

# SPONTANEOUS LEPTOGENESIS IN HIGGS INFLATION



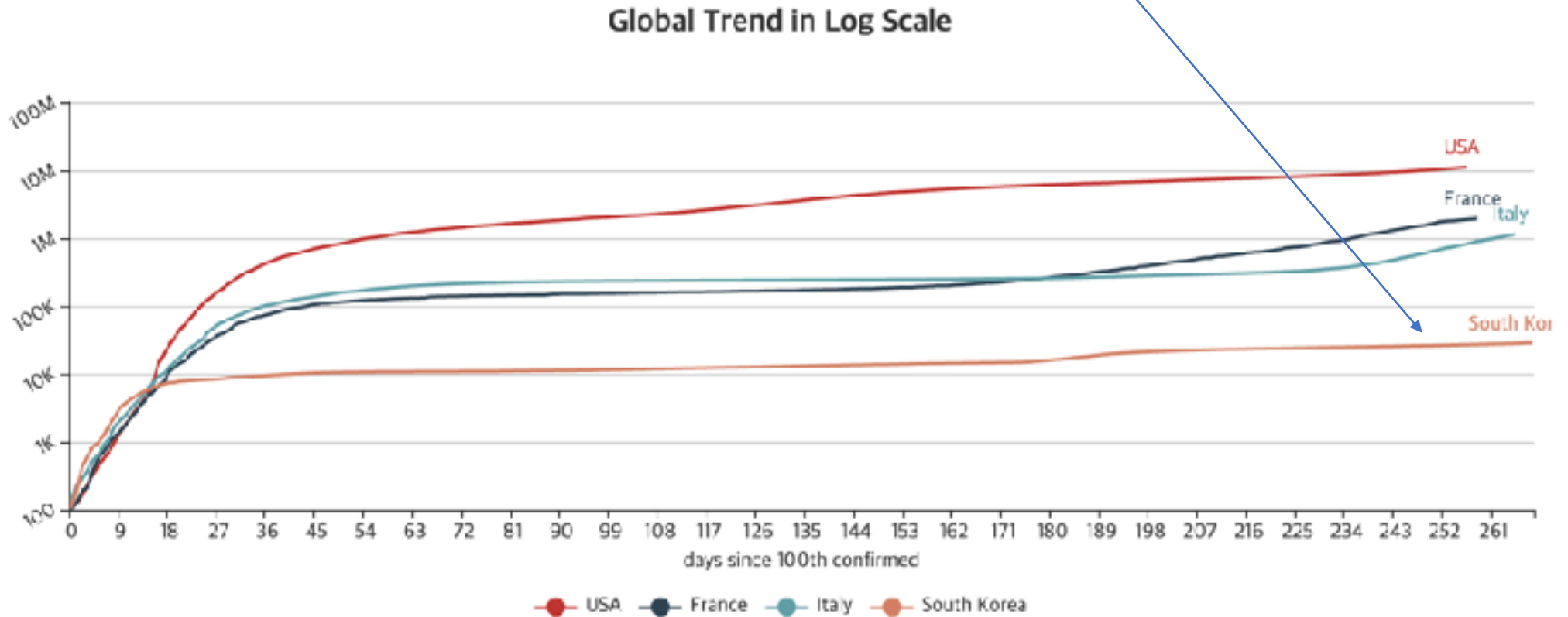
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based on **arXiv:2010.07563**

with Sung Mook Lee (Yonsei), Kin-ya Oda (Osaka)



If something works well,  
there could be some good reasons behind



# 'Higgs' works well beyond the original expectation

- EW symmetry breaking
- Masses of elementary particles
- Successful inflation BEST fitting the data

Bezrukov, Shaposhnikov 0710.3755

Hamada, Kawai, Oda, SCP 1403.5043, 1408.4864 (Critical)

- Dark matter can be understood by Primordial Black Hole production

Cheong, Lee, SCP 1912.12032

- Baryon asymmetry of the universe ==> THIS TALK

Lee, Oda, SCP 2010.07563

# Content

- Review on Baryon Asymmetry, Higgs Inflation & Reheating
- Higher Dimensional Operators (Dim 5, Dim 6) for LNV & chemical potential for baryon-number
- Leptogenesis in Higgs inflation
- Conclusions

# Introduction

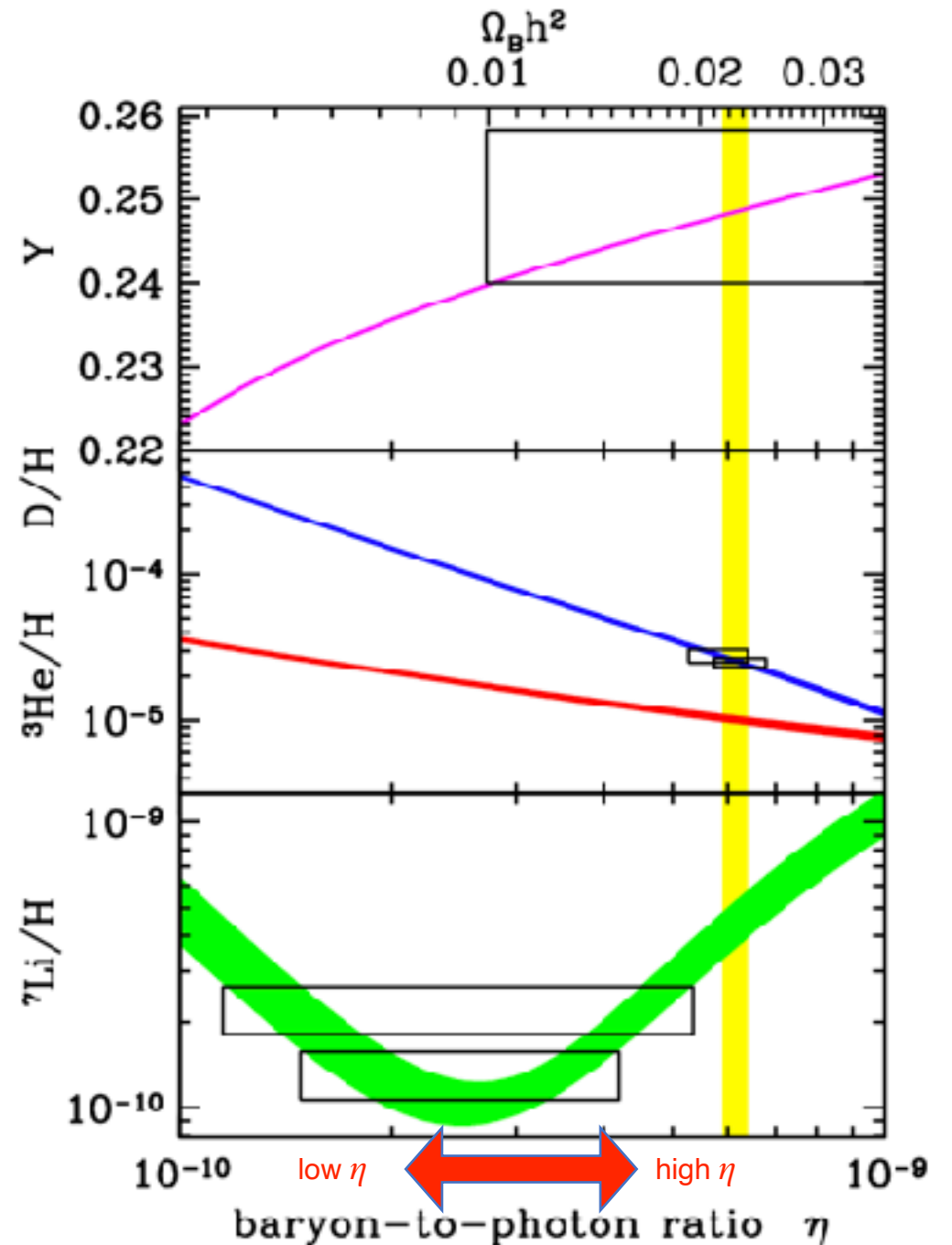
- We see baryons rather than anti-baryons in nature

$$\frac{\bar{p}}{p} \sim 10^{-4} \text{ in cosmic ray}$$

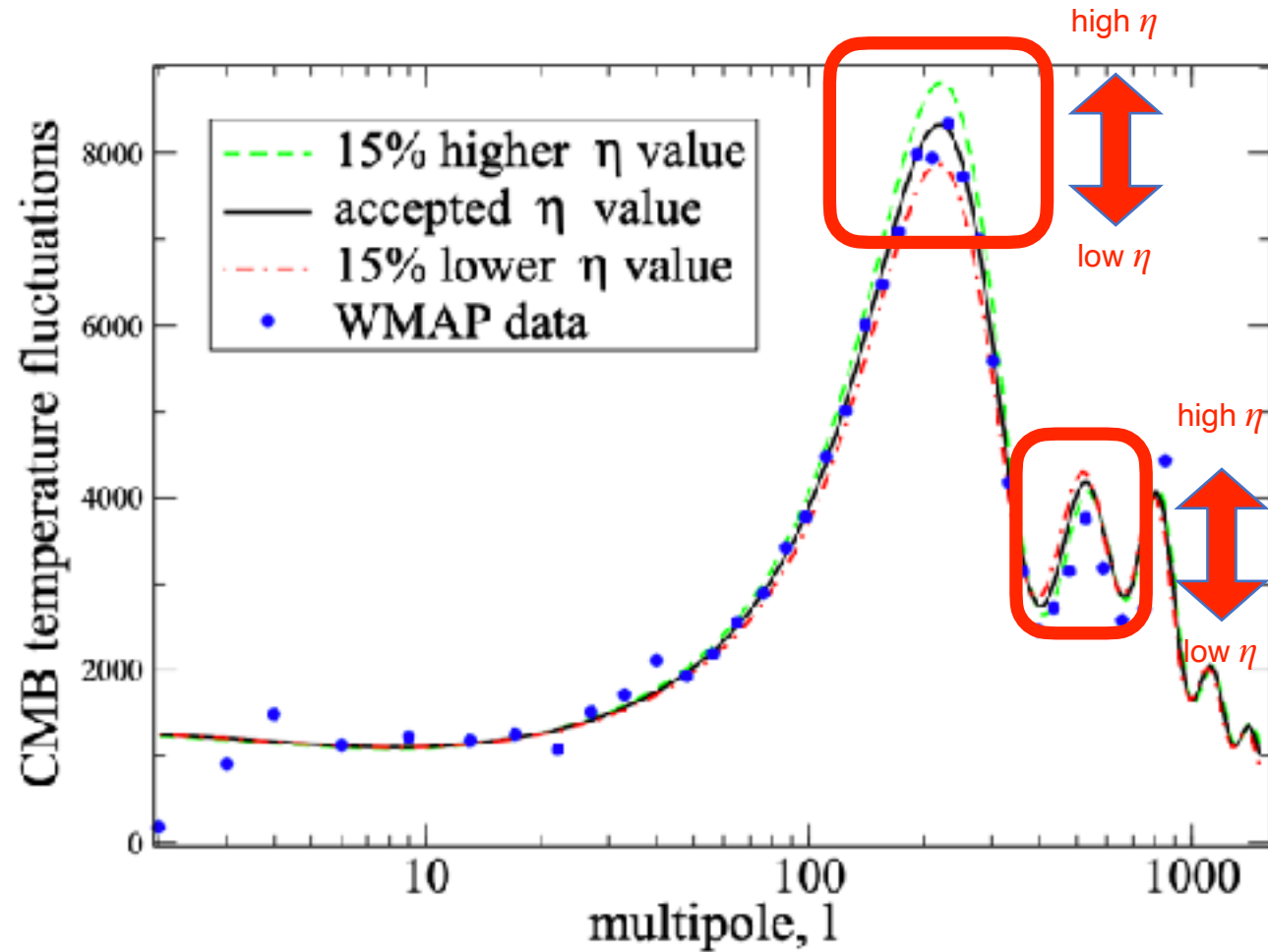
- Making  $e^+$ ,  $\bar{p}$  cost a lot at colliders
- Baryon asymmetry is well determined by BBN & CMB measurements

$$\eta \equiv \frac{n_B - n_{\bar{B}}}{n_\gamma} \sim 6 \times 10^{-10}$$

- $n_B$  : number density of Baryons
- $n_{\bar{B}}$  : number density of anti-Baryons
- $n_\gamma$  : number density of photons =  $\frac{\zeta(3)}{\pi^2} g_* T^3$ ,  
 $g_* = 2$  polarizations,  $\zeta(3) = 1.20\dots$

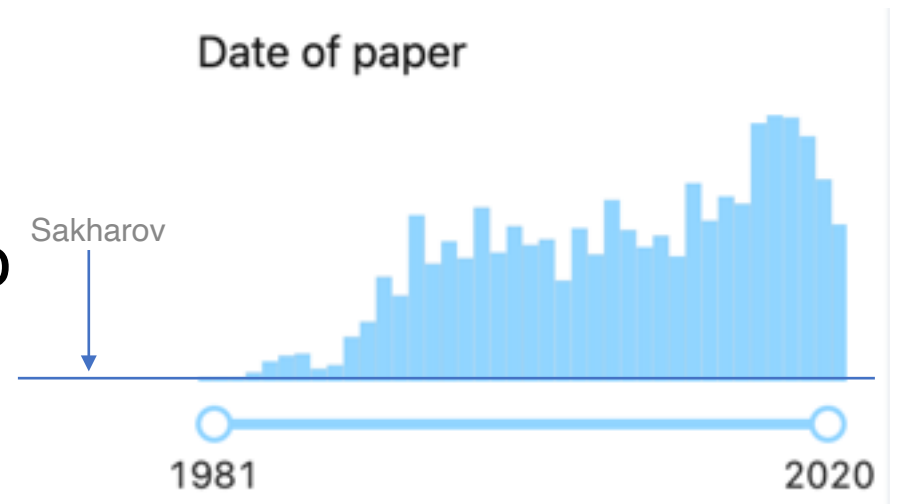


# Baryon asymmetry from CMB spectrum



# Questions

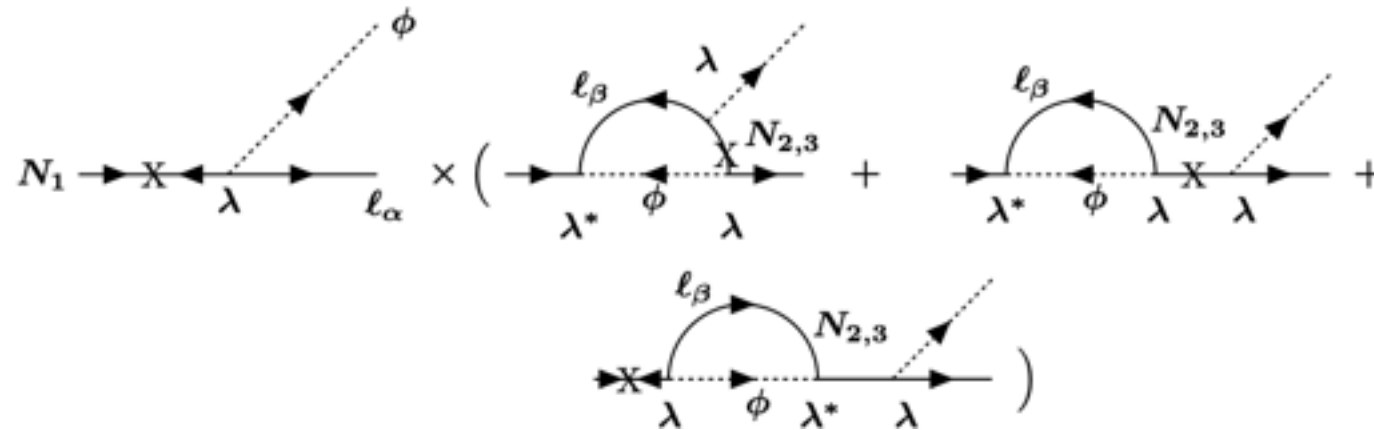
- B and anti-B are spatially separated? ==> no
- Is it generated before the inflation? ==> no
- **Why is it non-zero? ==> Baryogenesis**
- With exact CPT symmetry, **Sakharov's 3 conditions (1967)** are needed
  - B-violation, C & CP violation, out of thermal equilibrium
- Then enormous efforts have been made in 'Baryogenesis' ever since
- **Leptogenesis** is my personal favorite ...



# Leptogenesis

M. Fukugita, T. Yanagida (1986)

- Thanks to the sphaleron process active  $Q > EW$ , the generated lepton number can be converted into baryon number
- Lepton number can be generated in heavy Majorana Neutrino decay



- A beautiful idea but hardly tested :  $m_N \sim m_{\text{GUT}}$



# We claim

In Higgs inflation, **spontaneous Leptogenesis** can be still achieved with help from Weinberg operator (Dim-5) and chemical potential of lepton number (Dim-6) with no new particle

# Higgs Inflation

Non-minimal coupling

[F.L. Bezrukov et al. 0710.3755]

## Model

$$S_{J,\text{inf}} = \int d^4x \sqrt{-g_J} \left[ \frac{1}{2} \left( M_P^2 + \xi \phi_J^\dagger \phi_J \right) R_J - \frac{1}{2} |\partial_\mu \phi_J|^2 - V_J(\phi_J) \right] \quad V_J(\phi_J) = \frac{\lambda}{4} \phi_J^4$$

Weyl transformation

$$g_{\mu\nu} = \Omega(\phi_J)^2 g_{J\mu\nu} \quad \Omega(\phi_J)^2 \equiv 1 + \frac{\xi}{M_P^2} \phi_J^2$$

$$\psi_J \rightarrow \Omega^{\text{Dim}} \psi$$

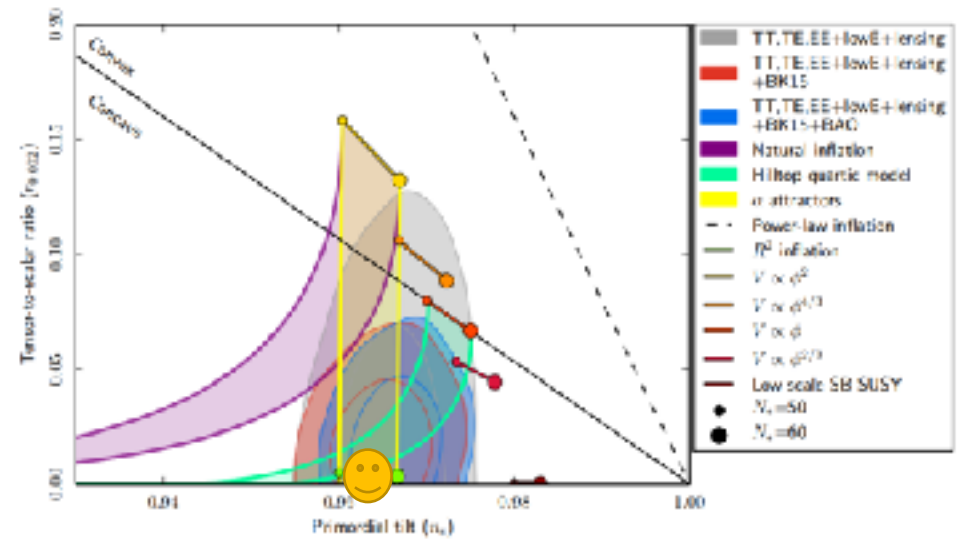
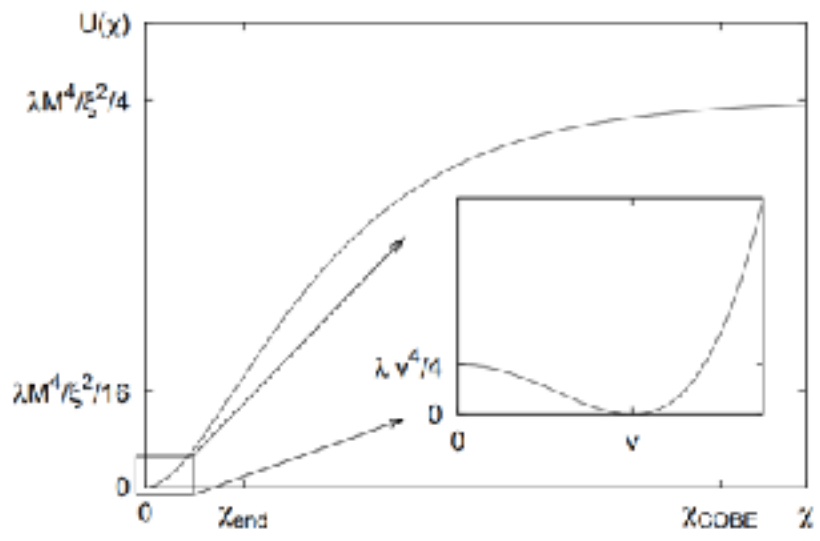
Dim : conformal dimension

3/2 : fermion

1 : boson

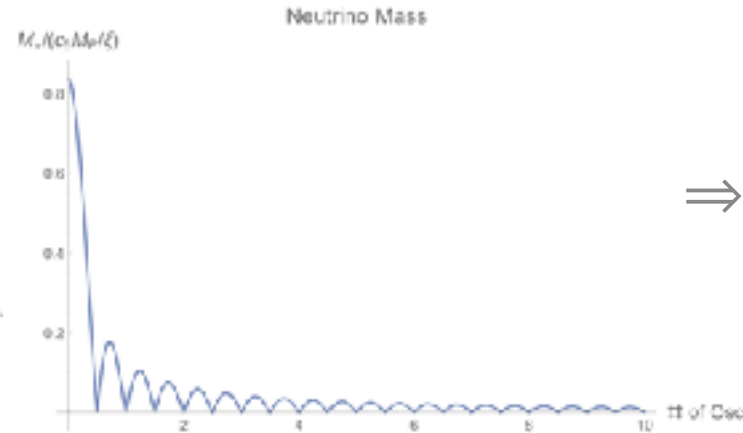
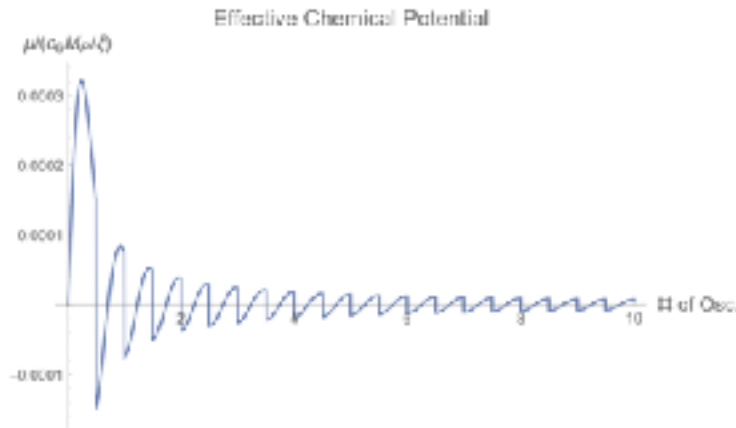
$$S_{E,\text{inf}} = \int d^4x \sqrt{-g} \left[ \frac{M_P^2}{2} R - \frac{1}{2} |\partial_\mu \phi|^2 - V(\phi) \right]$$

- Minimal (only candidate in SM) / Best-fit to Planck result



# Matter production in Higgs inflation

- Time Dependent Fermion Masses from  $\sqrt{g}yH\bar{\psi}\psi$  and  $g_{\mu\nu} \rightarrow \Omega^2 g_{\mu\nu}$
- Scaling behavior & dynamics of Higgs :  $m \rightarrow \frac{m}{\Omega(t)}$
- 'Change of mass' can be understood as change of vacuum  
==> **Bogoliubov transformation** ==> **Particle Production** (just as Hawking Radiation!)



⇒ Particle Production

# Higher Dimension Operators : Dim-5

- SM as EFT
- Dim-5 Operator : Weinberg Operator

$$\mathcal{L}_{\text{dim-5}} = \frac{c_5}{M_P} (\bar{L} \tilde{\Phi}) (\tilde{\Phi} L)^\dagger \quad \tilde{\Phi} \equiv i\sigma_2 \Phi^*$$

- Lepton Number Violation
- CP violation
- Possible Origin : Heavy Majorana Neutrino  $M_N \sim 10^{15} \text{ GeV}$ 
  - Note that the reheating temperature  $T_{\text{rch}} < 10^{15} \text{ GeV}$

# Higher Dimension Operators : Dim-6

- Dim-6 Operator [Pearce et al. 1410.0722, 1505.02461]

$$\mathcal{O}_6 = -\frac{c_6}{M_P^2} \Phi_J^\dagger \Phi_J \partial_\mu j_L^\mu = \frac{c_6}{M_P^2} (\partial_\mu \phi_J^2) j_L^\mu = \frac{c_6}{M_P^2} (\partial_t \phi_J^2) j_L^0$$

- Coherent Field spontaneously breaks CPT
- Chemical Potential of lepton number  
==> Energy costs differently from anti-lepton to lepton
- Dominantly acting ONLY at reheating when time derivative becomes sizable  
(cf) During inflation, inflaton slowly rolling

**Neutrino masses** are derived from the Weinberg operator

$$\sqrt{-g_J} \frac{c_5}{M_P} \phi_J^2 \psi_J \psi_J = \sqrt{-g} \frac{c_5}{M_P} \frac{\phi_J^2}{\Omega} \psi \psi. \quad (\text{A.21})$$

with identification  $y^2/M_N = c_5/M_P$ .

## Neutrino masses from seesaw:

$$S_f = \int d^4x \sqrt{-g_J} \left[ -\frac{1}{2} \bar{\psi}_J e_{J\alpha}{}^\mu \gamma^\alpha D_{J\mu} \psi_J - \frac{1}{2} (M_N + y\phi_J) \bar{\psi}_J \psi_J + \frac{c}{\Lambda^2} (\partial_\mu \phi_J^2) J_{JL}^\mu \right]$$

Note that the Dirac and Majorana mass terms change differently as

$$M_N \rightarrow \frac{M_N}{\Omega} = M_N e^{-\frac{1}{\sqrt{6}} \frac{|\phi|}{M_P}}, \quad M_D \rightarrow \frac{y}{\Omega} \phi_J = \frac{y M_P}{\sqrt{\xi}} \left( 1 - e^{-\sqrt{\frac{2}{3}} \frac{|\phi|}{M_P}} \right)^{1/2}.$$

If the origin of neutrino masses is the seesaw mechanism,

$$m_\nu = \frac{M_D^2}{M_N} \rightarrow \frac{y^2 \phi_J^2}{M_N \Omega} = \frac{2y^2 M_P^2}{M_N \xi} \sinh \left( \frac{|\phi|}{\sqrt{6}} \right).$$

# Particle Production in curved spacetime

## ■ Bogoliubov Transformation

- When *adiabaticity conditions* are violated, the definition of the vacuum changes
- Non-zero  $\beta$  coefficient is interpreted as *particle production*
- Particle production (Neutrino) from time dependent classical background (Higgs)

$$(i\partial_\tau + \vec{\sigma} \cdot \vec{k})\nu_L = -\tilde{m}_\nu(i\sigma_2)\nu_L^* - \tilde{\mu}\nu_L$$

$$\alpha'_s(\tau, k) = -\frac{\beta_s(\tau, k)}{2\omega_s^2} [\tilde{m}_\nu \tilde{\mu}' - (sk + \tilde{\mu})\tilde{m}'_\nu] e^{2i \int_0^\tau \omega_s(\tau') d\tau'}$$

$$\beta'_s(\tau, k) = \frac{\alpha_s(\tau, k)}{2\omega_s^2} [\tilde{m}_\nu \tilde{\mu}' - (sk + \tilde{\mu})\tilde{m}'_\nu] e^{-2i \int_0^\tau \omega_s(\tau') d\tau'}$$

- Manifest helicity dependence  $\alpha_s(0, k) = 1$  and  $\beta_s(0, k) = 0$
- Time dependence of neutrino mass is also essential

occupation number  $f_s(t, k)$

$$n_s(t) = \frac{1}{(a(t)/a_{\text{end}})^3} \int \frac{d^3k}{(2\pi)^3} |\beta_s(\tau(t), k)|^2$$

$$n_L|_{\text{reh}} \equiv \lim_{t \rightarrow t_{\text{reh}}} n_\ell(t) - n_{\bar{\ell}}(t)$$

$$\eta_L(t_{\text{reh}}) \equiv \left. \frac{n_L}{n_\gamma} \right|_{\text{reh}} = \frac{\pi^2}{2\zeta(3)} \left. \frac{\tilde{n}_L}{\tilde{T}^3} \right|_{\text{reh}}$$

- transforms to B asymmetry via sphaleron



little more detail ... “standard technique”  
(see appendix )

$$\{a_s(\vec{k}), a_{s'}^\dagger(\vec{k}')\} = (2\pi)^3 \delta_{ss'} \delta(\vec{k} - \vec{k}')$$

$$\nu_L = \int \frac{d^3k}{(2\pi)^3} \sum_{s=\pm 1} \left[ \xi_s(\tau, \vec{k}) a_s(\vec{k}) e^{i\vec{k} \cdot \vec{x}} + \chi_s(\tau, \vec{k}) a_s^\dagger(\vec{k}) e^{-i\vec{k} \cdot \vec{x}} \right]$$

$$\xi_s(\tau, \vec{k}) = u_s(\tau, \vec{k}) h_s(\vec{k}),$$

$$\chi_s^c(\tau, \vec{k}) = v_s(\tau, \vec{k}) h_s(\vec{k})$$

$$u_s(\tau, \vec{k}) = \frac{\alpha_s}{\sqrt{2}} \sqrt{1 - f_s} e^{-i \int_0^\tau \omega_s(\tau') d\tau'} + \frac{\beta_s}{\sqrt{2}} \sqrt{1 + f_s} e^{i \int_0^\tau \omega_s(\tau') d\tau'},$$

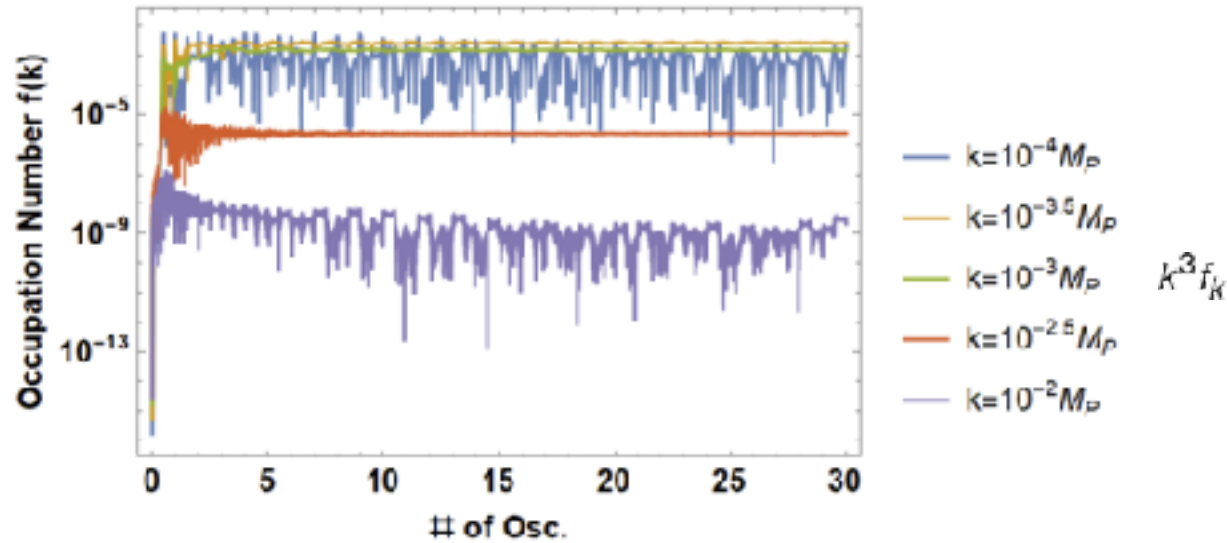
$$v_s(\tau, \vec{k}) = -\frac{\alpha_s}{\sqrt{2}} \sqrt{1 + f_s} e^{-i \int_0^\tau \omega_s(\tau') d\tau'} + \frac{\beta_s}{\sqrt{2}} \sqrt{1 - f_s} e^{i \int_0^\tau \omega_s(\tau') d\tau'},$$

where

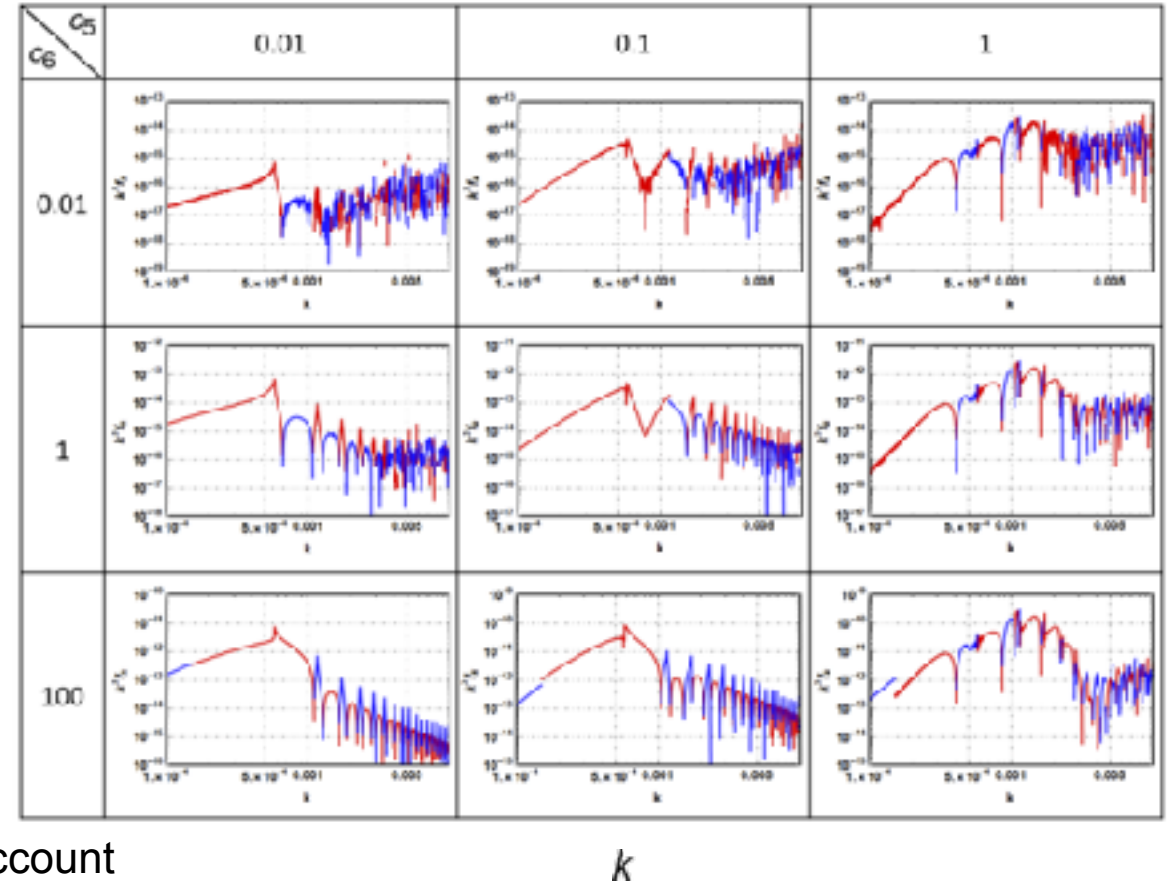
$$\omega_s^2(\tau, \vec{k}) = (k + s\tilde{\mu})^2 + \tilde{m}_\nu^2,$$

$$f_s \equiv \frac{sk + \tilde{\mu}}{\omega_s}.$$

# Lepton Asymmetry



Occupation number for  
particle, anti-particle

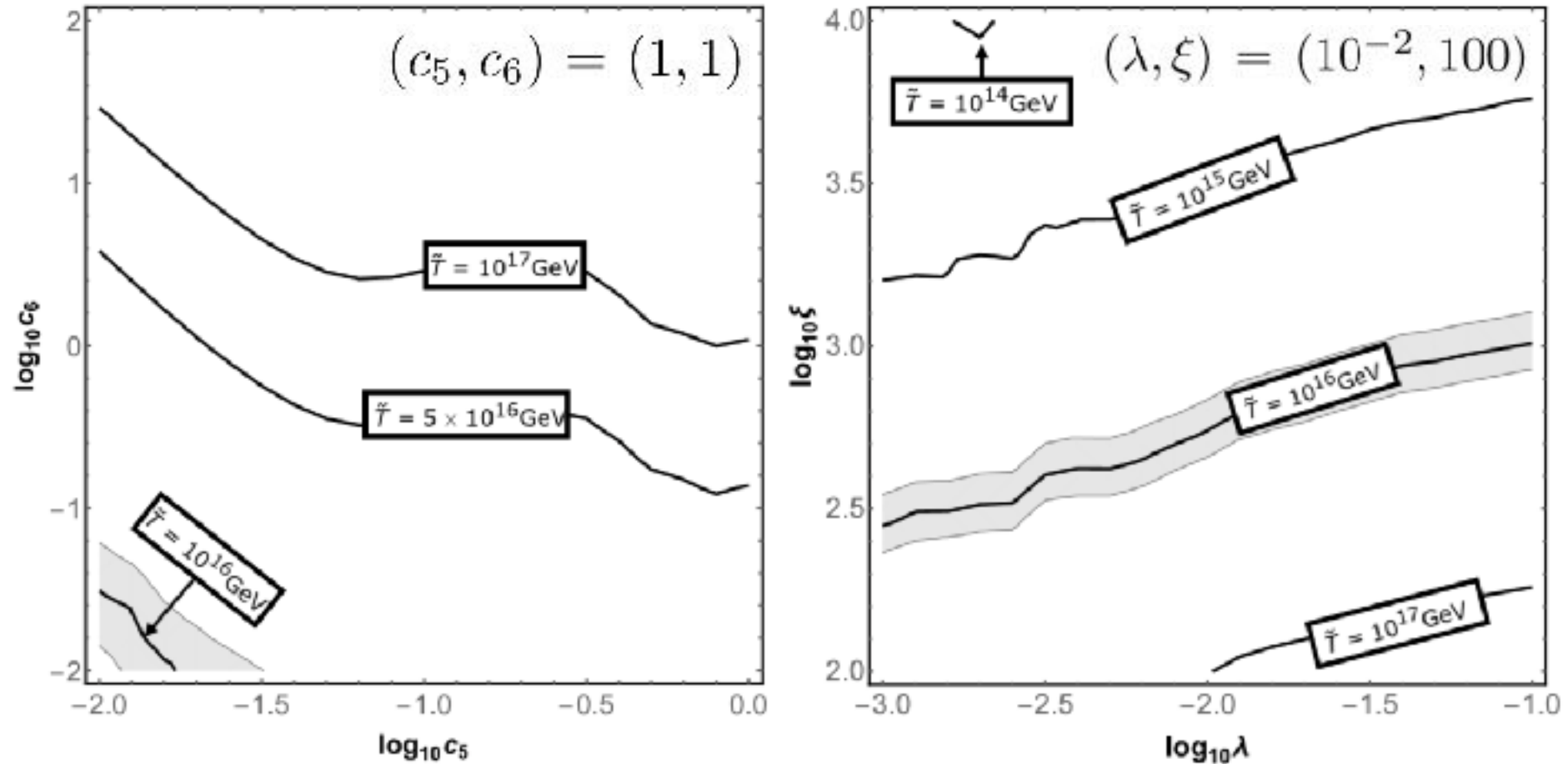


- Perform numerically taking actual inflationary dynamics into account
  - It turned out that almost all asymmetry is produced at early time ( $\leq 5$  osc.)
- Insensitive to the details of late time reheating history

[SML, K. Oda, SC. Park. 2010.07563]

# Results for observed B-asymmetry

$$\eta_B(c_5, c_6, \tilde{T}) \simeq \frac{C_{\text{sphal}}^{(\text{SM})} \pi^2 \tilde{n}_L(c_5, c_6)}{2\zeta(3)\tilde{T}^3}$$



# Summary & Conclusion

- Coherently oscillating Inflaton field provide natural possibility of spontaneous baryogenesis during the reheating.
- With the help of Planck-suppressed higher dimension operators, Higgs inflation *consistently* explains baryon asymmetry with its unique characteristics (e.g. time dependent fermion masses), albeit large reheating temperature with  $10^{15} \text{ GeV} \lesssim aT_{\text{reh}} \lesssim 10^{18} \text{ GeV}$
- Future collider experiments (e.g. top quark mass) and astrophysical observations (e.g. spectral index) will provide direct/indirect probes to our scenario.