

# Two science cases with the CMB B-mode polarization: Hubble tension and LQC prediction

**Donghui Jeong**, and Marc Kamionkowski  
*Gravitational waves, CMB polarization, and the Hubble tension*  
[2020, PRL 124, 041301 \[arXiv:1908.06100\]](#)

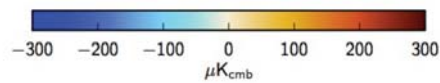
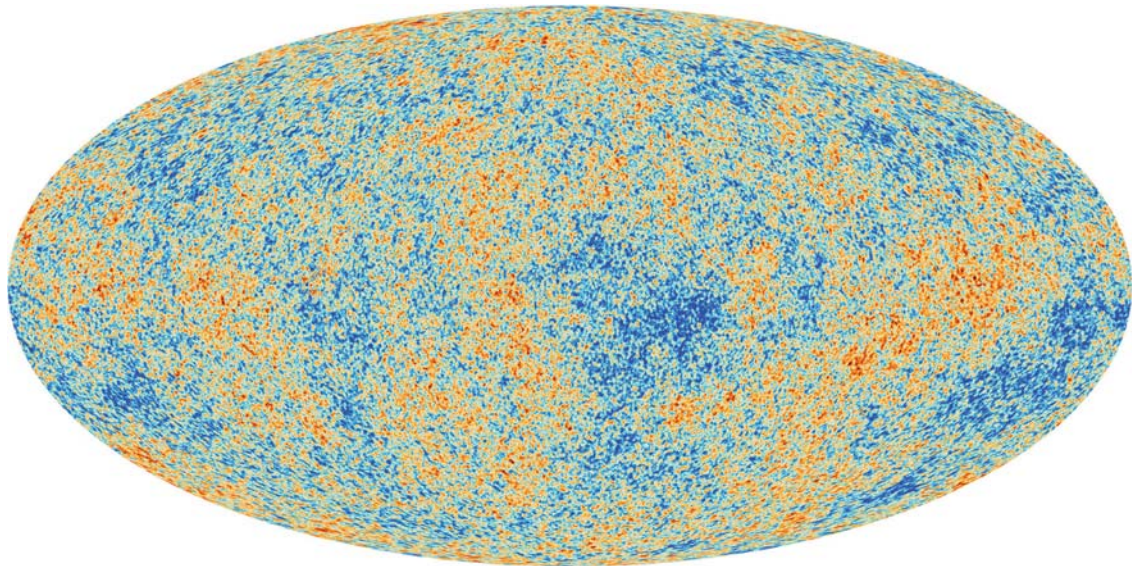
Abhay Ashtekar, Brajesh Gupta, **Donghui Jeong**, and V. Sreenath  
*Alleviating the tension in CMB using Planck-scale Physics*  
[2020, PRL 125, 051302 \[arXiv:2001.11689\]](#)

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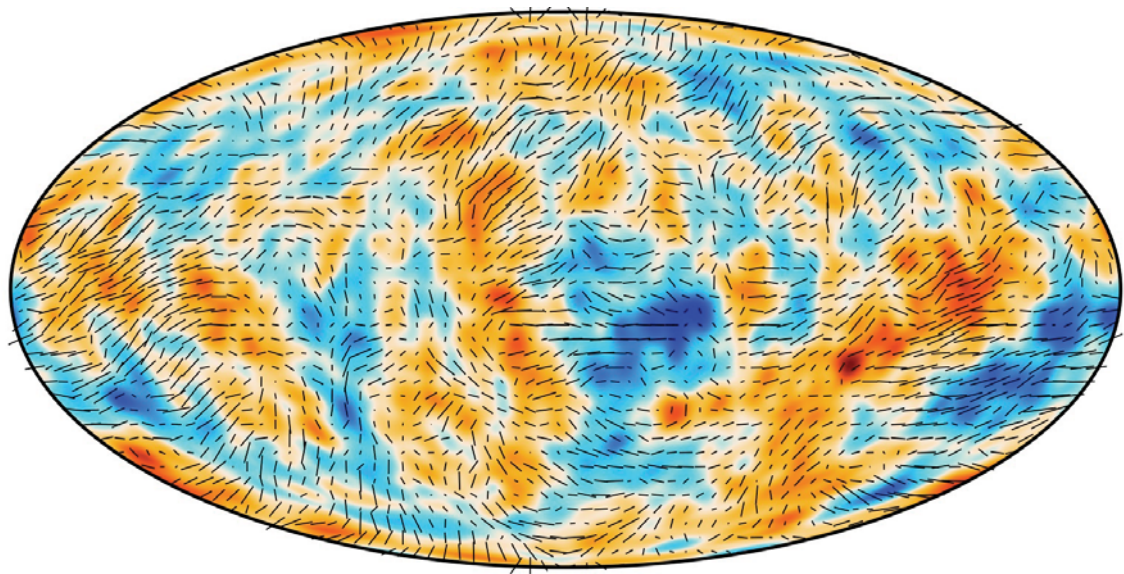
SGC2020 workshop, 20 November 2020

# Temperature map of the CMB



maximum likelihood posterior map  
Planck Collaboration

# Polarization map of the CMB



1 0.41  $\mu\text{K}$

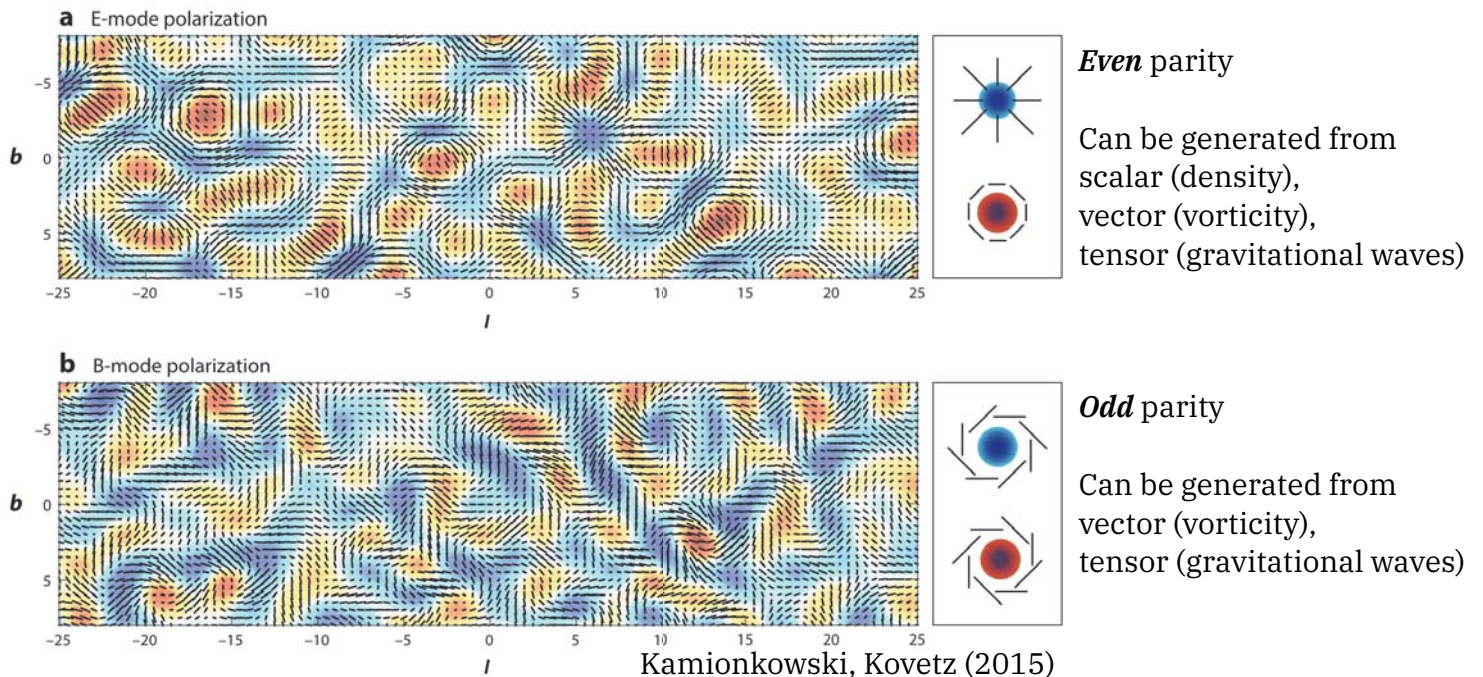
-160



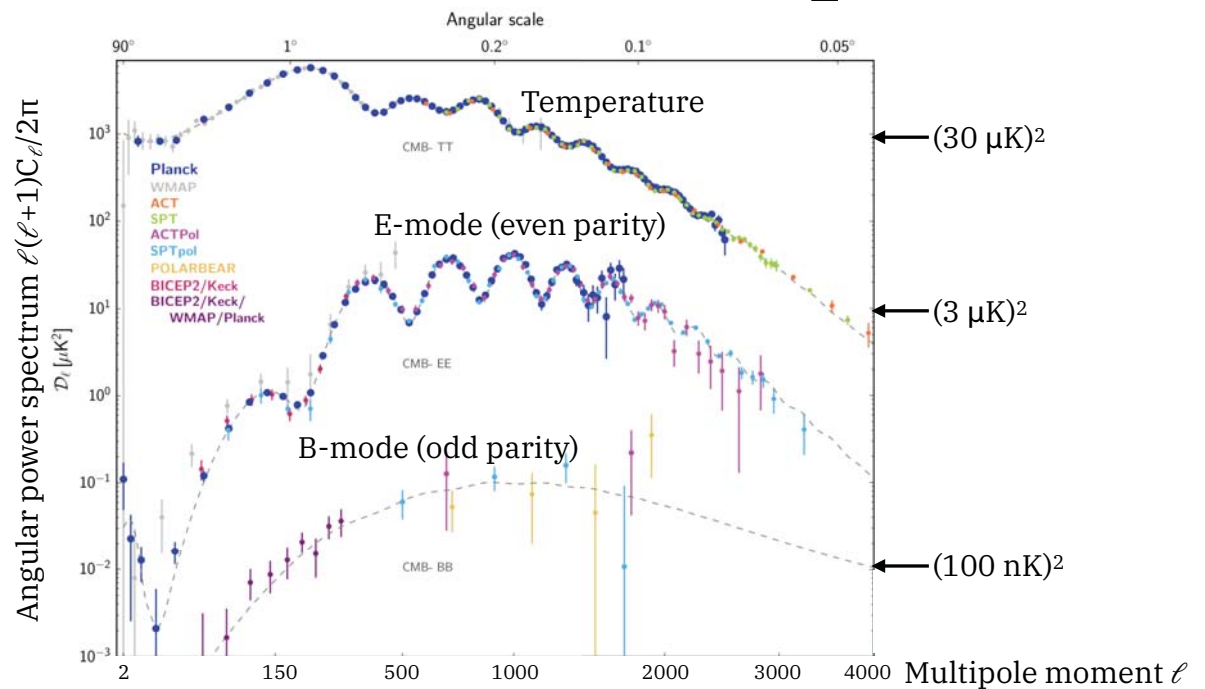
160  $\mu\text{K}$

Planck map smoothed with  $5^\circ$  filter

# E-mode and B-mode



$C_\ell$  = fluctuation amplitude



# Three puzzles in the CMB

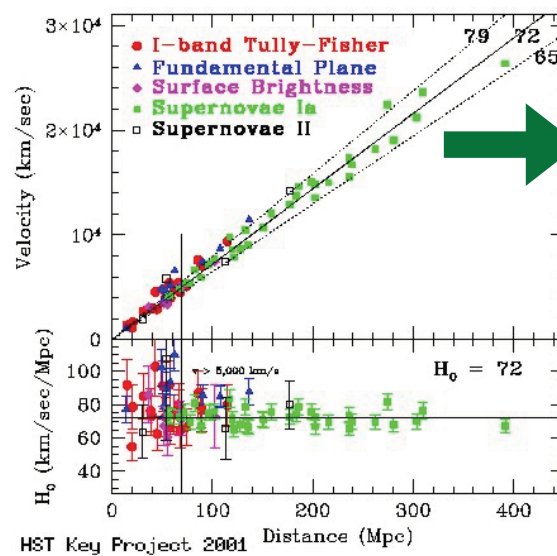
- Hubble tension
- Lack of CMB clustering on large angular scales
- “Crisis for cosmology”:  $A_L$  (lensing amplitude) anomaly



# Three puzzles in the CMB

- Hubble tension
- Lack of CMB clustering on large angular scales
- “Crisis for cosmology”:  $A_L$  (lensing amplitude) anomaly

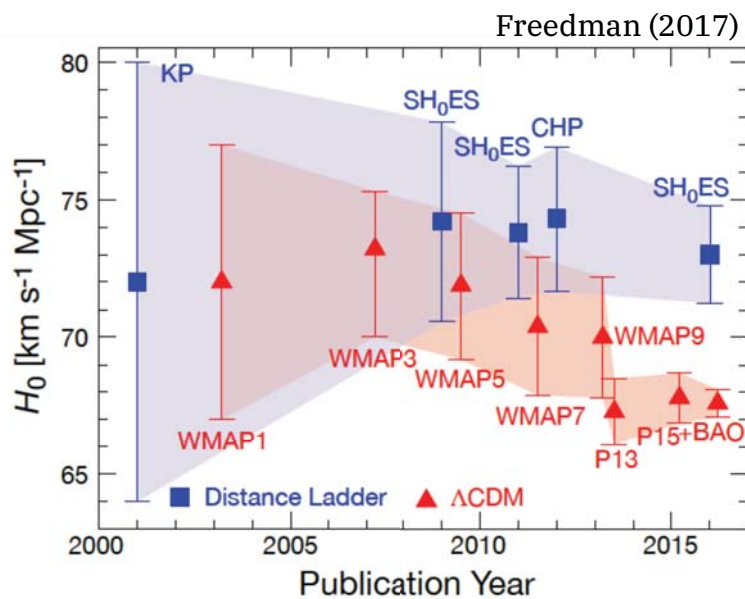
# $H_0$ from the HST Key Project

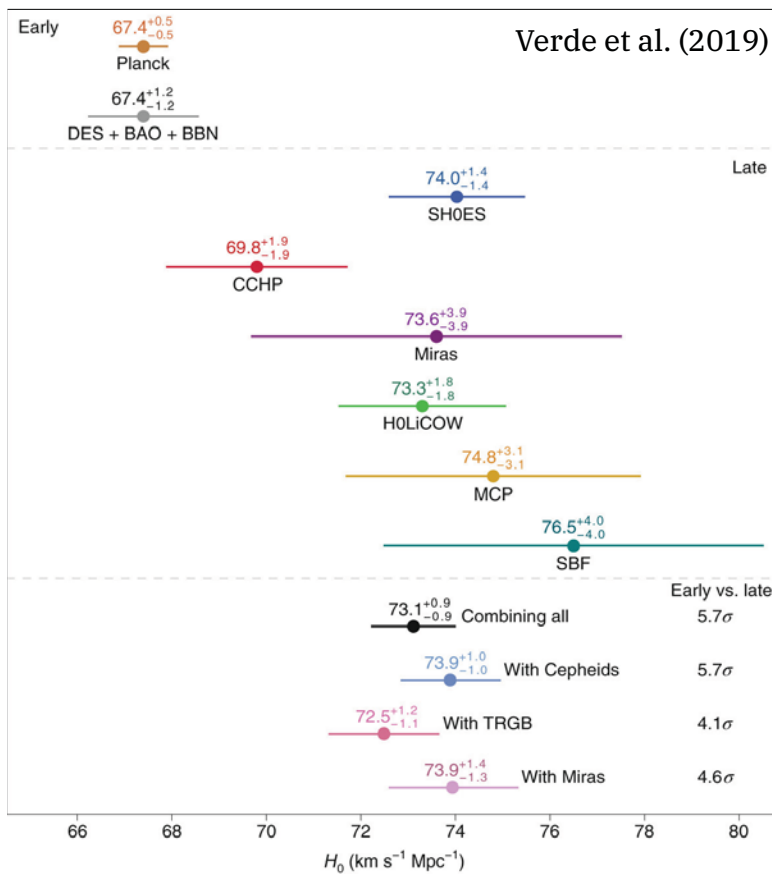


$H_0$  = slope of this line  
=  $100h \text{ km/s/Mpc}$



# $H_0$ since HST Key Project

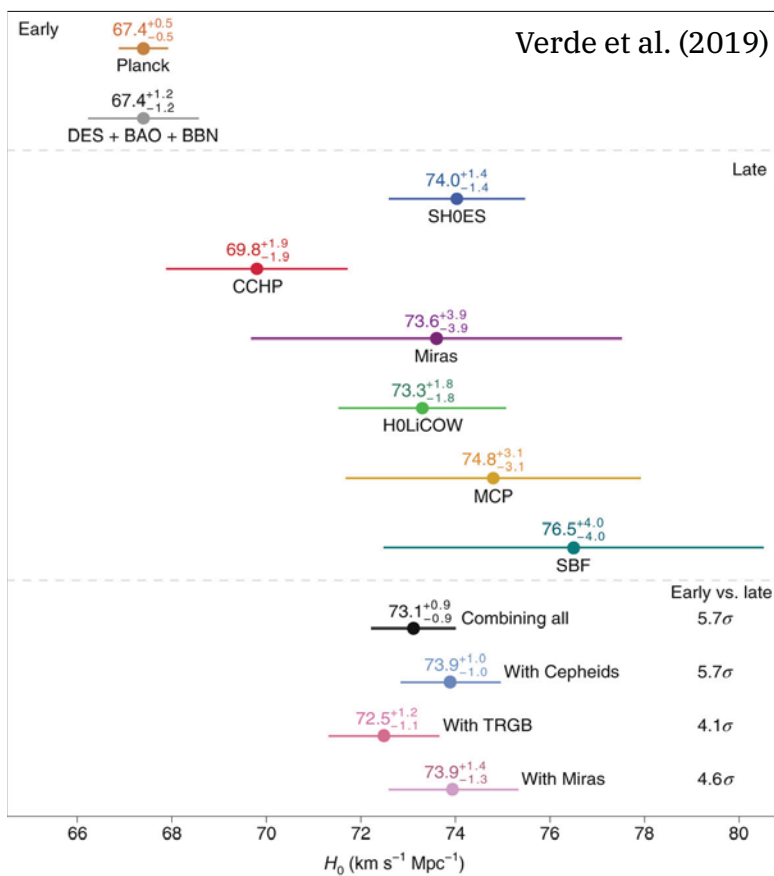




# H<sub>0</sub> tension now

- Planck (CMB)
- DES + BAO + BBN
- Variable stars + SN:  
SH0ES (Cepheid), Miras (Mira)
- TRGB + SN (CCHP)
- Strong lensing (H0LiCOW)
- Megamaser (MCP)
- Surface-brightness fluc. (SBF)

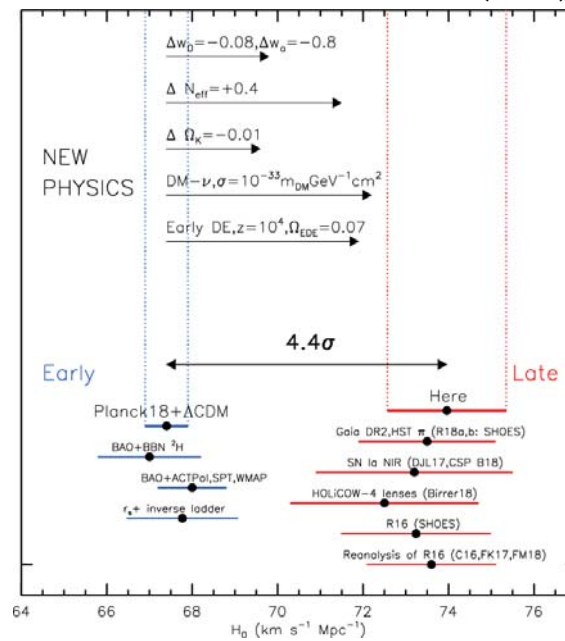
# “Sound Discordant”



- It is the discrepancy between
  - **Late:**  
Standard distance ladder
  - **Early:**  
Cosmological sound horizon  
(at photon/baryon decoupling)  
in  $\Lambda$ CDM model

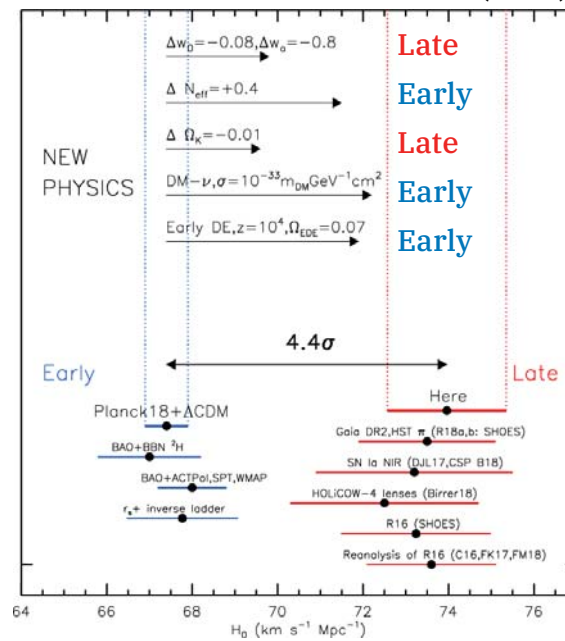
# Possible solutions

Riess et al. (2019)

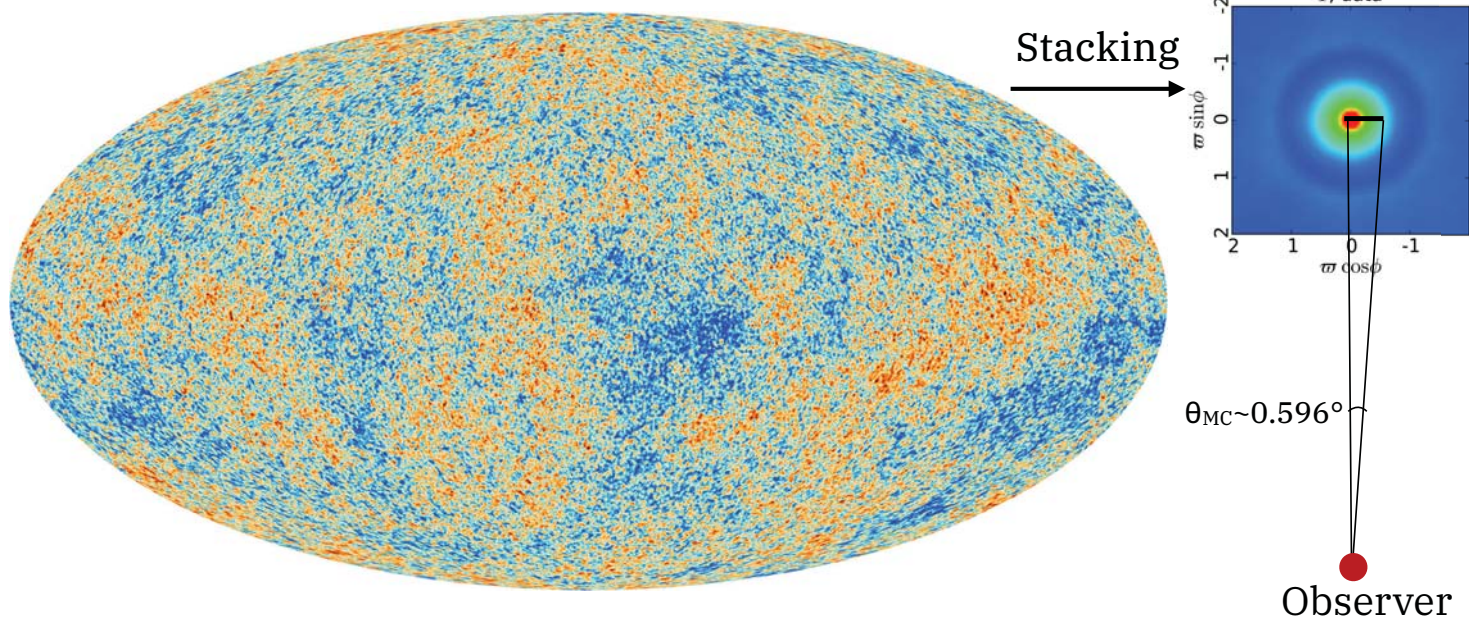


# Possible solutions

Riess et al. (2019)



# Acoustic scale at $\theta \sim 0.6^\circ$



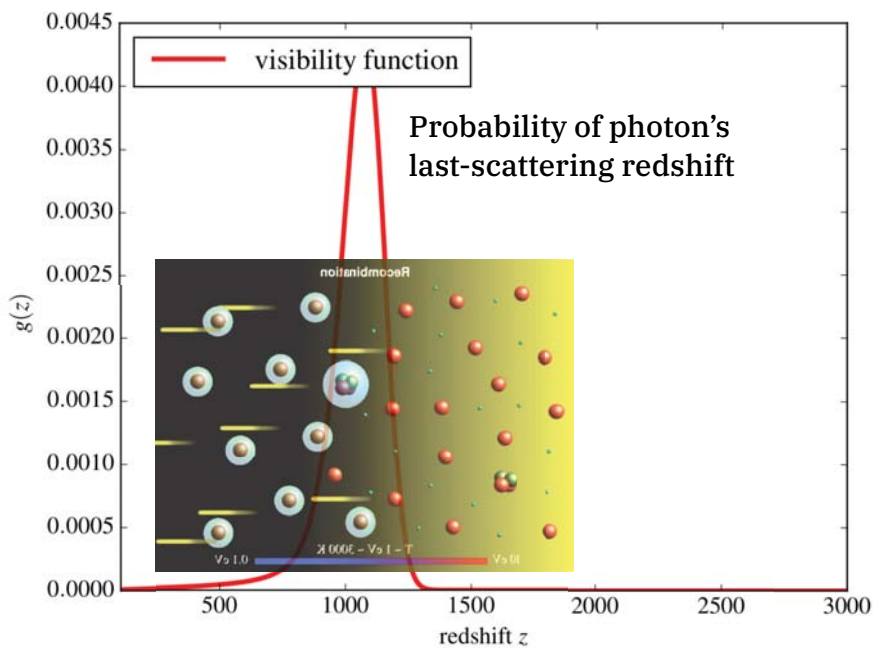
# Physics of acoustic scale

- ***Acoustic oscillation***: Tightly coupled baryon-photon plasma evolves as the pressure wave in the external gravitational field provided by dark matter
- The comoving sound horizon scale is given as

$$r_s = \int_0^{t_{\text{dec}}} c_s(t) \frac{dt}{a(t)} = \int_0^{a_{\text{dec}}} c_s(a) \frac{da}{a^2 H(a)} \quad c_s = \frac{c}{\sqrt{3(1 + 3\bar{\rho}_b/4\bar{\rho}_\gamma)}}$$
$$3H^2 = 8\pi G (\bar{\rho}_r + \bar{\rho}_m)$$



# Decoupling epoch



- The decoupling epoch ( $a_{\text{dec}}$ ) also depends on
  - **baryon density:**  
how many hydrogen to break
  - **matter density:**  
how fast the photons loose energy

# Calculating acoustic scale

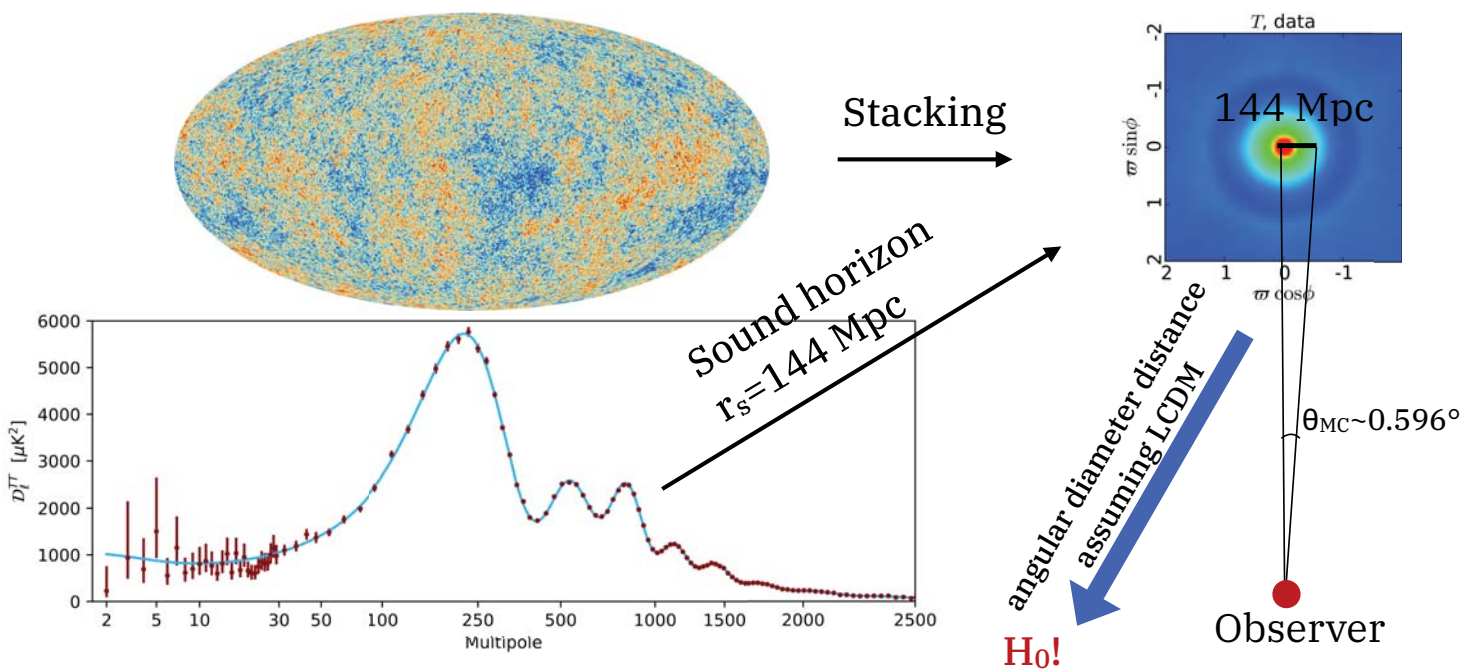
- Given  $\rho_m, \rho_b, \rho_\gamma, \rho_\nu$ , we can determine the acoustic scale!
  - $\rho_m, \rho_b$ : from the relative heights of CMB power spectrum
  - $\rho_\gamma$ : from  $T_{\text{cmb}}$  (CMB is very good black body)
  - $\rho_\nu$ : from  $N_{\text{eff}}$  ( $T_\nu = 0.714 T_{\text{cmb}}$ , and neutrinos are fermions)
  - **Note:  $r_s$  is independent from  $H_0$ !**

$$r_s = \int_0^{t_{\text{dec}}} c_s(t) \frac{dt}{a(t)} = \int_0^{a_{\text{dec}}} c_s(a) \frac{da}{a^2 H(a)}$$

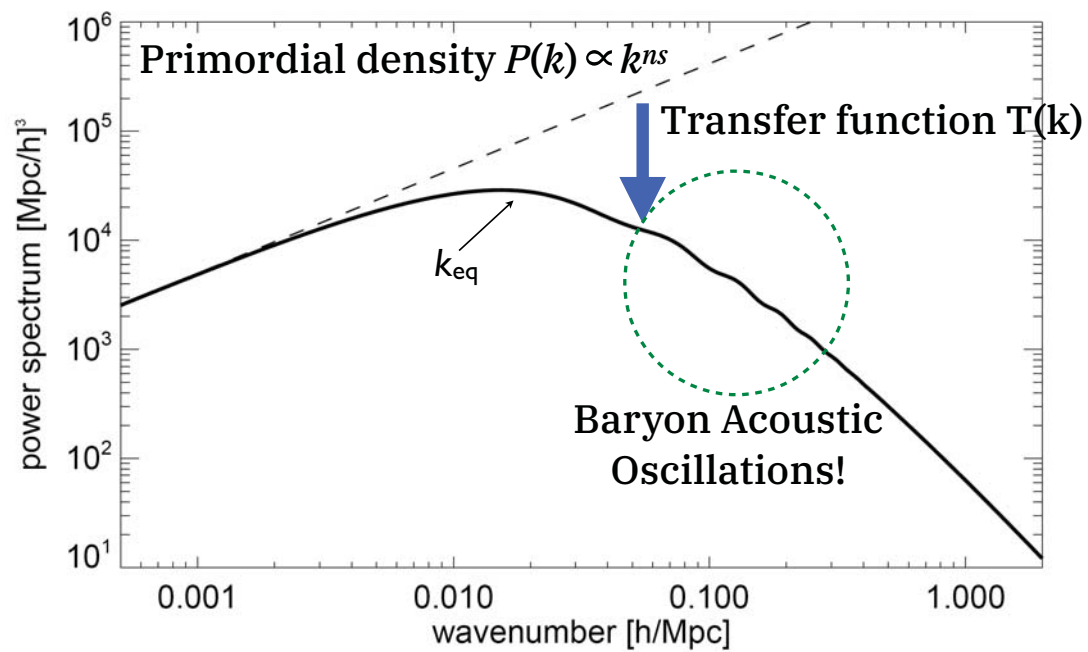
$$c_s = \frac{c}{\sqrt{3(1 + 3\bar{\rho}_b/4\bar{\rho}_\gamma)}}$$

$$3H^2 = 8\pi G (\bar{\rho}_r + \bar{\rho}_m)$$

# CMB power spectrum



# The BAO in the galaxy $P(k)$



# Dark energy with BAO

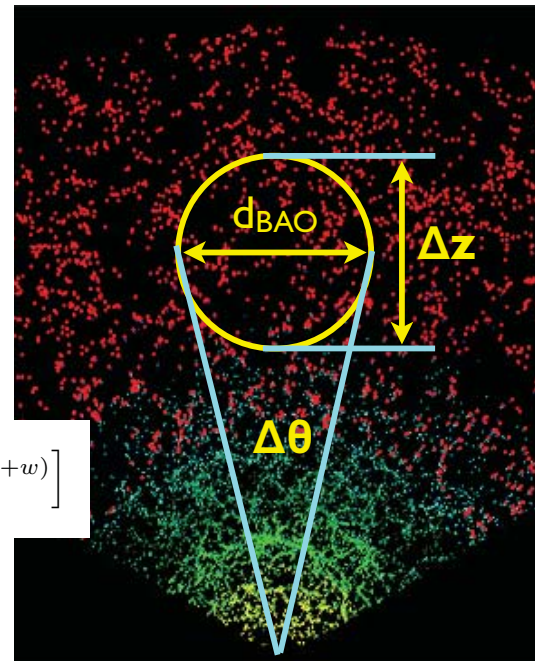
- $d_{\text{BAO}}$  is given by CMB, slightly larger than  $r_s$ .
- We can measure the angular diameter distance,  $d_A(z)$  and Hubble parameter,  $H(z)$ :

$$d_{\text{BAO}} = d_A(z) \Delta\theta = c \Delta z / H(z)$$

- $d_A(z)$ ,  $H(z)$  depend on  $H_0$  (assuming  $\Lambda$ CDM)!

$$H^2(z) = H_0^2 \left[ \Omega_m (1+z)^3 + \Omega_K (1+z)^2 + \Omega_{\text{DE}} (1+z)^{3(1+w)} \right]$$

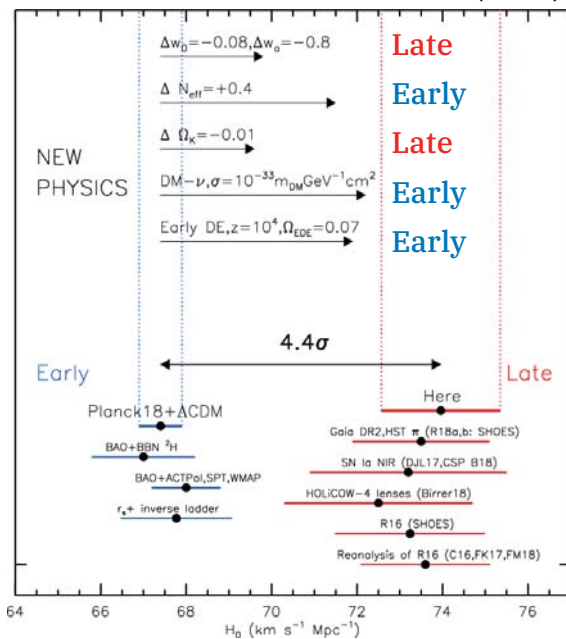
$$d_A(z) = \frac{\chi(z)}{1+z} \left[ 1 - \frac{k}{6} \frac{\chi^2(z)}{R^2} \right] \quad \chi(z) = c \int \frac{dz}{H(z)}$$



Early time

# Mission $H_0$ : reduce $r_s$ by 9%!

Riess et al. (2019)



- Direct observable =  $\theta \sim 0.6^\circ = r_s / d_A(a_{\text{dec}}) \sim H_0 r_s$ .
- If somehow we over-estimate for  $r_s$  by 9%, CMB measurement of  $H_0$  would be lower than the true value by 9%.
- How? Faster expansion at early time:
  - Increase  $N_{\text{eff}}$
  - Add exotica (early DE) for that job
- But, CMB does not allow full 9%!

# Can we confirm/rule out?

- **Yes**, if we have another distance in the early universe!
- Where do we have that distance?

In the *B-mode polarization from primordial gravitational waves!*

$$r_s = \int_0^{t_{\text{dec}}} c_s(t) \frac{dt}{a(t)} = \int_0^{a_{\text{dec}}} c_s(a) \frac{da}{a^2 H(a)} \quad c_s = \frac{c}{\sqrt{3(1 + 3\bar{\rho}_b/4\bar{\rho}_\gamma)}}$$

$$r_t = \int_0^{t_{\text{dec}}} c \frac{dt}{a(t)} = \int_0^{a_{\text{dec}}} c \frac{da}{a^2 H(a)}$$

$$3H^2 = 8\pi G (\bar{\rho}_r + \bar{\rho}_m)$$



# Gravitational Waves (GW)

- are the traceless and transverse (tensor) components of the metric perturbations: [with Einstein convention, Greeks=0-4, Latin=1-3]

$$ds^2 = a^2(\eta) \left[ -d\eta^2 + \{ \delta_{ij} + h_{ij}(\eta, \boldsymbol{x}) \} dx^i dx^j \right]$$

$$\text{Traceless : } \text{Tr}[h_{ij}] = h^i_i = g^{ij} h_{ij} = 0$$

$$\text{Transverse : } \nabla_i h_{ij} = 0$$

- There are 6 (symmetric 3-by-3 matrix) - 3 (transverse) - 1 (traceless) = 2 degrees of freedom ( $h_{\times}, h_{+}$ )

# Primordial GW (PGW)

- de Sitter spacetime generates stochastic gravitational waves with amplitude of (here,  $m_{\text{pl}} = \sqrt{G_N}$ ):

$$\Delta_h^2(k) = \frac{k^3 P_T(k)}{2\pi^2} = \frac{64\pi}{m_{\text{pl}}^2} \left( \frac{H}{2\pi} \right)^2 \Big|_{k=aH}$$

+ Friedmann equation:  $3H^2 \sim 8\pi G\rho$

- ***PGW = energy scale*** of inflation:  $E \sim (r/0.01)^{1/4} 10^{16} \text{GeV}$ !
- ***PGW = expansion rate*** during inflation: can prove inflation!

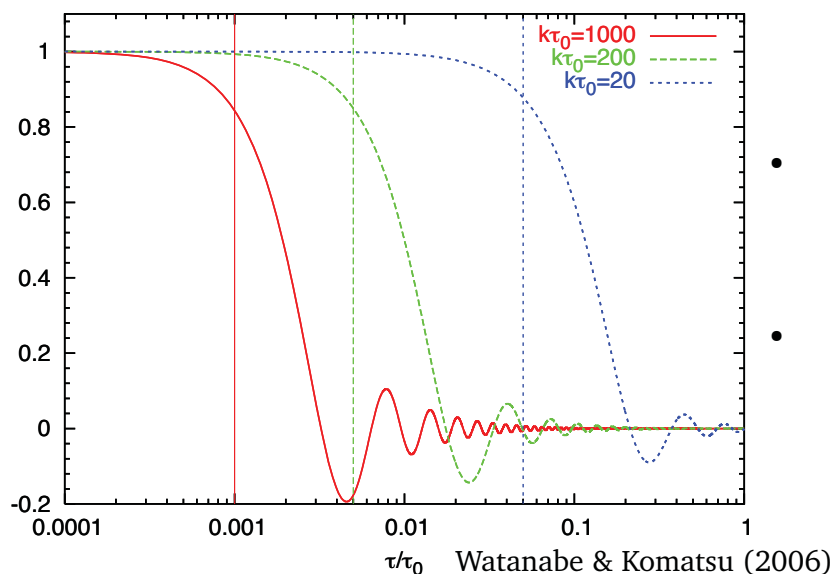
# Evolution of GW

- Evolution of GW amplitudes ( $h_{\times}$ ,  $h_{+}$ ) is governed by Klein-Gordon equation sourced by anisotropic stress  $\Pi_p$   
( $\mathcal{H} = a'/a$  and  $' = d/d\eta$ ):

$$-h_{ij;\nu}{}^{;\nu} = h_p''(\mathbf{k}) + \underbrace{2\mathcal{H}h_p'(\mathbf{k})}_{\text{Hubble damping}} + k^2 h_p(\mathbf{k}) = 16\pi G a^2 \Pi_p(\mathbf{k})$$

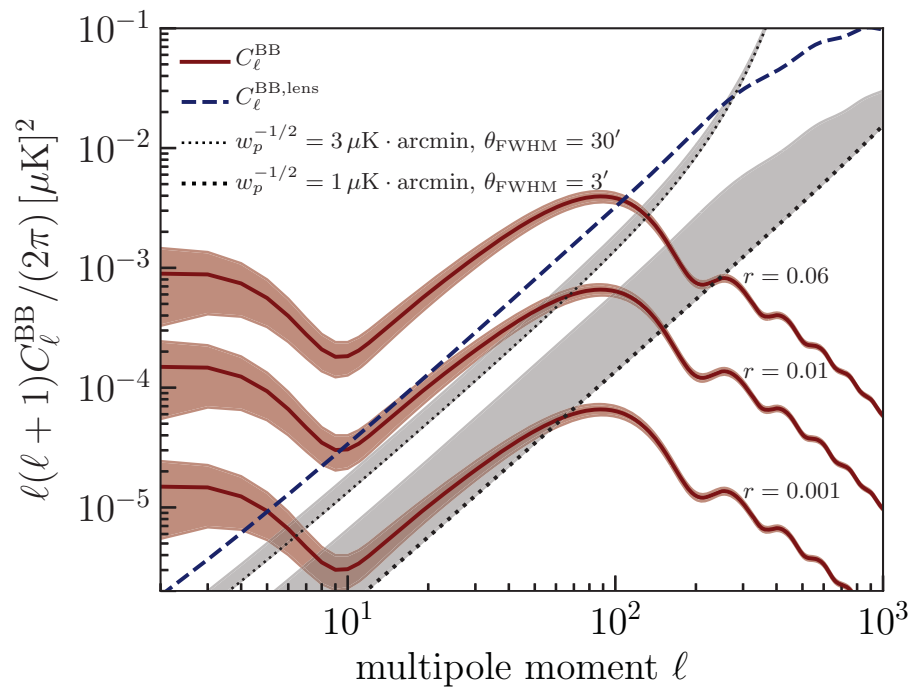
# Evolution of PGW w/o sources

$$-\square h_{ij} = h_p''(\mathbf{k}) + 2\mathcal{H}h_p'(\mathbf{k}) + k^2 h_p(\mathbf{k}) = 0$$

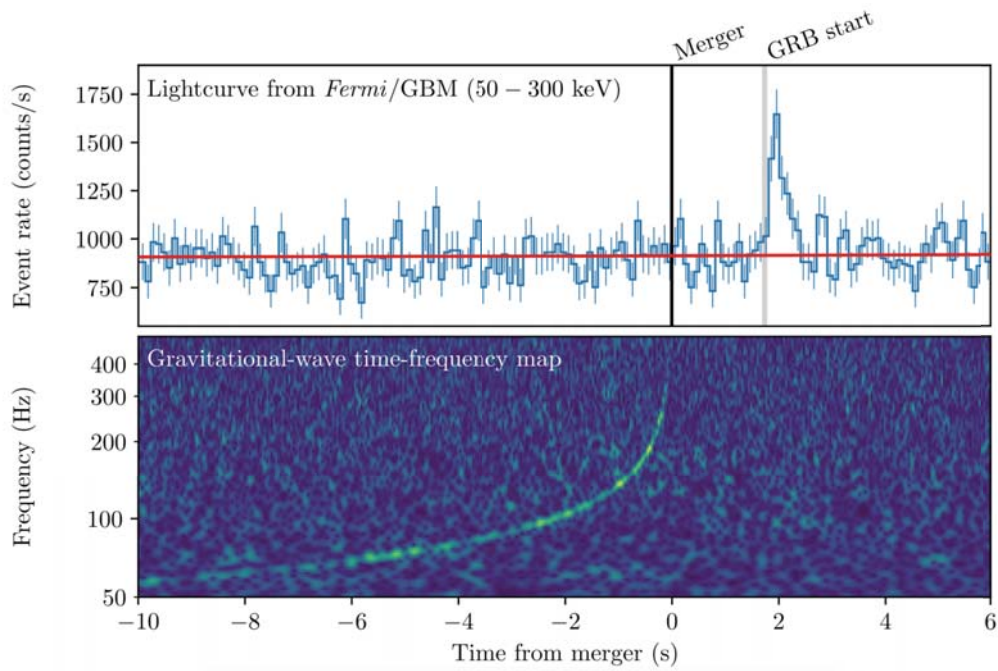


- **PGW** stays constant outside of horizon, but **decays** once the mode enters the horizon.
- *cf.* **scalar perturbations grow** inside of horizon.

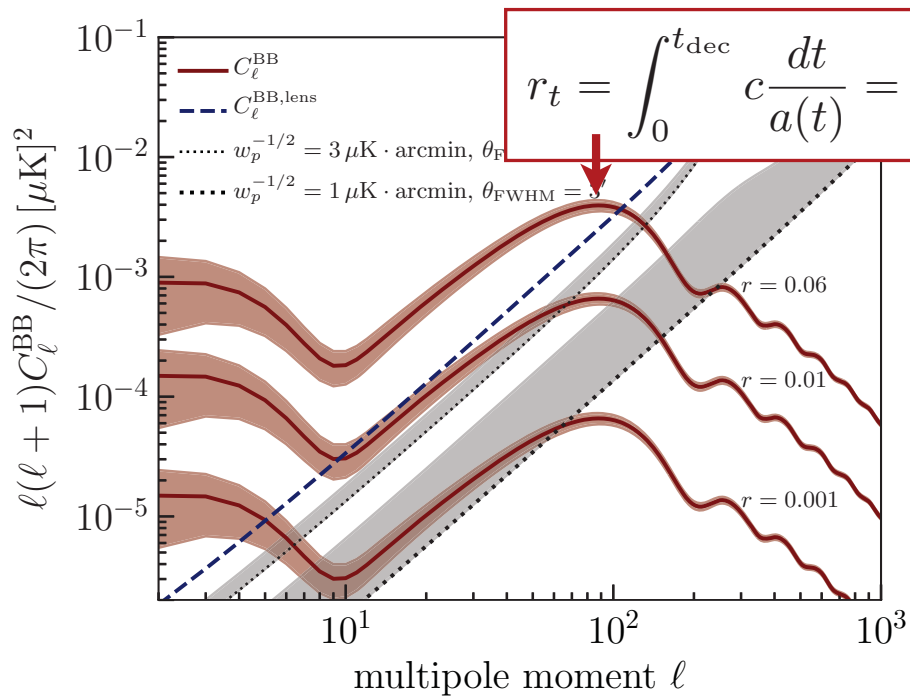
# B-mode power spectrum



# GW170817 and GRB 170817A



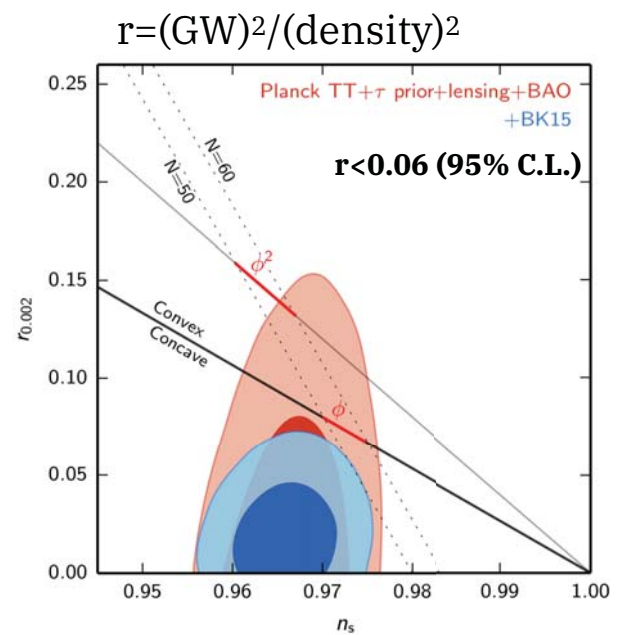
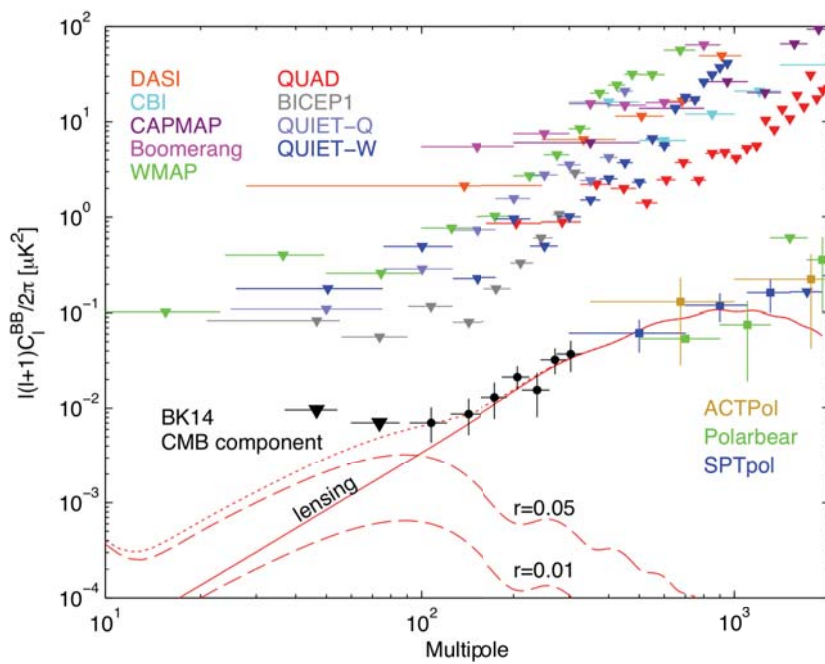
# Turn-over scale $r_t$



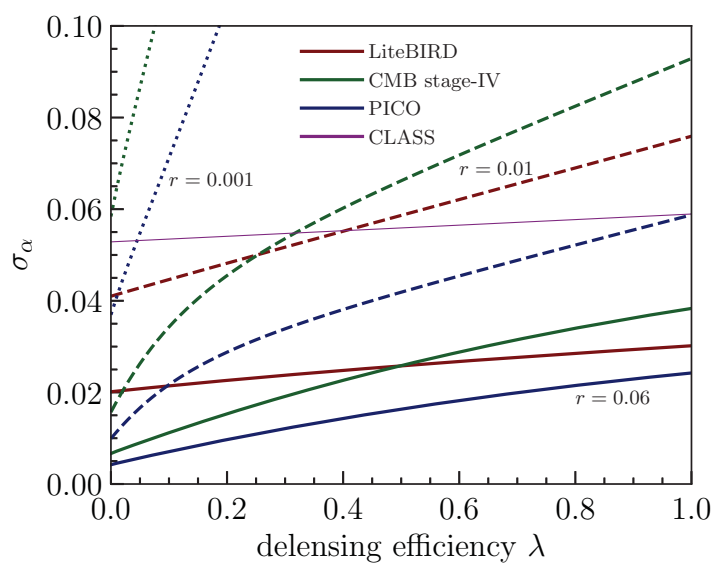
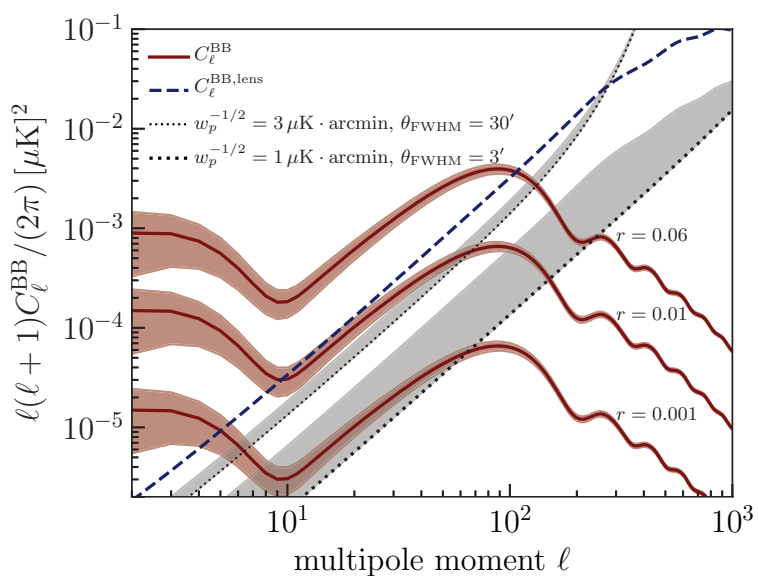


BICEP/Keck Collaboration (2016, 2018)

# B-mode polarization, status



# We can measure $r_t$ , if $r > 0.001$ !

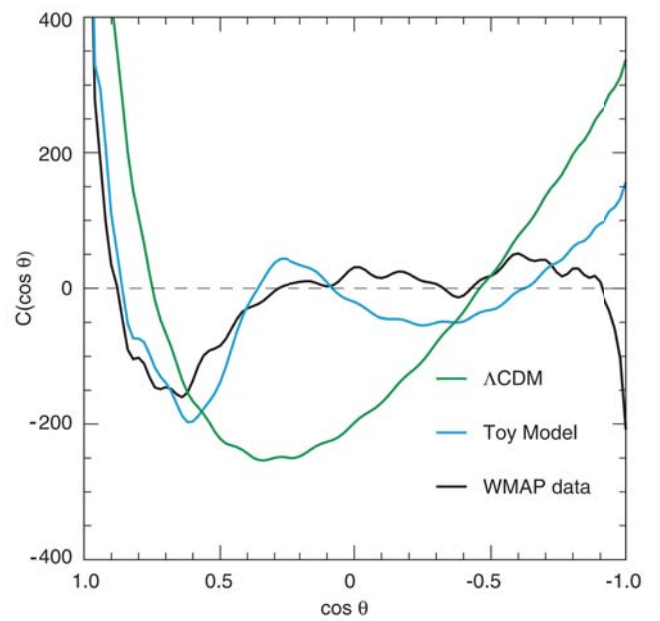
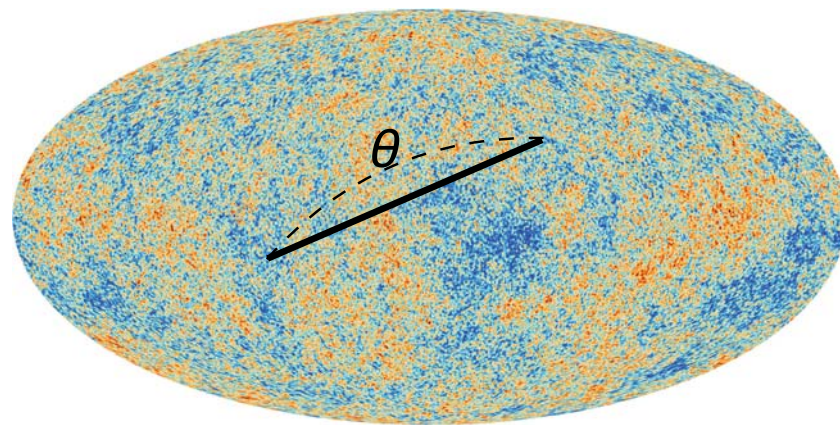


# Three puzzles in the CMB

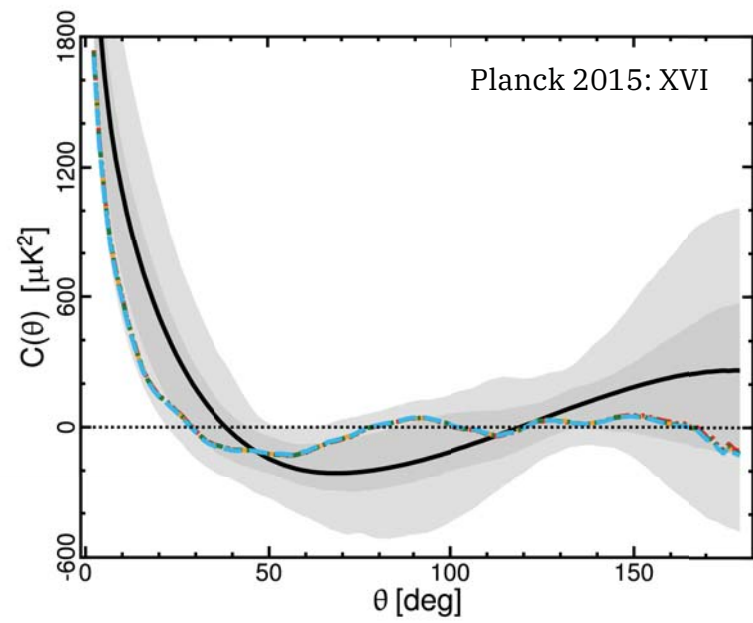
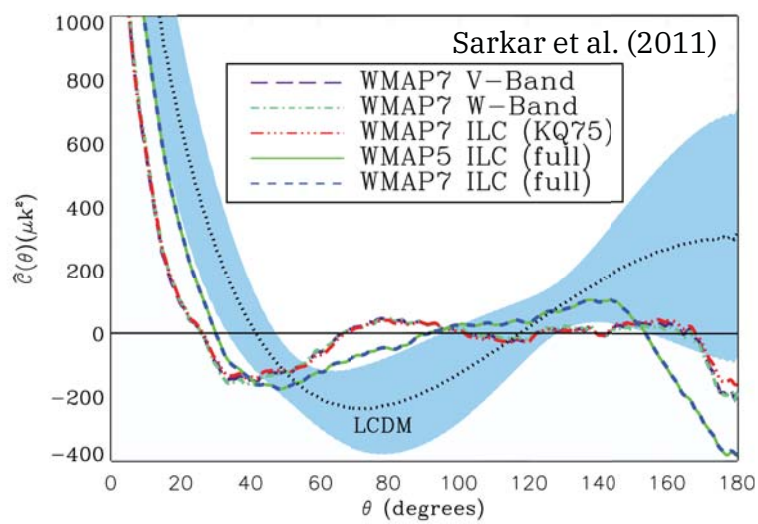
- Hubble tension
- Lack of CMB clustering on large angular scales
- “Crisis for cosmology”:  $A_L$  (lensing amplitude) anomaly

WMAP1, Spergel et al. (2003)

# “Intriguing discrepancy”



# $C(\theta)$ after WMAP1



# The $S_{1/2}$ parameter

$$S_{1/2} \equiv \int_{-1}^{1/2} d(\cos \theta) [C(\theta)]^2$$

**Table 11.** Values for the  $S_{1/2}^{XY} \equiv S^{XY}(60^\circ, 180^\circ)$  statistic (in units of  $\mu\text{K}^4$ ) for the *Planck* 2018 data with resolution parameter  $N_{\text{side}} = 64$ .

Statistic	$S_{1/2}^{XY} [\mu\text{K}^4]$			
	Comm.	NILC	SEVEM	SMICA
$TT$ . . . . .	1209.2	1156.6	1146.2	1142.4
$Q_r Q_r$ . . . . .	$8.3 \times 10^{-5}$	$8.6 \times 10^{-5}$	0.00019	$4.9 \times 10^{-5}$
$U_r U_r$ . . . . .	$3.9 \times 10^{-5}$	$4.8 \times 10^{-5}$	$5.9 \times 10^{-5}$	$1.6 \times 10^{-5}$
$TQ_r$ . . . . .	0.26	0.13	0.45	0.13
$TU_r$ . . . . .	0.065	0.044	0.2	0.081
$Q_r U_r$ . . . . .	$6.4 \times 10^{-6}$	$3.6 \times 10^{-5}$	$7.1 \times 10^{-6}$	$2.1 \times 10^{-6}$

**Table 12.** Probabilities of obtaining values for the  $S_{1/2}^{XY}$  statistic for the *Planck* fiducial  $\Lambda\text{CDM}$  model at least as large as the observed values of the statistic for the *Planck* 2018 CMB maps with resolution parameter  $N_{\text{side}} = 64$ , estimated using the Commander, NILC, SEVEM, and SMICA maps.

Statistic	Probability [%]			
	Comm.	NILC	SEVEM	SMICA
$TT$ . . . . .	>99.9	>99.9	>99.9	>99.9
$TT$ (no quadr.) . . .	96.0	96.1	96.1	96.2
$Q_r Q_r$ . . . . .	42.8	50.5	30.3	57.0
$U_r U_r$ . . . . .	74.5	71.7	68.9	89.0
$TQ_r$ . . . . .	83.5	94.0	74.6	94.8
$TU_r$ . . . . .	94.5	97.8	79.1	88.6
$Q_r U_r$ . . . . .	88.8	59.7	94.4	97.7

**Notes.** The second row shows results for each temperature map after removing the corresponding best-fit quadrupole. In this table high probabilities would correspond to anomalously low  $S_{1/2}^{XY}$  values.

# Three puzzles in the CMB

- Hubble tension
- Lack of CMB clustering on large angular scales
- “Crisis for cosmology”:  $A_L$  (lensing amplitude) anomaly

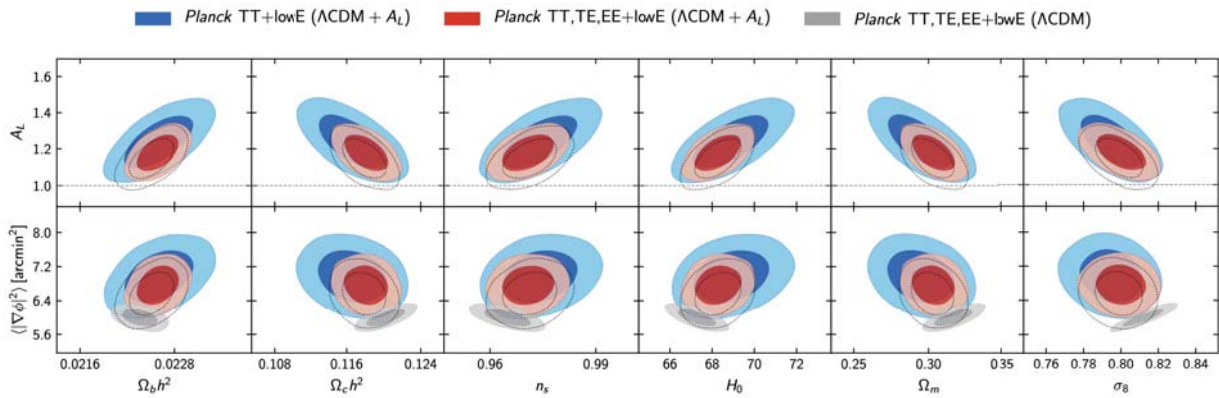
Di Valentino, Melchiorri, Silk

“Planck evidence for a closed Universe and a possible crisis for cosmology”

Nature Astronomy (2019), arXiv:1911.02087



$$A_L = (\text{lensing amplitude}) / (\text{best-fitting } \Lambda\text{CDM})$$

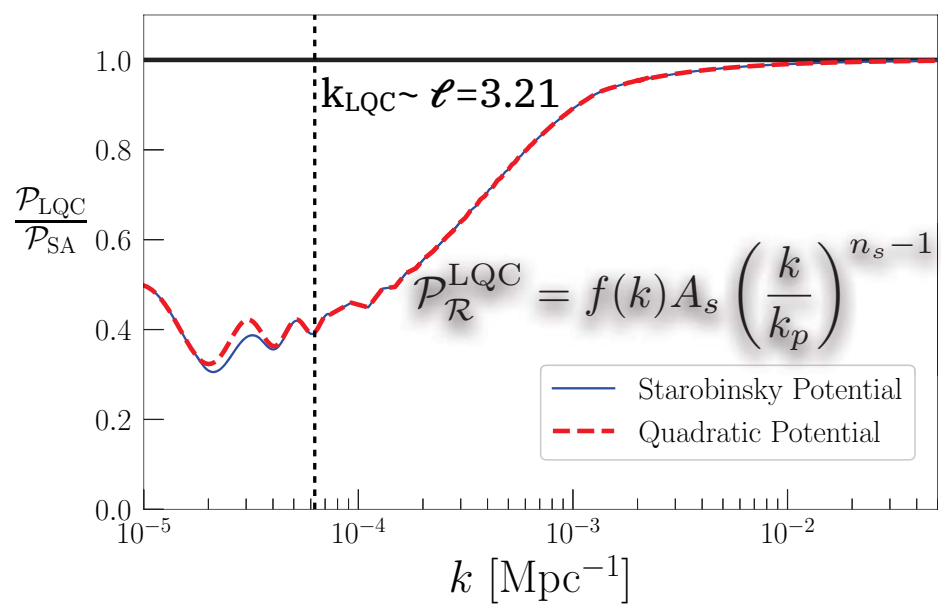


**Fig. 25.** Marginalized 68 % and 95 % parameter constraint contours when adding  $A_L$  as a single-parameter extension to the base- $\Lambda$ CDM model, with (red) and without (blue) small-scale polarization, compared to the constraints in the base- $\Lambda$ CDM model (grey). The dashed contours show equivalent results for *Planck* TT,TE,EE+lowE when using the CamSpec likelihood, which gives results with  $A_L$  nearer unity and with slightly larger errors. The second row of subplots show, on the left axis, the predicted lensing deflection angle variance (from lensing multipoles  $2 \leq L \leq 2000$ ), which is a measure of the amount of actual lensing: the TT,TE,EE+lowE likelihood prefers about 10 % more actual lensing power (associated with lensing smoothing), but in the (unphysical) varying- $A_L$  case this can be achieved using cosmological parameters that predict less lensing than in  $\Lambda$ CDM but substantially larger  $A_L$ , giving a preference for  $A_L \approx 1.2$ .

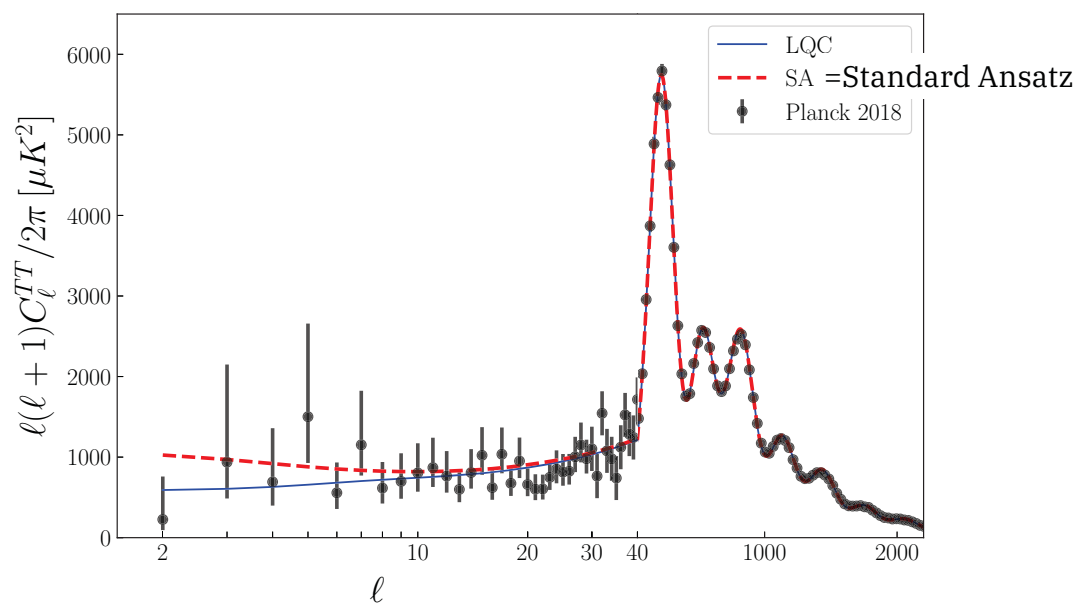
# Initial $P(k)$ from LQC

- Loop-Quantum Cosmology provides an initial condition of inflation
- Quantum correction yields the “bounce” at which  $R_{\text{max}} \sim 62$  (Planck unit).
- The “LQC scale” is given by  $k_{\text{LQC}} = (R_{\text{max}}/6)^{1/2} \sim 3.21$  (Planck unit).
- Fourier modes  $k < k_{\text{LQC}}$  are not in the Bunch-Davies vacuum; that leads to the **large-scale suppression**.
- Equating the CMB horizon size with the “unit spacetime quanta” at the bounce, we can equate  $k_{\text{LQC}}^{(\text{co-moving})} \sim 3.6 \times 10^{-4} \text{ Mpc}^{-1}$ .

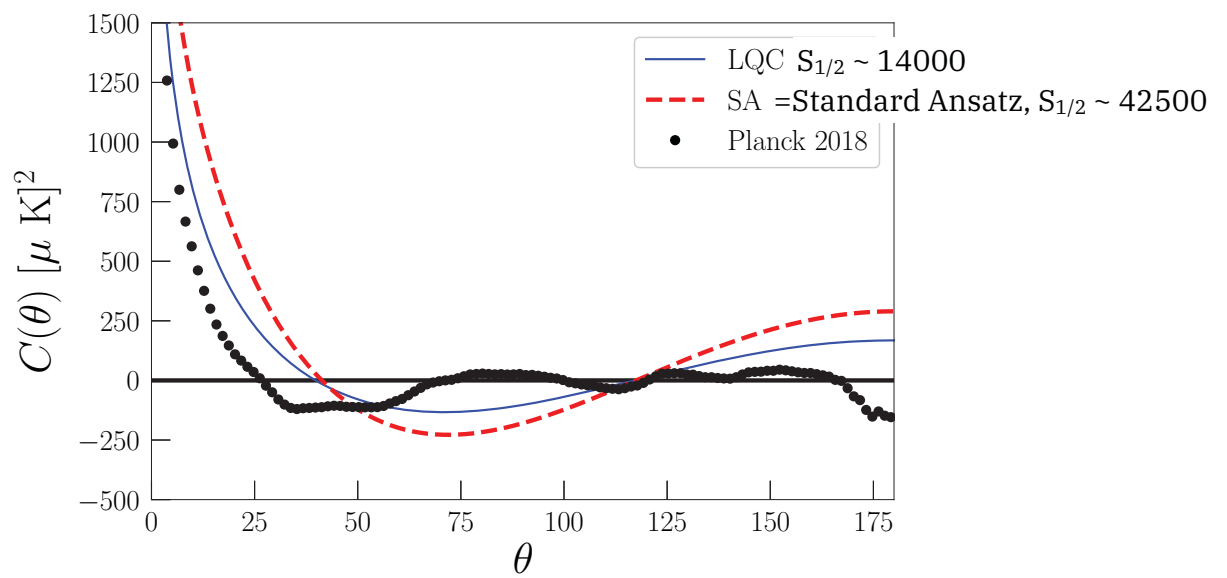
# Initial P(k) from LQC

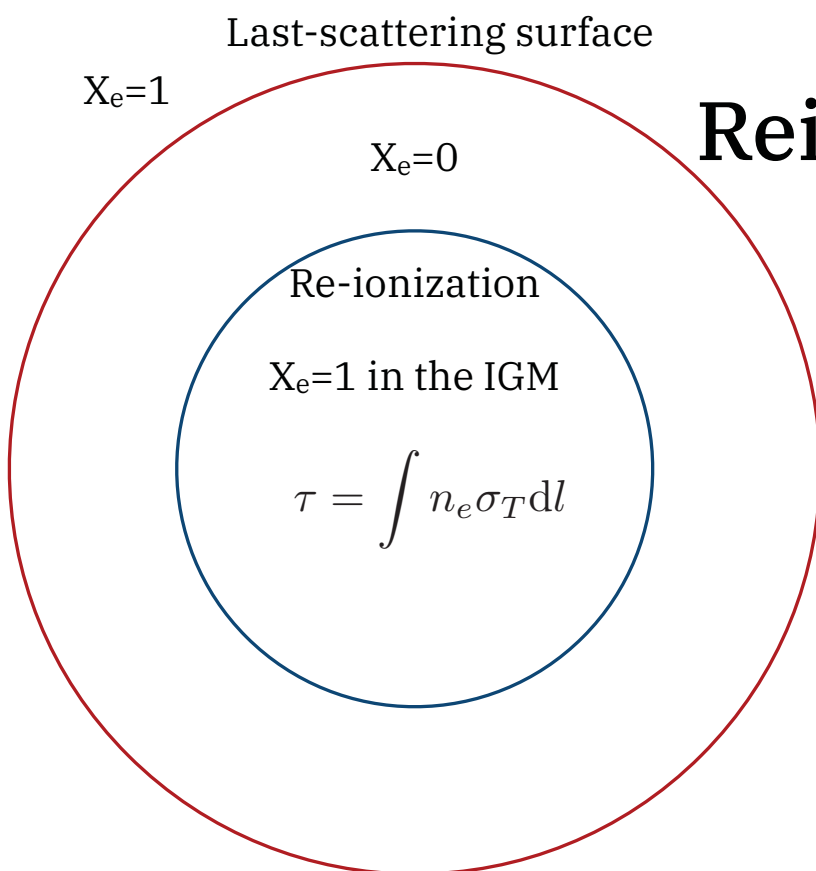


# CMB power spectrum with LQC



# $C(\theta)$ with LQC





# Reionization and CMB

- Reionization Optical depth  $\sim 0.05$  (Planck): 5% scatter
- Damping the temperature anisotropies on small scales

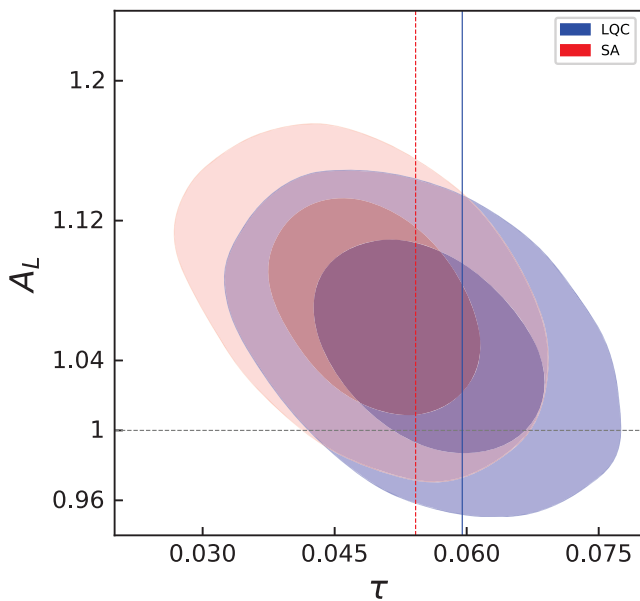
$$(T + \Delta T)^{\text{obs}} = (T + \Delta T)^{\text{primordial}} e^{-\tau} + T (1 - e^{-\tau})$$

$$(\Delta T)^{\text{obs}} = (\Delta T)^{\text{primordial}} e^{-\tau}$$

(For  $\ell > \ell_{\text{reionization}} \sim 40$ )

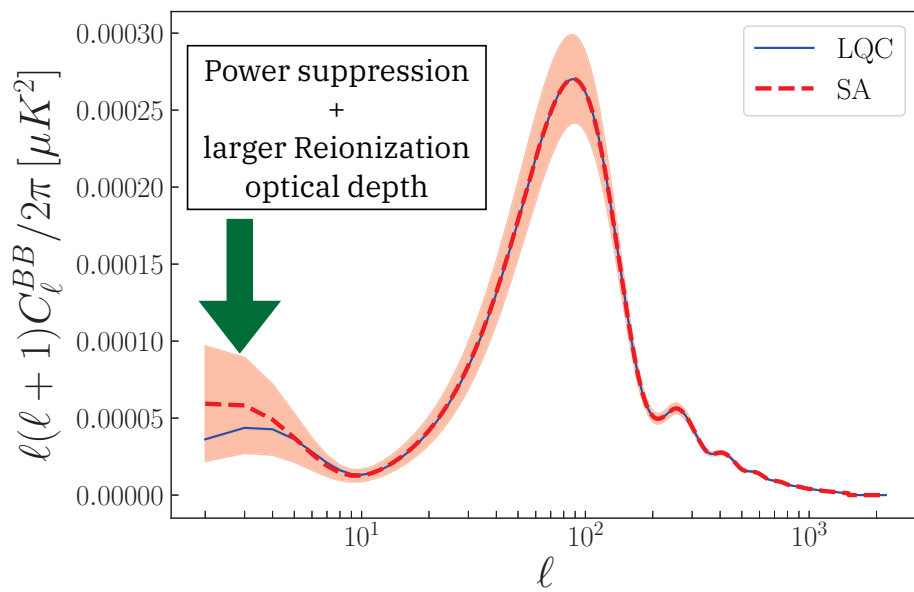
- Polarization on large scales.

# LQC and $A_L$



- Interplay between large and small scales
- Small scale anisotropy measures =  $A_s e^{-2\tau}$
- By increasing the optical depth, we increases the density fluctuation amplitude  $A_s$  in the CMB
- The ratio  $A_L = (\text{lensing amplitude})/A_s$  drops!
- All of them without screwing the large-scale  $C_\ell$  **thanks to the power suppression!**

# LQC prediction for $C_\ell^{BB}$





# Conclusion

- $C_\ell^{\text{BB}}$  can test the early-type resolution of the Hubble tension hypothesizing that Universe expanded with a faster rate prior to the decoupling time.
- $C_\ell^{\text{BB}}$  can test the LQC prediction that primordial power spectrum is suppressed on large-scales ( $k < 0.002 \text{ Mpc}^{-1}$ ).
- Resolving the Hubble tension may require first-principle measurements at low redshifts, such as standard siren from Gravitational Waves.
- Large-scale power suppression can also be probe with full-sky galaxy/21cm surveys in the future.