and S. A. Coon, Phys. Rev. A 67, 042712 (2003).
$>$ The above equation is scale invariant under the transformation $r \rightarrow \lambda_{0} r$,
$>$ The consequence is if $E_{n}$ is the binding energy, so is $E_{n+1}=E_{n} / \lambda_{0}^{2}$
$>$ This resembles the three-body system if thinking of $r$ as the hyper-radius $\rho$
$\square$ For $g>-1 / 4$, the above equation has a power law solution

$$
u(r)=c_{+} r^{\frac{1}{2}+\nu}+c_{-} r^{\frac{1}{2}-\nu} \quad \nu=\sqrt{1 / 4+g}
$$

$\square$ For $g<-1 / 4$, the solution enjoys discrete scale invariance

$$
u(r)=c r^{1 / 2} \sin \left(\nu \log \Lambda_{2} r\right) \quad \nu=\sqrt{-1 / 4-g} \quad \lambda_{0}=e^{\pi / v}
$$

$\Lambda_{2}$ encodes short-distance physics and breaks the exact scale invariance

## A surprising finding



The $\Sigma_{c} \bar{D}^{*}-\Lambda_{c 1} D$ interaction behaves like a $1 / r^{2}$ potential, which may lead to discrete scale invariance in a two-body hadronic system—an Efimov like effect

## $J^{p}=3 / 2^{-}$

$\square$ Four coupled-channels

$$
\Sigma_{c} \bar{D}^{*}\left({ }^{2} D_{3 / 2}\right) \quad \Sigma_{c} \bar{D}^{*}\left({ }^{4} S_{3 / 2}\right), \Sigma_{c} \bar{D}^{*}\left({ }^{4} D_{3 / 2}\right) \text { and } \Lambda_{c 1} \bar{D}\left({ }^{2} P_{3 / 2}\right)
$$

- The Schroedinger equation reads



## $J^{p}=3 / 2^{-}:$no discrete scale invariance

$\square$ Four coupled-channels

$$
\Sigma_{c} \bar{D}^{*}\left({ }^{2} D_{3 / 2}\right) \quad \Sigma_{c} \bar{D}^{*}\left({ }^{4} S_{3 / 2}\right), \Sigma_{c} \bar{D}^{*}\left({ }^{4} D_{3 / 2}\right) \text { and } \Lambda_{c 1} \bar{D}\left({ }^{2} P_{3 / 2}\right)
$$

$\square$ The Schroedinger equation reads

$$
-u_{i}^{\prime \prime}+\frac{g_{i}}{r^{2}} u_{i}=0
$$

$$
g_{i}=\left\{6,2,3+\sqrt{9+3 g^{2}}, 3-\sqrt{9+3 g^{2}}\right\}
$$

$\square$ Negative $\boldsymbol{g}_{\boldsymbol{i}}\left(<-\frac{1}{4}\right)$ can trigger discrete scale invariance, which means $|g|>\frac{5}{4 \sqrt{3}} \sim 0.7217$.
$\square$ With $g_{1}=0.59 \pm 0.01 \pm 0.07$ from $D^{*} \rightarrow D \pi / \gamma$, this requires $\left|h_{2}\right|>1.21_{-0.19}^{+0.25}$, well above $h_{2}=0.60 \pm 0.07$ from the CDF value extracted from $\Lambda_{c 1} \rightarrow \Sigma_{c} \pi$
$\square$ For $J^{p}=1 / 2^{-}, 3 / 2^{+}, 5 / 2^{+}, 5 / 2^{-}$the same conclusion

## $J^{p}=1 / 2^{+}$: discrete scale invariance likely

- Three coupled-channels

$$
\Sigma_{c} \bar{D}^{*}\left({ }^{2} P_{1 / 2}\right) \quad \Sigma_{c} \bar{D}^{*}\left({ }^{4} P_{1 / 2}\right) \text { and } \Lambda_{c 1} \overline{\bar{D}}\left({ }^{2} S_{1 / 2}\right)
$$

The Schroedinger equation reads

$$
\mathbf{g}\left(\frac{1}{2}\right)=\left(\begin{array}{ccc}
2 & 0 & g \\
0 & 2 & -\sqrt{2} g \\
g & -\sqrt{2} g & 0
\end{array}\right)
$$

$\square$ The attractive eigenvalue is $1-\sqrt{1+3 g^{2}}$, which requires $|g|>\frac{\sqrt{3}}{4} \sim 0.4330$ and $h_{2}=$ $0.73_{-0.06}^{+0.11}$, marginally overlapping with that of CDF $h_{2}=0.60 \pm 0.07$

## Long and short range consequences

- The approximate scale invariance of the Schroedinger equations has two consequences: long range and short range
$\square$ The long range consequence leads to the appearance of a geometric spectrum, depending on how far the systems are from $\mu_{\boldsymbol{\pi}}=\mathbf{0}$
$\square$ For $\mu_{\pi} \neq 0$, scale invariance holds for

$$
R_{s}<r<\frac{1}{\left|\mu_{\pi}\right|}
$$

The existence of a geometric excited state requires the relative size of the scale invariant window to be bigger than the discrete scaling factor
$\square$ For the $\mathrm{Pc}^{*},\left|R_{s} \mu_{\pi}\right| \simeq 10 \sim 20$, requiring $\left|g_{-}\right| \geq 1$, which is considerably larger than $1 / 4$

## Long and short range consequences

-The observation of geometric states in hadron and atomic physics shares a similar difficulty: the finetuning of the pion mass (hadrons) or the scattering length (atoms).

DIn atomic physics, one can turn to a magnetic field
-In hadron physics, one can fine-tune the pion mass in the lattice or increase $\left|g_{-}\right|$, by having a larger reduced mass (two bottom hadrons) or exchanging a kaon.
> For the first way out, we strongly encourage our lattice QCD
colleagues to pursue such a study
$>$ We will explore the $2^{\text {nd }}$ and $3^{\text {rd }}$ options in the following.
(1) To have a larger reduced mass

## $\Lambda_{c 1} \overline{\Xi_{b}}-\Sigma_{c}{\overline{\Xi_{b}}}^{\prime}$ baryonia system


$\square$ The potential

$$
\left\langle\Sigma_{c} \bar{\Xi}_{b}^{\prime}\right| V_{\mathrm{OPE}}(\vec{r})\left|\Lambda_{c 1} \bar{\Xi}_{b}\right\rangle=\frac{g_{3} h_{2} \omega_{\pi}}{8 \pi f_{\pi}^{2}} \frac{\sigma_{2} \cdot \hat{r}}{r^{2}}+\mathcal{O}\left(\mu_{\pi}^{2} r^{2}\right) g_{3}:{\overline{\Xi_{b}}}_{\bar{\Xi}_{b}^{\prime}}{ }^{\prime} \pi
$$

- Considering the following partial wave channels

$$
\begin{gathered}
0^{+}=\Sigma_{c} \bar{\Xi}_{b}\left({ }^{3} P_{0}\right)-\Lambda_{c 1} \bar{\Xi}_{b}\left({ }^{1} S_{0}\right), \\
0^{-}=\Sigma_{c} \overline{\bar{\Xi}}_{b}^{\prime}\left({ }^{1} S_{0}\right)-\Lambda_{c 1} \bar{\Xi}_{b}\left({ }^{3} P_{0}\right), \\
1^{-}=\Sigma_{c} \bar{\Xi}_{b}{ }^{\prime}\left({ }^{3} S_{1}-{ }^{3} D_{1}\right)-\Lambda_{c 1} \bar{\Xi}_{b}\left({ }^{1} P_{1}-{ }^{3} P_{1}\right),
\end{gathered}
$$

For $|g|>3 / 4$, the attractive eigenvalues will trigger discrete scale invariance, which with $g_{3}=0.973_{-0.042}^{+0.019}$ requires $\left|\boldsymbol{h}_{2}\right|>0.67_{-0.02}^{+0.03}$, overlapping with the CDF value
$\mathbf{g}\left(0^{+}\right)=\left(\begin{array}{ll}2 & g \\ g & 0\end{array}\right)$,
$\mathbf{g}\left(0^{-}\right)=\left(\begin{array}{ll}0 & g \\ g & 2\end{array}\right)$,
$\mathbf{g}\left(1^{-}\right)=\left(\begin{array}{cccc}0 & 0 & \frac{1}{\sqrt{3}} g & -\sqrt{\frac{2}{3}} g \\ 0 & 6 & -\sqrt{\frac{2}{3}} g & -\frac{1}{\sqrt{3}} g \\ \frac{1}{\sqrt{3}} g & -\sqrt{\frac{2}{3}} g & 2 & 0 \\ -\sqrt{\frac{2}{3}} g & -\frac{1}{\sqrt{3}} g & 0 & 2\end{array}\right)$

## Long and short range consequences

$\square$ Even if the vector force is not enough to trigger discrete scale invariance it will still play a remarkable role in binding
$\square$ Suppose the binding mechanism is $s$-wave short range physics, one has for $\left|r \leq R_{s}\right|$

$$
V(r)=V_{\mathrm{OPE}}(r) \theta\left(r-R_{s}\right)+\frac{C_{0}\left(R_{s}\right)}{4 \pi R_{s}^{2}} \delta\left(r-R_{s}\right)
$$

$>$ In the one-channel problem of $g>-\frac{1}{4}$ and in the absence of tensor OPE, the relative strength of $C_{0}$ is $v+1 / 2$ of that required to bind if $g=0$ (for $\left|\mu_{\pi} \mathrm{R}_{s}\right|<$ ),
$>$ Thus if $v=0(g \rightarrow-1 / 4)$ the short-range potential only has to be half the normal strength to be able to bind the system.

- If the binding mechanism is standard OPE or other intermediate physics, the number will change a bit but not the qualitative effect
$>$ For the $3 / 2^{-} \mathrm{Pc}^{*}$, the number is $70 \%$;
$>$ For the heavy baryonium, the number is $46 \%\left(0^{-}\right)$or $53 \%\left(1^{-}\right)$


## For the $1 / r^{2}$ force to work


$\square H_{1}$ and $H_{1}^{\prime}$ are of opposite parity but with the same spin
$\square H_{2}$ and $H_{2}^{\prime}$ are of the same parity and their spin differs by one
$\square m\left(H_{1 / 2}\right)-m\left(H_{1 / 2}^{\prime}\right) \approx m(\phi)$, implying long range interaction
$\square$ The larger $g_{1}, g_{2}, m(\phi)$, the smaller $m\left(H_{1 / 2}\right)-m\left(H_{1 / 2}^{\prime}\right)-m(\phi)$, the stronger the attraction

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> A new (long range ) binding mechanism
$\square$ Two recent applications
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## A coulomb like force: a modification of the $1 / \mathbf{r}^{2}$ case


$\square H_{1}$ and $H_{1}^{\prime}$ are of opposite parity but with the same spin
$\square \boldsymbol{H}_{2}$ and $\boldsymbol{H}_{\mathbf{2}}^{\prime}$ are of opposite parity but with the same spin
$\square m\left(H_{1 / 2}\right)-m\left(H_{1 / 2}^{\prime}\right) \approx m(\phi)$, implying long range interaction
$\square$ The larger $g_{1}, g_{2}, \boldsymbol{m}(\phi)$, the smaller $m\left(H_{1 / 2}\right)-m\left(H_{1 / 2}^{\prime}\right)$ $\mathrm{m}(\phi)$, the stronger the attraction

## A doubly charmed baryon $Y_{c c}$ (5050)



$$
V_{\mathrm{OPE}}(r)=-\frac{h_{2}^{2} \omega_{\pi}^{2}}{4 \pi f_{\pi}^{2}} \frac{e^{-\mu_{\pi} r}}{r}\left(\begin{array}{ll}
0 & 1 \\
1 & 0
\end{array}\right)
$$

where $\mu_{\pi}^{2}=m_{\pi}^{2}-\omega_{\pi}^{2}$ with $\omega_{\pi}=m_{\Lambda_{c 1}}-m_{\Sigma_{c}}$

Attraction appears in spin 0 channel:

$$
\left|Y_{c c}\right\rangle=\frac{1}{\sqrt{2}}\left\{\left|\Lambda_{c 1} \Sigma_{c}\right\rangle+\left|\Sigma_{c} \Lambda_{c 1}\right\rangle\right\}
$$

## A doubly charmed baryon $Y_{c c}$ (5050)

Assuming again, that the one-baryon exchange is only valid above a certain cutoff radius

$$
V(r)=V_{\mathrm{OPE}}(r) \theta\left(r-R_{c}\right)+\frac{C_{0}}{4 \pi R_{c}^{2}} \delta\left(r-R_{c}\right)
$$

Introducing a reduced coupling

$$
c_{0}=-\frac{2 \mu_{Y} C_{0}}{4 \pi R_{c}}
$$ and $c_{0} \geq 1$ generates a bound state with binding momentum $\gamma=\left(c_{0}-1\right) / R_{c}$



- $c_{0} \rightarrow-\infty, E_{B}=-0.09_{-0.08}^{+0.06} \mathrm{MeV}$
- $c_{0} \rightarrow 1, E_{B}=-1.9_{-0.6}^{+0.5} \mathrm{MeV}$
- $c_{0}>0.9_{-0.4}^{+0.2} 1$, a shallow excited state appears
$R_{c}=1 \mathrm{fm}$ probably lies in an intermediate zone dominated by two-pion exchange and other contributions which might be attractive. Hence we expect the fundamental state of the doubly charmed Ycc to be deeper than the predictions from OPE alone


## A hidden charmed baryon $Y_{c \bar{c}}$ (5050)

Replacing $\Sigma_{c}$ with $\overline{\Sigma_{c}}$ will lead to a formation of hidden charmed baryon $Y_{c \bar{c}}(\mathbf{5 0 5 0})$ in both spin 0 and 1. The discussion is more involved because it involves annihilation.

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> Are there near-threshold Coulomb-like Baryonia?
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> ${ }^{2}$ State Key Laboratory of Nuclear Physics and Technology, School of Physics, Peking University, Beijing 100871, China
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> (0) (Received 6 May 2017; published 2 May 2018)
> https://crossmark.crossetetorg/lialog/?
of the $\Lambda_{c}(2590)$ and $\Sigma_{c}$, the pion is exenangea in J -wave. This gives rise to a Coulomb-like force that might
be able to bind the system. If one takes into account that the pion is not exactly on the mass shell, there is a
shallow S-wave state, which we generically call the $Y_{c c}(5045)$ and $Y_{c \bar{c}}(5045)$ for the $\Lambda_{c}(2590) \Sigma_{c}$ and
$\Lambda_{c}(2590) \bar{\Sigma}_{c}$ systems respectively. For the baryon-antibaryon case this Coulomb-like force is independent
of spin: the $Y_{c \bar{c}}(5045)$ baryonia will appear either in the spin $S=0$ or $S=1$ configurations with G-parities
$G=(-1)^{L+S+1}$. For the baryon-baryon case the Coulomb-like force is attractive in the spin $S=0$
configuration, for which a doubly charmed molecule is expected to form near the threshold. This type of
spectrum might be very well realized in other molecular states composed of two opposite parity hadrons
with the same spin and a mass difference close to that of a pseudo-Goldstone boson, of which a few
examples include the $\Lambda(1405) N, \Lambda(1520) \Sigma^{*}, \Xi(1690) \Sigma, D_{s 0}^{*}(2317) D$ and $D_{s 1}^{*}(2460) D^{*}$ molecules.

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## Exotic doubly charmed mesons

$\square$ A straightforward extension of the above idea is investigating the exchange of the kaon-large attraction
$\square$ In such a case, $D_{s 0}^{*}(2317) D$ and $D_{s 1}(2460) D^{*}$ are two interesting systems


Using the $D_{\text {s } 0}^{*}(2317) D$ system as one example

## Exotic doubly charmed mesons

- In the following basis: $\left\{D D_{s 0}^{*}, D_{s 0}^{*} D\right\}\left\{D^{*} D_{s 1}^{*}, D_{s 1}^{*} D^{*}\right\}$

$$
\begin{aligned}
V(\vec{q})=-h^{2} \frac{\omega_{K}^{2}}{f_{\pi}^{2}} \frac{1}{m_{K}^{2}-\omega_{K}^{2}+\vec{q}^{2}}\left(\begin{array}{ll}
0 & 1 \\
1 & 0
\end{array}\right) \\
\omega_{K}=m_{D_{s 0}^{*}}-m_{D} \text { or } m_{D_{11}^{*}}-m_{D^{*}}
\end{aligned}
$$

ㅁ The effective range is set by $\mu_{K}^{2}=m_{K}^{2}-\omega_{K}^{2}$, about $200 \mathbf{M e V}$

- For the following linear combinations, the interaction is attractive

$$
\begin{aligned}
& \frac{1}{\sqrt{2}}\left[\left|D D_{s 0}^{*}\right\rangle+\left|D_{s 0}^{*} D\right\rangle\right], \\
& \frac{1}{\sqrt{2}}\left[\left|D^{*} D_{s 1}^{*}\right\rangle+\left|D_{s 1}^{*} D^{*}\right\rangle\right]
\end{aligned} \quad V(r)=-h^{2} \frac{\omega_{K}^{2}}{f_{\pi}^{2}} \frac{e^{-\mu_{K} r}}{4 \pi r}
$$

## Exotic doubly charmed mesons

ㅁ. The system will bind for $\quad \lambda_{B}=\frac{2 \mu_{H}}{\mu_{K}} \frac{\omega_{K}^{2}}{4 \pi f_{\pi}^{2}} h^{2} \geq 1.68$ which means for $\mathrm{DD}_{\mathrm{s} 0}^{*}$ and $\mathrm{DD}_{\mathrm{s} 1},|h|>0.43$ and 0.40 , respectively
$\square$ The requirement is satisfied, because $h \approx 0.5 \sim 0.9$ as deduced from the $D$ meson decay

$$
\begin{aligned}
\Gamma\left(D_{0} \rightarrow D \pi\right) & =\Gamma\left(D_{0} \rightarrow D \pi^{0}\right)+\Gamma\left(D_{0} \rightarrow D \pi^{ \pm}\right) \\
& =\frac{3}{2} \Gamma\left(D_{0} \rightarrow D \pi^{ \pm}\right) \\
& =\frac{3}{2} \frac{m_{D}}{m_{D_{0}}} \frac{q_{\pi}}{2 \pi} \frac{h^{2}}{f_{\pi}^{2}}\left(m_{D_{0}}-m_{D}\right)^{2},
\end{aligned}
$$

$$
\begin{aligned}
& \mathrm{D}_{0}^{0} \rightarrow h=0.61 \pm 0.07 \\
& \mathrm{D}_{0}^{+} \rightarrow h=0.50 \pm 0.06 \\
& \mathrm{D}_{1}^{0} \rightarrow h=0.8 \pm 0.2 \\
& \quad \text { arXiv: } 1207.6940
\end{aligned}
$$

ㅁ Concretely, one has $E_{B}=-40_{-50}^{+30} \mathrm{MeV} \quad E_{B}=-50_{-50}^{+30} \mathrm{MeV}$

## Understanding the results in EFT

## $\square$ The kaon exchange can be rewritten

$$
V_{\mathrm{OKE}}(\vec{q})=-\frac{2 \pi}{\mu_{H} \Lambda_{\mathrm{OKE}}} \frac{\mu_{K}^{2}}{\mu_{K}^{2}+\vec{q}^{2}} \quad \Lambda_{\mathrm{OKE}}=\frac{2 \pi}{\mu_{H}} \frac{f_{\pi}^{2} \mu_{K}^{2}}{h^{2} \omega_{K}^{2}} \simeq 50_{-20}^{+40} \mathrm{MeV}
$$

- We count $\quad V_{\mathrm{OKE}}(\vec{q}) \sim \frac{2 \pi}{M Q}$, which is enhanced
- Heavy quark symmetry implies

$$
\begin{aligned}
& V_{C}\left(\vec{q}, D D_{s 0}^{*}\right)=C_{0 a}, \\
& V_{C}\left(\vec{q}, D^{*} D_{s 1}^{*}\right)=C_{0 a}+\vec{S}_{1} \cdot \vec{S}_{2} C_{0 b} \quad \begin{array}{l}
\text { - } \\
\text { (2017), arXiv: } 17060.02588 \text { [hep-ph]. }
\end{array}
\end{aligned}
$$

## Understanding the results in EFT

$\square$ In an natural scaling, the contact terms count as of subleading

$$
C_{0 a} \sim \frac{2 \pi}{M^{2}} \quad, \quad C_{0 b} \sim \frac{2 \pi}{M^{2}}
$$

$\square$ In an unnatural scaling, they also appear at LO (fine tuning)
$>$ Even in a worst case scenario, there exists a repulsive core at the cutoff radius

$$
V_{\mathrm{EFT}}=V_{\mathrm{OKE}}(r) \theta\left(r-R_{c}\right)+C_{0}\left(R_{c}\right) \frac{\delta\left(r-R_{c}\right)}{4 \pi R_{c}^{2}}
$$

The system will still bind for $R_{c} \leq 1.3_{-0.3}^{+0.3} \mathrm{fm}$

## Summary and outlook

- We have studied the $\Sigma_{c} \bar{D}^{*}-\Lambda_{c 1} D$ off diagonal interaction in an attempt to better understand the $P_{C}(4450)$ and accidentally identified a new binding mechanism that may lead to discrete scale invariance
$\square$ We have identified two other similar mechanisms that are of long-range nature and can lead to relatively robust predictions of molecular states, namely $\Lambda_{c}(2590) \Sigma_{c}\left(\overline{\bar{\Sigma}_{c}}\right)--Y_{c c / \bar{c}}(5045)$, $D_{s 0}^{*}(2317) D$ and $D_{s 0}^{*}(2317) D^{*}$
$\square$ Many similar but more sophisticated studies are underway to explore/check the proposed mechanisms




## Thanks for your attention

August 23rd， 2018

## Bottom line

If binding happens for distances in which the present picture is valid，short－range physics is not necessary
$>3 / 2^{-}, 1 / 2^{+}, 0.94 \mathrm{fm}, 0.92 \mathrm{fm}$ two－pion exchange and hadron finite－size effects dominate for $r<\frac{m_{\pi}}{2} \sim 0.7 \mathrm{fm}$ ，
$>0^{-}, 1^{-}, 1^{+}, 0^{+}$baryoia $0.40 \mathrm{fm}, 0.84 \mathrm{fm}, 0.87 \mathrm{fm}, 0.86 \mathrm{fm}$
＞Two systems bind in p－wave，where the vector force effectively induces the existence of a channel behaving much like an s－wave

In short，the vector force induces a series of binding mechanisms which do not require the ratio $m_{\pi} / \mu_{\pi}$ to be particularly large（a factor of $2-3$ is probably enough）and which in a few cases lead to predictions of new molecules．

## Introducing a cutoff

$\square$ Suppose the potential is only valid for large radius

$$
V\left(r ; R_{c}\right)=V(r) \theta\left(r-R_{c}\right)
$$



The system will bind for $R_{c} \leq 1.3 \pm 0.3 \mathrm{fm}$

For $R_{C}=0.5 \mathrm{fm}, E_{B}=-6_{-7}^{+4} \mathrm{MeV}$

## Summary and outlook

$$
\begin{array}{ll}
\Xi_{b}^{\prime}(5935)^{-} & J^{P}=\frac{1}{2}^{+} \quad \text { Status: } * * * \\
\hline & \Xi_{\mathbf{b}}^{\prime}(\mathbf{5 9 3 5})^{-} \text {MASS } \\
\frac{\operatorname{VALUE}(\mathrm{MeV})}{\mathbf{5 9 3 5 . 0 2} \pm \mathbf{0 . 0 2} \pm \mathbf{0 . 0 5}} & 1 \frac{\text { DOCUMENT ID }}{\text { AAIJ }} \quad 15 \mathrm{H} \\
\frac{\text { TECN }}{\text { LHCB }} \frac{\text { COMMENT }}{\text { pp at } 7,8 \mathrm{TeV}}
\end{array}
$$

${ }^{1}$ Not independent of the mass difference measurement below. Observed in $\bar{E}_{b}^{0} \pi^{-}$channel with $\Xi_{b}^{0} \rightarrow \Xi_{c}^{+} \pi^{-}$and $\Xi_{c}^{+} \rightarrow p K^{-} \pi^{+}$.


$$
J^{P}=\frac{3}{2}^{+} \quad \text { Status: } * * *
$$

Quantum numbers are based on quark model expectations.

| $\bar{E}_{b}(5945)^{0}$ MASS |  |  |  |
| :---: | :---: | :---: | :---: |
| VALUE (MeV) | DOCUMENT ID | TECN | COMMENT |
| $5949.8 \pm 1.4$ OUR AVERAGE |  |  |  |
| $5949.8 \pm 0.1 \pm 1.4$ | ${ }^{1}$ AAIJ 16aE | LHCB | $p p$ at 7, 8 TeV |
| $5948.9 \pm 0.8 \pm 1.4$ | 2 CHATRCHYAN 12 S | CMS | $p p$ at $7 \mathrm{TeV}, 5.3 \mathrm{fb}{ }^{-1}$ |

